



Oxford Cambridge and RSA

Friday 8 October 2021 – Morning

A Level Physics B (Advancing Physics)

H557/01 Fundamentals of Physics

Time allowed: 2 hours 15 minutes



You must have:

- the Data, Formulae and Relationships Booklet

You can use:

- a scientific or graphical calculator
- a ruler (cm/mm)



Please write clearly in black ink. **Do not write in the barcodes.**

Centre number

--	--	--	--	--

Candidate number

--	--	--	--

First name(s)

Last name

StemUp Model Solution

INSTRUCTIONS

- Use black ink. You can use an HB pencil, but only for graphs and diagrams.
- Write your answer to each question in the space provided. If you need extra space use the lined pages at the end of this booklet. The question numbers must be clearly shown.
- Answer **all** the questions.
- Where appropriate, your answer should be supported with working. Marks might be given for using a correct method, even if your answer is wrong.

INFORMATION

- The total mark for this paper is **110**.
- The marks for each question are shown in brackets [].
- Quality of extended response will be assessed in questions marked with an asterisk (*).
- This document has **44** pages.

ADVICE

- Read each question carefully before you start your answer.

2
SECTION A

You should spend a maximum of 40 minutes on this section.

Write your answer for each question in the box provided.

Answer **all** the questions.

- 1** Which expression gives a quantity that can be expressed in watts?
- A** $F s$ where F is the force causing a body to move and s is its displacement
- B** $I^2 R$ where I is the current in a conductor of resistance R
- C** $m v$ where m is the mass of a body moving with velocity v
- D** $V I t$ where V is the potential difference across a conductor and I is the current through it, which passes for time t

Your answer

B

[1]

- 2** The camera in a smartphone contains a CCD detector of 1136 pixels × 640 pixels. Each pixel records in full RGB colour, encoded into three bytes of memory.

How much information is recorded in one image from the camera?

- A** 90.9 kbits
- B** 727 kbits
- C** 5.82 Mbits
- D** 17.4 Mbits

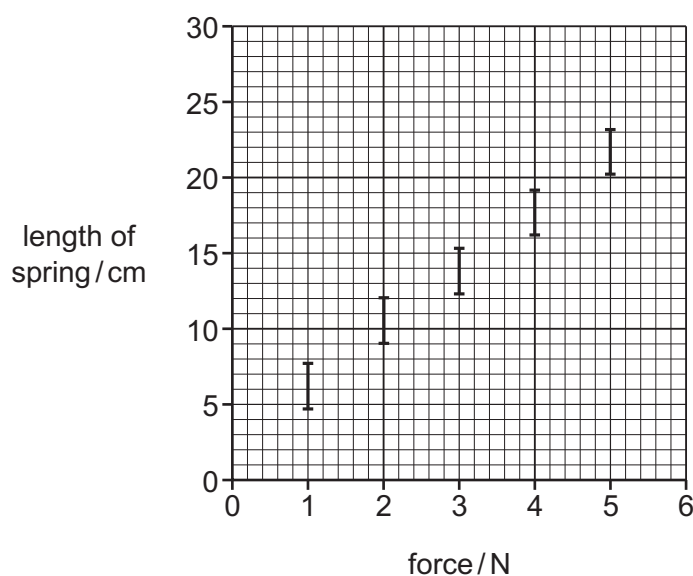
Your answer

D

[1]

The following information is for use in questions 3 and 4.

A series of experiments on stretching a spring gave the data plotted in this graph. Analysis of the graph gives the information in the box.



Best-fit gradient $m = 3.81$
 Max gradient $m_a \approx 4.5$
 Min gradient $m_b \approx 3.2$
 $m_a - m \approx m - m_b \approx 0.6$ to 0.7
 y-axis intercept = 2.57

- 3 Using the information in the box, which is the best estimate of the gradient of the graph, together with its uncertainty?

- A $3.8 \pm 0.7 \text{ cm N}^{-1}$
- B $3.8 \pm 1.4 \text{ cm N}^{-1}$
- C $3.81 \pm 0.35 \text{ cm N}^{-1}$
- D $4 \pm 2 \text{ cm N}^{-1}$

Your answer

A

[1]

- 4 Which is the best estimate of the unstretched length of the spring?

- A 0.5 cm
- B 2.6 cm
- C 4.5 cm
- D 7.5 cm

Your answer

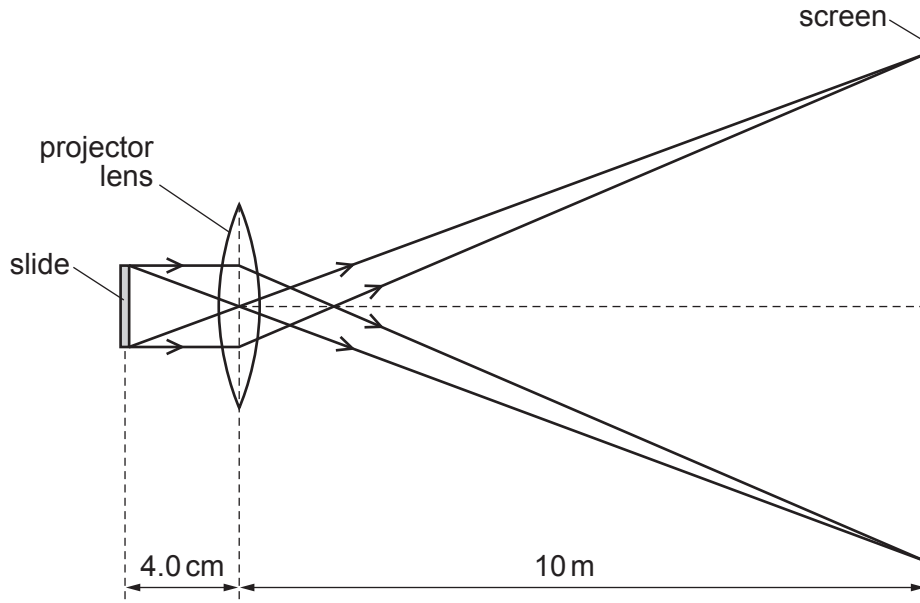
B

[1]

The following information is for use in questions 5 and 6.

The diagram shows a slide projector producing a magnified image on a distant screen. The slide is fixed in position and the lens and screen can be moved.

The slide is 4.0 cm from the lens and the screen is 10 m from the lens.



5

5 Which adjustments need to be made to produce a more magnified image?

	Screen	Lens
A	closer to the lens	closer to the slide
B	closer to the lens	further from the slide
C	further from the lens	closer to the slide
D	further from the lens	further from the slide

Your answer

C

[1]

6 The power of the projecting lens in dioptries, D is

A 0.040

B 0.071

C 25.0

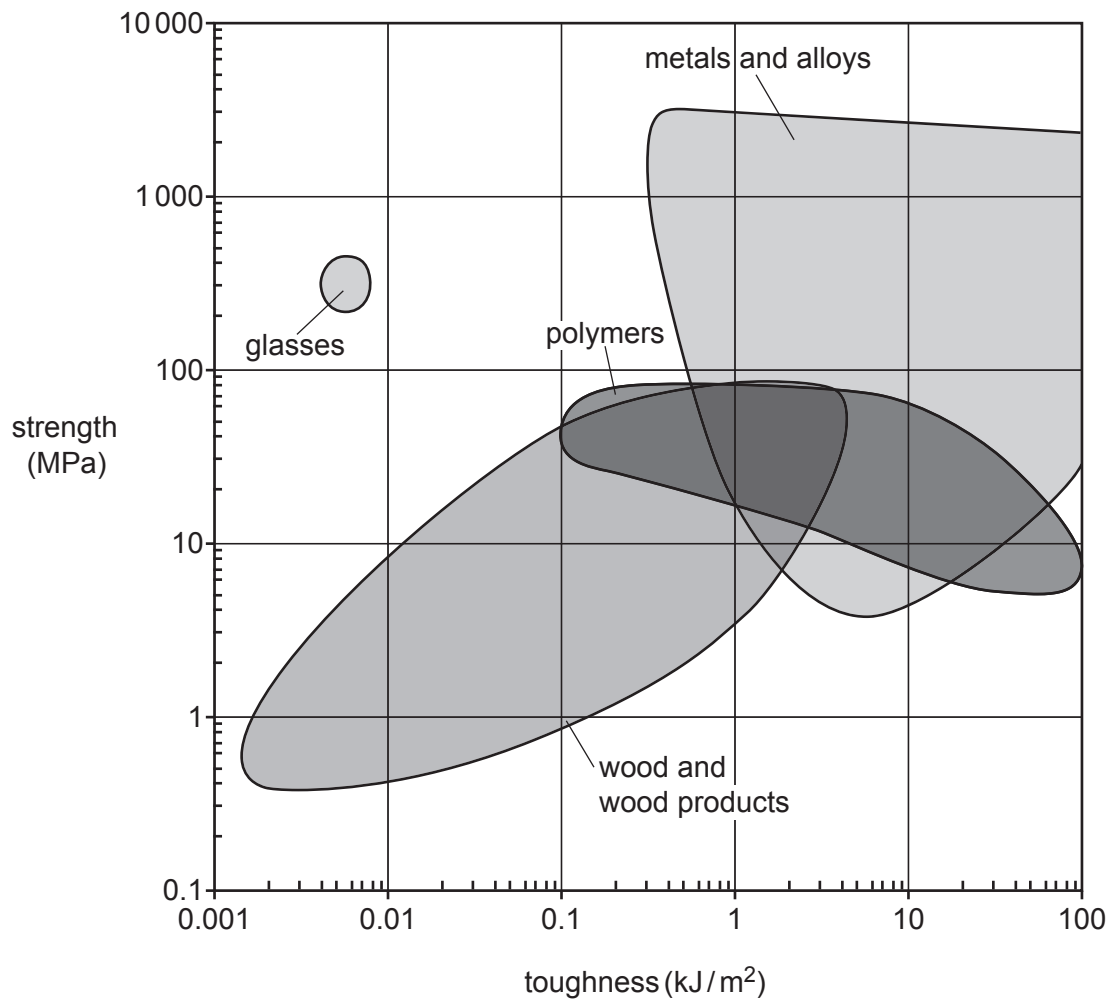
D 25.1

Your answer

D

[1]

7 The chart displays the strength and toughness of various materials.



Which type of material is weak and brittle?

- A glasses
- B metals and alloys
- C polymers
- D wood and wood products

Your answer

D

[1]

- 8 The following three statements were made by students to explain the relationship between current I in an ohmic resistor and the p.d. V across it.

- 1 I is directly proportional to V
- 2 I and V are positively correlated
- 3 the ratio I/V becomes smaller as V increases

Which statements are correct?

- A 1, 2 and 3 are correct
- B only 1 and 2 are correct
- C only 2 and 3 are correct
- D only 1 is correct

Your answer

B

[1]

- 9 The planet Mercury has an orbital period of 88.0 Earth days.

The mean angular velocity of its orbit, in rad s^{-1} , is

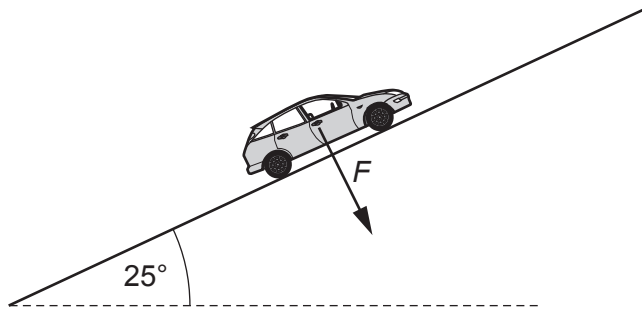
- A 4.13×10^{-7}
- B 8.26×10^{-7}
- C 4.73×10^{-5}
- D 4.96×10^{-5}

Your answer

B

[1]

- 10 A car of mass 1100 kg moves up a hill of gradient 25° .



The force F is a component of the weight of the car.
What is the value of F , to 2 significant figures?

- A 4600 N
- B 9800 N
- C 12 000 N
- D 26 000 N

Your answer

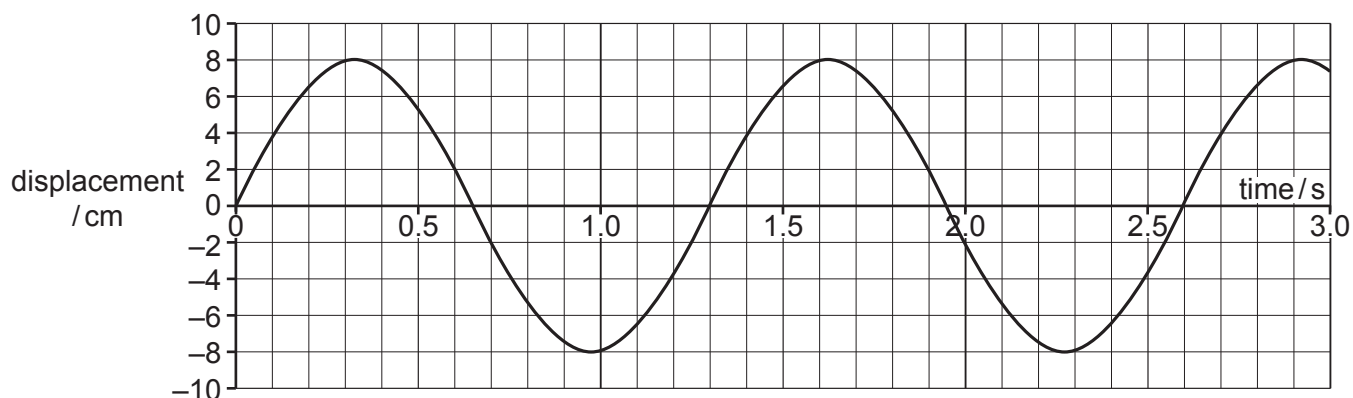
B

[1]

The following information is for use in questions 11 and 12.

The questions are about the oscillation of an object suspended on a spring.

The graph shows the variation in displacement with time from its equilibrium position when the object is pulled down and released.



11 The maximum speed of the oscillating object is

- A 0.08 ms^{-1}
- B 0.24 ms^{-1}
- C 0.39 ms^{-1}
- D 39 ms^{-1}

Your answer

C

[1]

12 The mass of the oscillating object is 600 g.

The spring constant k of the spring is

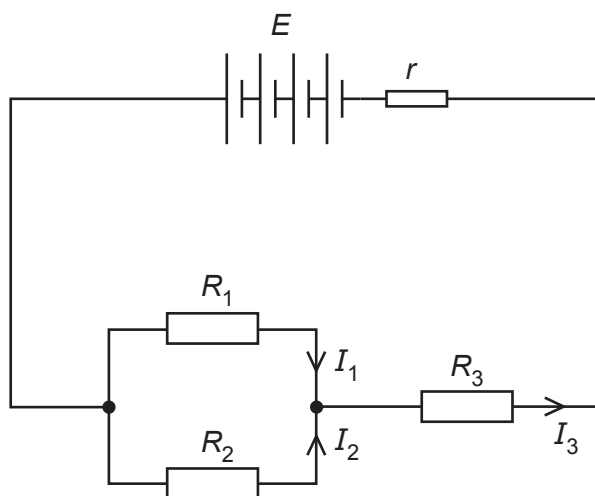
- A 14 N m^{-1}
- B 18 N m^{-1}
- C 56 N m^{-1}
- D $14\,000 \text{ N m}^{-1}$

Your answer

A

[1]

- 13 Kirchhoff's Second Law states that the sum of the potential differences around any closed loop in the circuit must be zero.



Here are three statements about the circuit above.

- 1 $I_3 r < E$
- 2 p.d. across R_1 = p.d. across R_2
- 3 p.d. across $R_2 < \text{p.d. across } R_3$

Which statements follow directly from Kirchhoff's Second Law?

- A** 1, 2 and 3
B only 1 and 2
C only 2 and 3
D only 1

Your answer

B

[1]

- 14 Kirchhoff's First Law states that the sum of currents going into a junction is equal to the sum of currents coming out of that junction. Which conservation law is this equivalent to?

- A** conservation of charge
B conservation of energy
C conservation of mass
D conservation of momentum

Your answer

A

[1]

- 15 A ball is thrown vertically upwards with an initial velocity of 24 ms^{-1} and is caught by the thrower a time t later.

To an **appropriate number** of significant figures, the time t is

- A 2.4 s
- B 2.45 s
- C 4.89 s
- D 4.9 s

Your answer

D

[1]

- 16 A charged capacitor discharges through a resistor with the time constant $\tau = RC$. What is the best explanation of the time constant τ ?

- A τ is the time for the charge stored to become half of its initial value
- B τ is the time for the current from the capacitor to become one-third of its initial value
- C τ is the time for the energy stored to become half of its initial value
- D τ is the time for the p.d. across the capacitor to become $\frac{1}{e}$ of its initial value

Your answer

D

[1]

- 17 What is the gain in potential when rising 1000 km above the surface of the planet Mars?

Mass of Mars = $6.4 \times 10^{23} \text{ kg}$

Radius of Mars = 3400 km

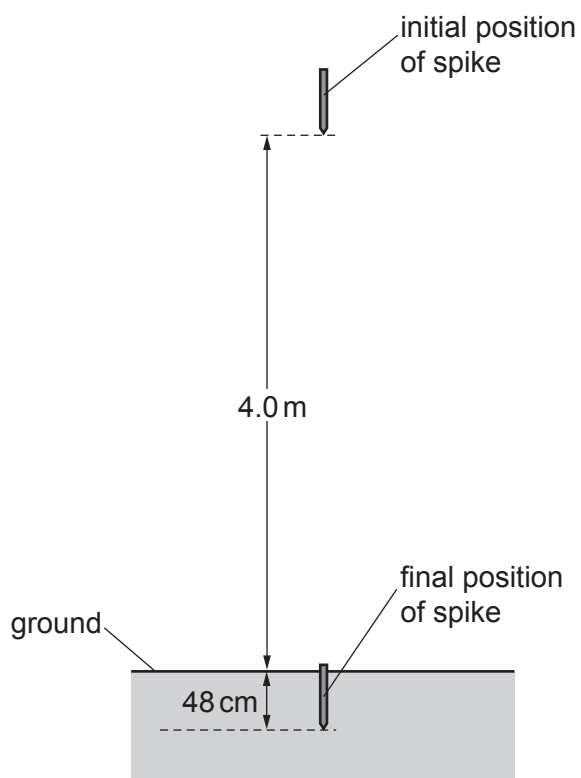
- A $2.9 \times 10^6 \text{ J kg}^{-1}$
- B $9.7 \times 10^6 \text{ J kg}^{-1}$
- C $1.3 \times 10^7 \text{ J kg}^{-1}$
- D $2.9 \times 10^9 \text{ J kg}^{-1}$

Your answer

A

[1]

- 18 A metal spike of mass 2.8 kg is dropped onto level ground from a height of 4.0 m , measured from the point of the spike. It penetrates into the ground a distance of 48 cm .



What is the mean force exerted on the spike by the ground as it penetrates?

- A 2.3 N
- B 82 N
- C 230 N
- D 260 N

Your answer

C

[1]

- 19 A muon of rest energy $= 106\text{ MeV}$ is travelling at a speed of $0.99c$. The total energy of the muon is

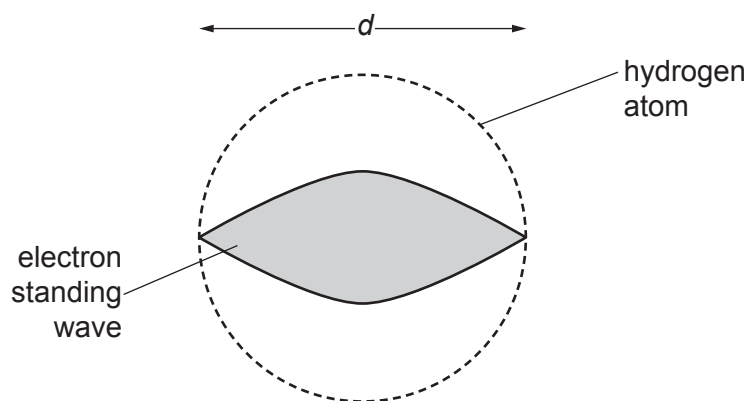
- A 133 MeV
- B 249 MeV
- C 751 MeV
- D 5330 MeV

Your answer

C

[1]

- 20 The hydrogen atom can be modelled as an electron standing wave. One simple version has one 'loop' of the standing wave fitting in the diameter of the atom, as shown in the diagram.



The atom is 'squeezed' so that the diameter d becomes smaller.

Here are three statements about the change to the electron.

- 1 The electron momentum increases.
- 2 The electron kinetic energy increases.
- 3 The electron potential energy becomes more negative.

Which statements are correct?

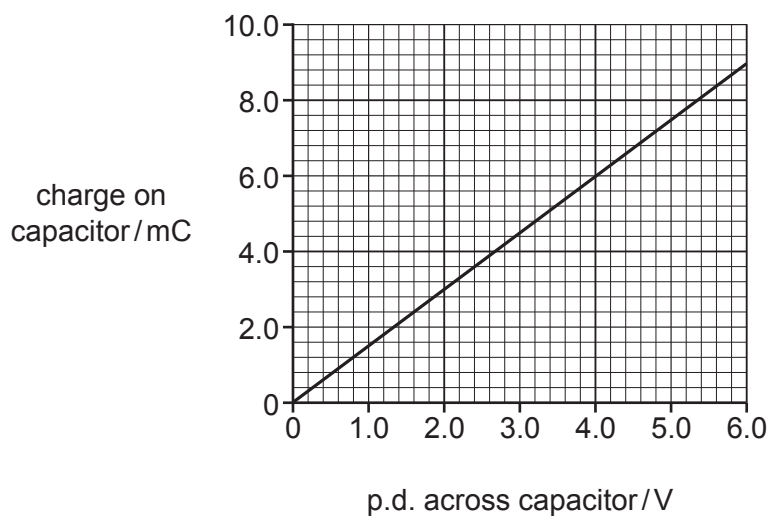
- A** 1, 2 and 3 are correct
- B** only 1 and 2 are correct
- C** only 2 and 3 are correct
- D** only 1 is correct

Your answer

A

[1]

- 21 The graph shows the variation of the charge on a capacitor with the potential difference across that capacitor.



The capacitor is initially uncharged and the p.d. is gradually increased.
Use the graph to calculate the energy stored by the capacitor when the p.d. is 4.0 V.

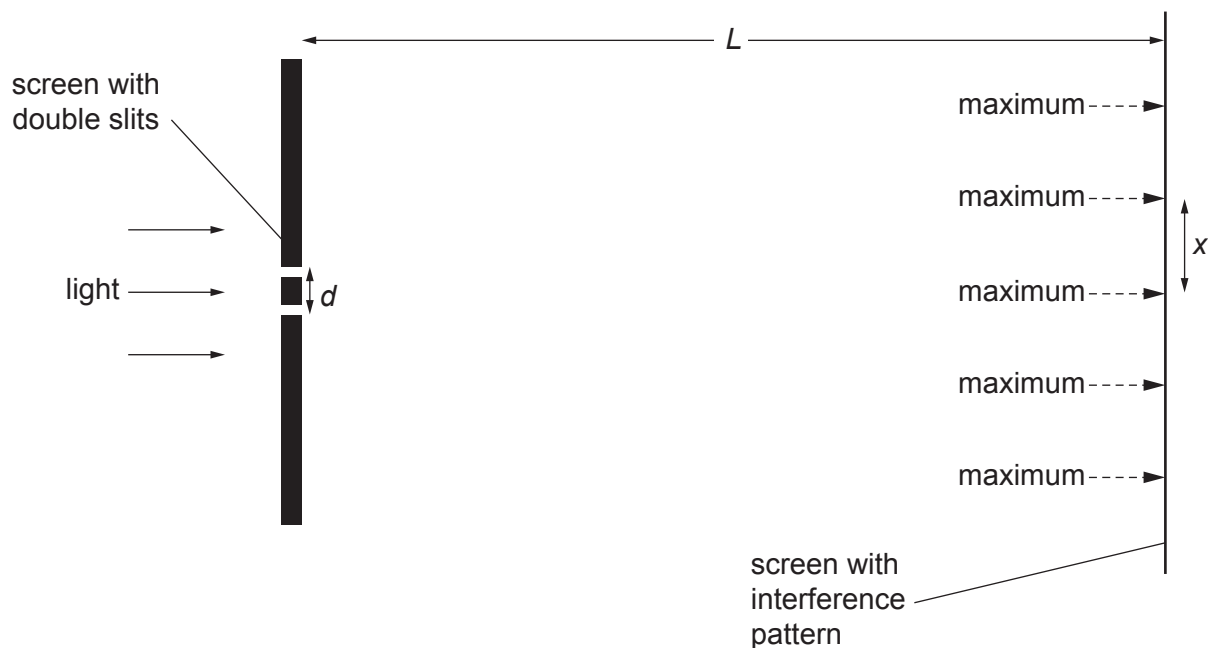
- A 0.012 J
- B 0.024 J
- C 12 J
- D 24 J

Your answer

A

[1]

- 22 Light of frequency f is incident normally on two slits in an opaque screen separated by a distance d . A pattern of maxima and minima is observed on a screen a distance L from the slits. Adjacent maxima are separated by a distance x .



Which of the statements 1, 2 and 3 are correct?

- 1 Doubling L would double x
- 2 Reducing d would increase x
- 3 Increasing f would increase x

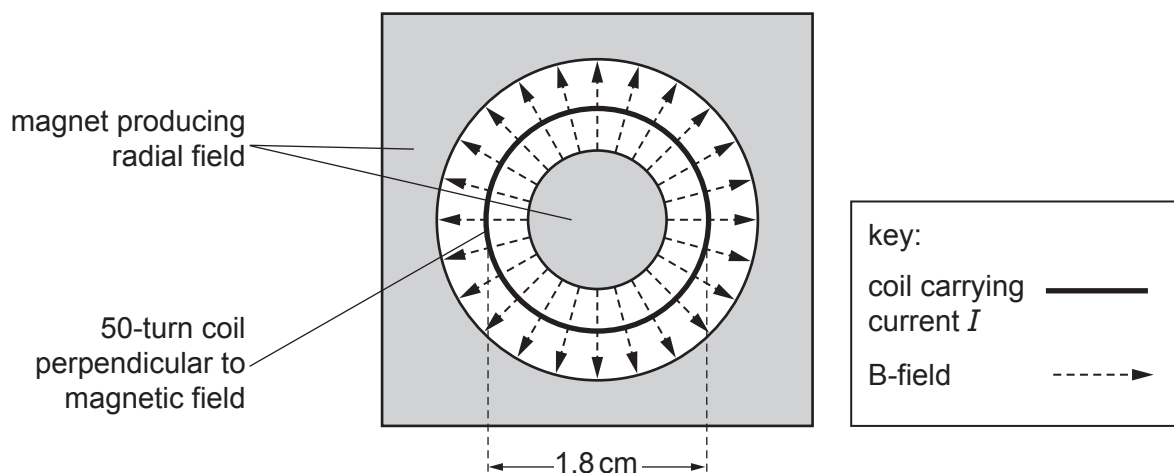
- A** 1, 2 and 3 are correct
- B** only 1 and 2 are correct
- C** only 2 and 3 are correct
- D** only 1 is correct

Your answer

B

[1]

- 23** The diagram is a section through part of an electrical linear motor. The motor contains a 50-turn coil of diameter 1.8 cm carrying a current of 0.16 A in a radial magnetic field of flux density 0.24 T where it meets the coil.



The magnetic force acting on the coil is

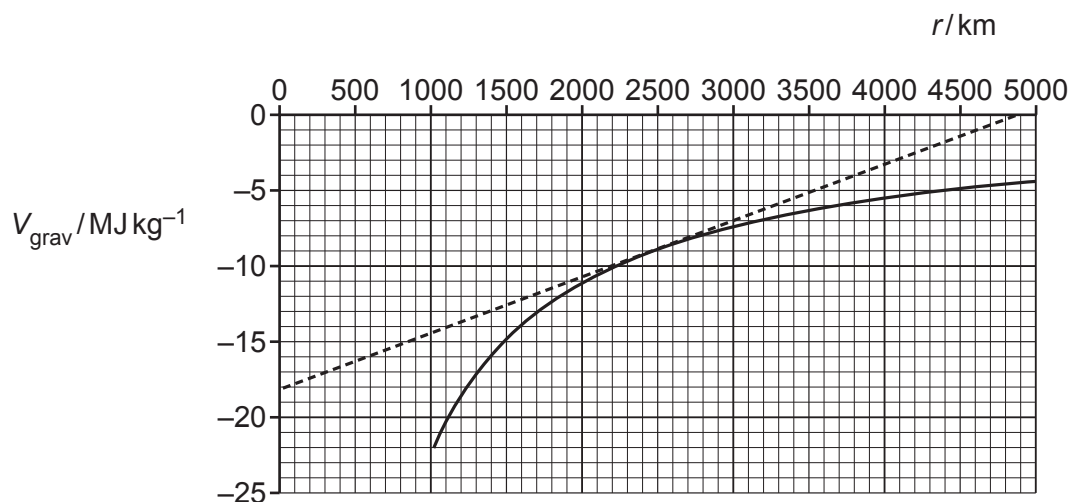
- A** 2.2 mN
- B** 0.11 N
- C** 0.22 N
- D** 11 N

Your answer

B

[1]

- 24 The graph shows the variation of gravitational potential with radial distance r from the centre of the planet Mercury.



The mean radius of Mercury is 2440 km.

The straight line drawn on the graph is the tangent to the curve at this value of r .

From the graph, the magnitude of the gravitational field strength at the surface of the planet is

- A 0.0037 N kg^{-1}
- B 3.7 N kg^{-1}
- C 9.0 N kg^{-1}
- D 18 N kg^{-1}

Your answer

B

[1]

- 25** The distance from the Earth to an asteroid is measured by sending a radar pulse to the asteroid at a known time and recording the time when the return pulse is detected. The data from these measurements are given in the table.

Time pulse is sent	07 hours 59 min 50.0 s
Time return pulse is received	08 hours 00 min 17.2 s

The distance of the asteroid from Earth is

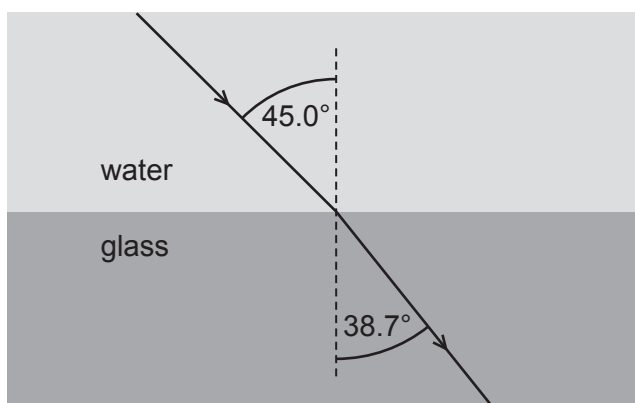
- A** 2.58 Gm
- B** 4.08 Gm
- C** 5.16 Gm
- D** 8.16 Gm

Your answer

B

[1]

- 26 The diagram shows the refraction of a ray of light passing from water into glass.



The refractive index for light travelling from vacuum into water is 1.33.

Which of the following is the speed of light in glass, expressed to **3** significant figures?

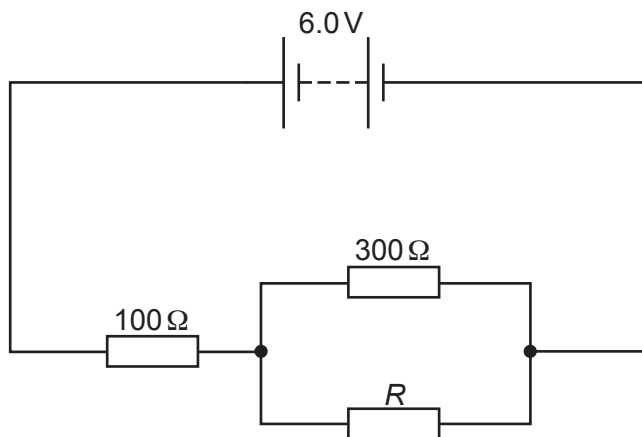
- A $1.99 \times 10^8 \text{ m s}^{-1}$
- B $2.26 \times 10^8 \text{ m s}^{-1}$
- C $2.40 \times 10^8 \text{ m s}^{-1}$
- D $2.65 \times 10^8 \text{ m s}^{-1}$

Your answer

A

[1]

- 27 The diagram shows a combination of three resistors connected to a 6.0V power supply of negligible internal resistance.



A voltmeter connected across resistor R reads 3.0V.
What is the resistance of resistor R ?

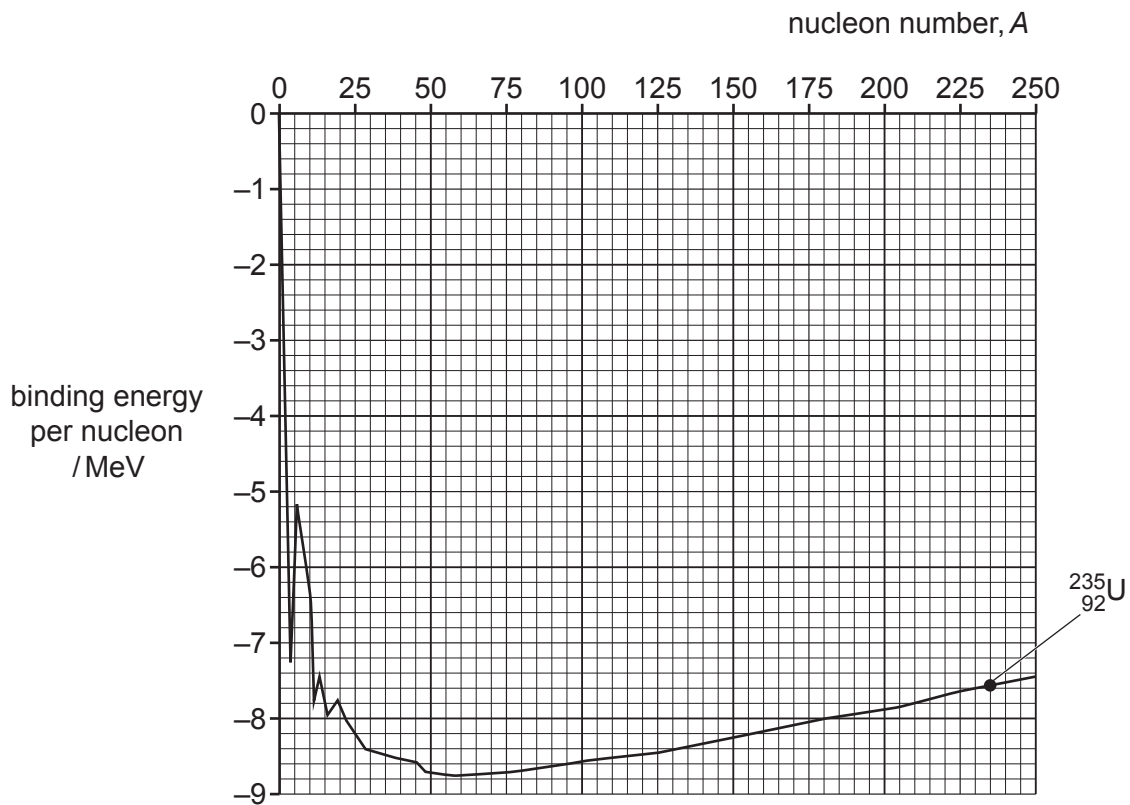
- A $50\ \Omega$
- B $100\ \Omega$
- C $150\ \Omega$
- D $200\ \Omega$

Your answer

C

[1]

28 The graph shows the binding energy per nucleon for different nuclides.



From the graph, what is the energy released when one nucleus of ${}^{235}_{92}\text{U}$ undergoes fission into one nucleus of ${}^{144}_{56}\text{Ba}$, one nucleus of ${}^{89}_{36}\text{Kr}$ and two neutrons?

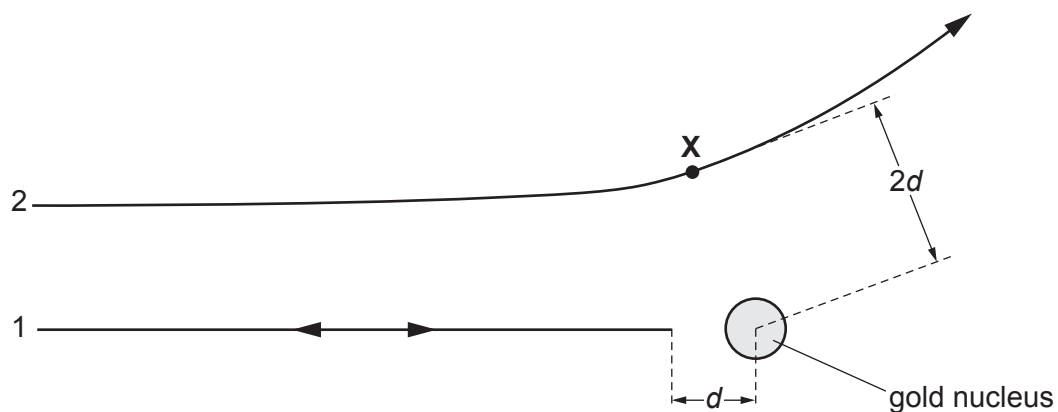
- A 9.3 MeV
- B 170 MeV
- C 1200 MeV
- D 1800 MeV

Your answer

B

[1]

- 29 The diagram shows the path of two alpha particles, each of initial kinetic energy 4.0 MeV, as they are scattered by a gold nucleus.



Alpha particle 1 approaches head-on towards the gold nucleus and is repelled back along its own path, with a closest distance of separation from the nucleus being d .

Alpha particle 2 follows the path shown, with a closest distance of separation from the nucleus being $2d$ at the point **X**.

What is the **kinetic energy** of alpha particle 2 at the point **X**?

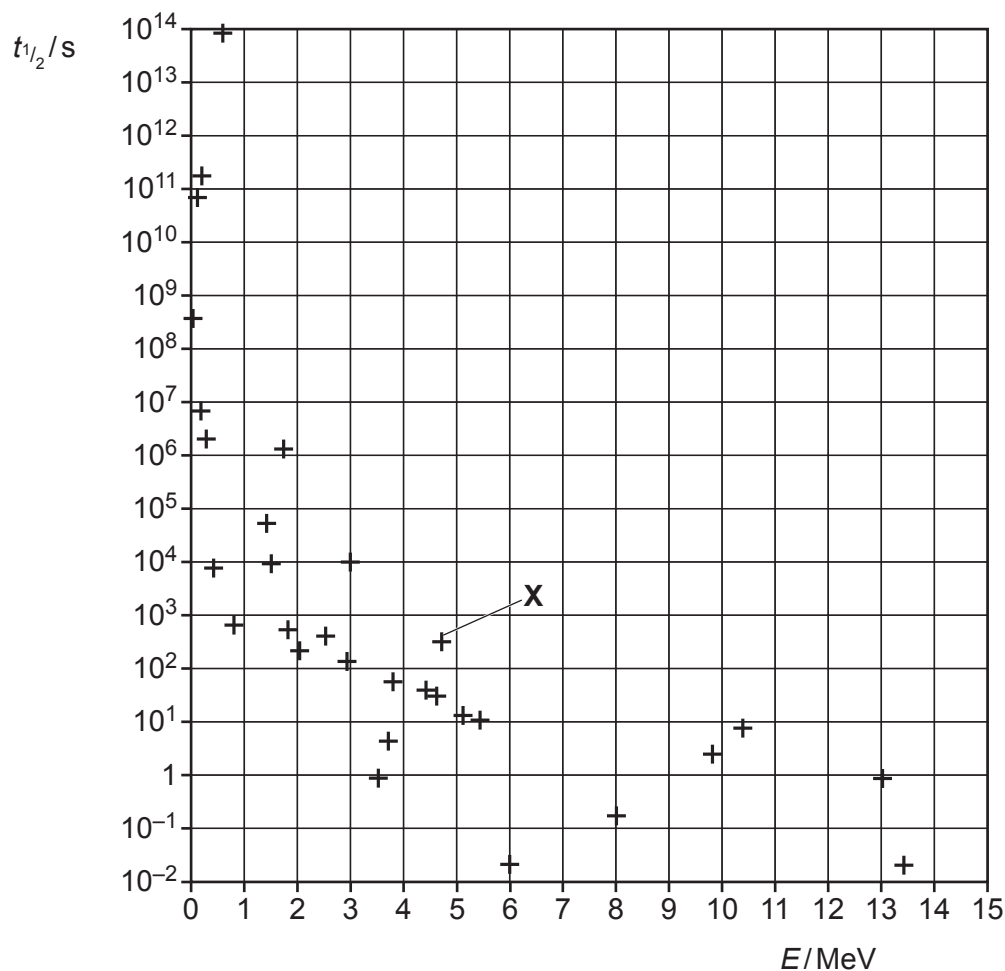
- A 0.0 MeV
- B 2.0 MeV
- C 3.0 MeV
- D 4.0 MeV

Your answer

B

[1]

- 30 The graph shows how the half-life $t_{1/2}$ of different beta-emitting radioactive nuclides varies with the energy E of the emitted beta-particles.



Which one of the following statements is true?

- A Most beta-emitting nuclides have half-lives shorter than a day.
- B Nuclides with shorter half-lives always emit higher energy particles than nuclides with longer half-lives.
- C The half-life is inversely proportional to the particle energy.
- D The nuclide labelled X has a half-life of 150 s.

Your answer

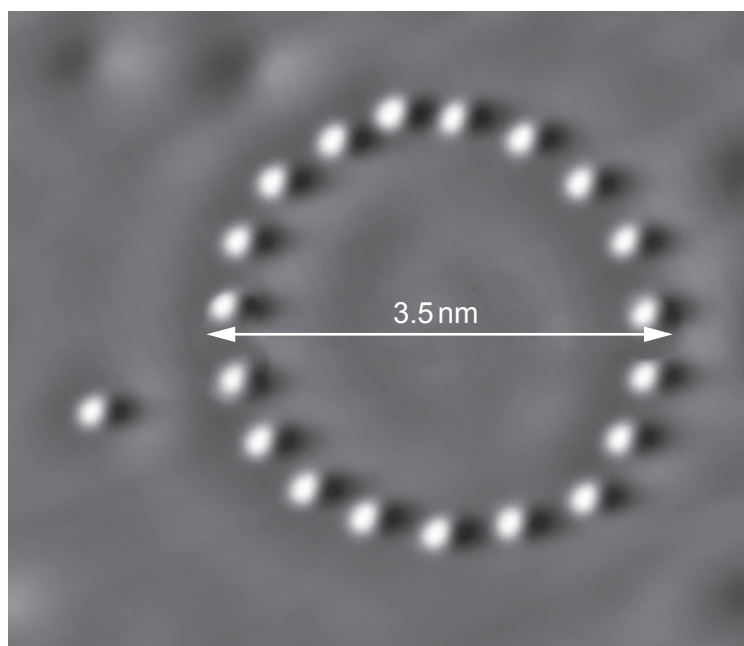
A

[1]

SECTION B

Answer **all** the questions.

- 31 The STM image below shows an open ring of silver atoms.



Use the scaled STM image to estimate the diameter of a silver atom.

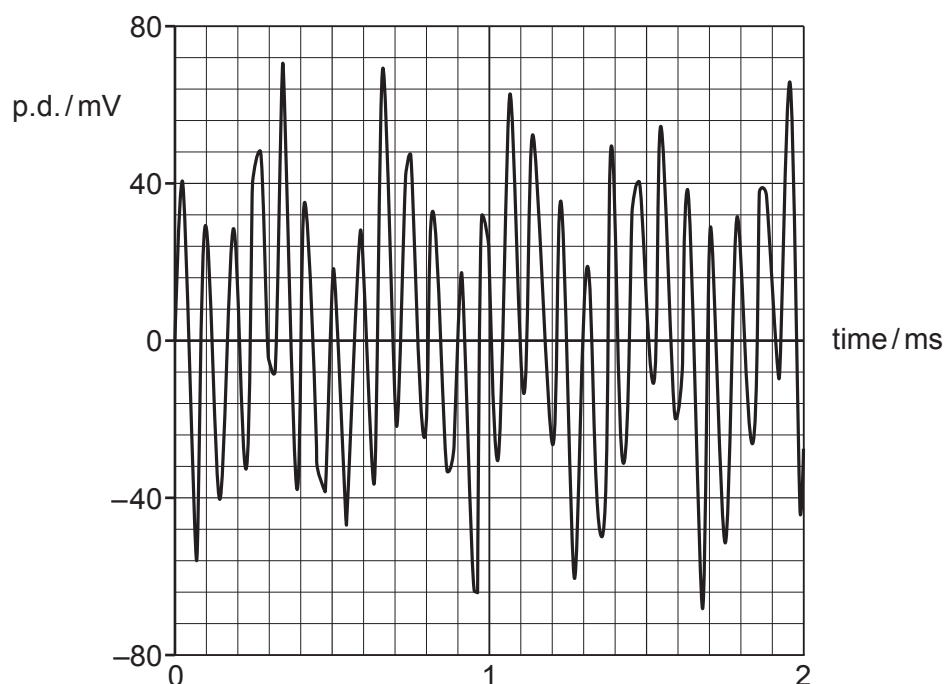
$$\text{circumference of ring} = \pi \times 3.5 = 11.0 \text{ nm}$$

$$\text{the ring holds } 19 \text{ atoms} + 19 \text{ spaces} = 38 \text{ atom widths}$$

$$\text{diameter of atom} = 3.5\pi / 38 = 11.0 / 38 = 0.29 \text{ nm}$$

$$\text{diameter} = \dots 0.29 \dots \text{ nm } [3]$$

- 32 The diagram shows a 2.0 ms interval of a waveform that is to be digitised. The waveform contains noise at the level $V_{\text{noise}} \approx 0.4 \text{ mV}$.



- (a) Explain why the sampling frequency should be at least 25 kHz.

There are about $12\frac{1}{2}$ waves (cycles) in 1 ms, so the highest frequency f_{max} $\approx 12\,500 \text{ Hz}$. At least 2 samples per cycle are needed, so sample at $2 \times 12.5 \text{ kHz} = 25 \text{ kHz}$ or more. [1]

- (b) Suggest and explain the number of bits per sample you would use to digitise this waveform.

$V_{\text{total}} / V_{\text{noise}} \approx 140 / 0.4 = 350$, so about 350 distinguishable levels are needed. $2^8 = 256$ is too few but $2^9 = 512 > 350$ ($\log_2 350 = 8.45$), so use 9 bits per sample. More bits would only record the noise. [2]

- 33** The figures below show evidence of the Hubble law ($v = H_0 d$ where v is the velocity of the galaxy relative to Earth and d is the distance of the galaxy from Earth).

Fig. 33a shows Hubble's original galactic red-shift data (1929). **Fig. 33b** shows evidence from supernovae red-shift data (1998).

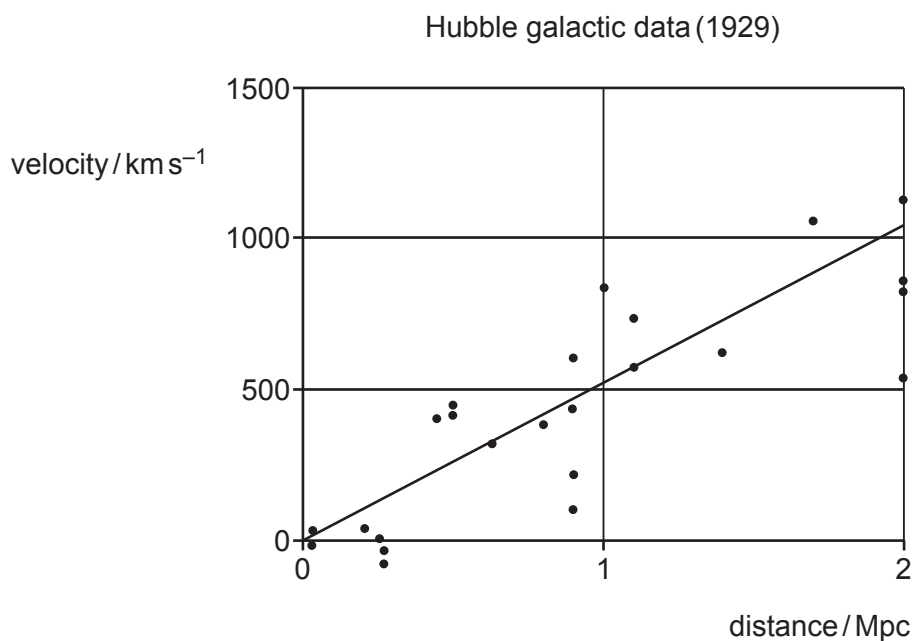


Fig. 33a

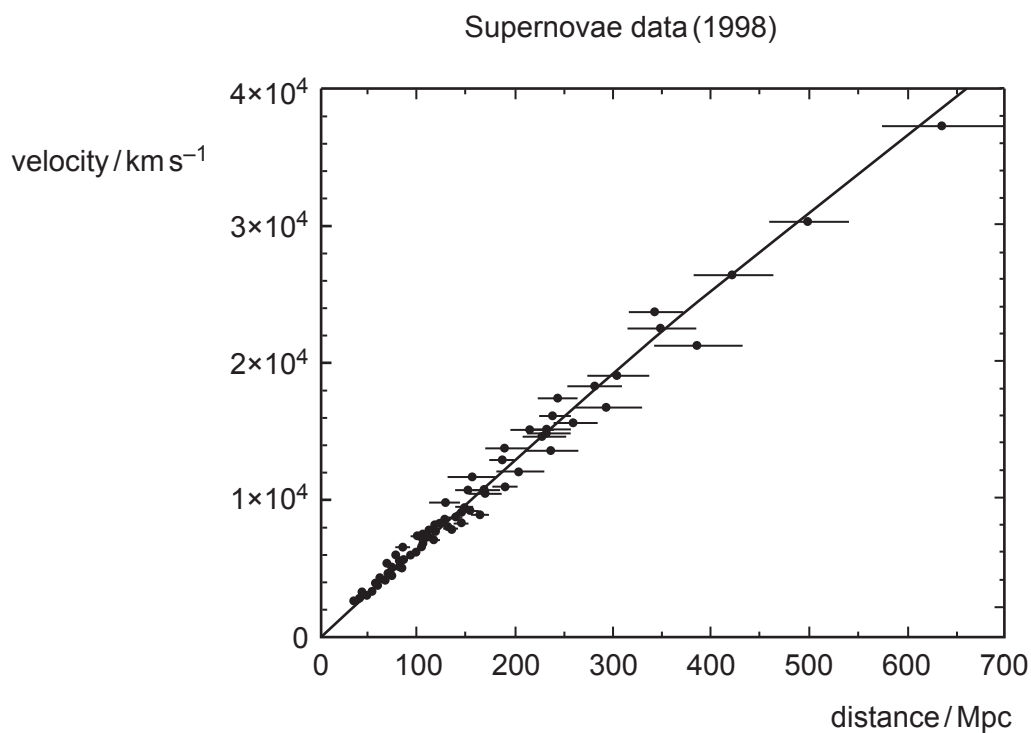


Fig. 33b

- (a) Three of the nearer galaxies in **Fig. 33a** have a negative velocity.

Suggest and explain the effect this has on the wavelength shift for these galaxies.

The wavelengths are shortened (the light is blue-shifted), because these galaxies are moving towards us (approaching the Milky Way), so the emitted waves are bunched up. [2]

- (b) (i) Show from the lines of best fit that the best estimate for the Hubble constant H_0 was more than eight times ($\times 8$) larger in 1929 than in 1998.

$$1929: H_0 = \text{gradient} = 1000 / 1.9 = 526 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

$$1998: H_0 = \text{gradient} = 4 \times 10^4 / 660 = 60.6 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

$$\text{ratio} = 526 / 60.6 = 8.7, \text{ which is more than } 8$$

[2]

- (ii) Show that the data from **Fig. 33b** indicate that the 'big bang' happened more than 10 billion years ago.

$$1 \text{ Mpc (megaparsec)} = 3.1 \times 10^{22} \text{ m}$$

$$\text{age of universe} \approx 1 / H_0 = d / v$$

$$= (660 \times 3.1 \times 10^{22} \text{ m}) / (4 \times 10^7 \text{ m s}^{-1}) = 5.1 \times 10^{17} \text{ s}$$

$$1 \text{ year} = 3.2 \times 10^7 \text{ s, so age} = 5.1 \times 10^{17} / 3.2 \times 10^7$$

$$= 1.6 \times 10^{10} \text{ years (16 billion years)}$$

which is more than 10 billion years

[2]

- 34 In radiotherapy, 'seeds' of radioactive material are implanted in tumours to eliminate cancer cells. Each seed contains a quantity of the isotope ^{125}I with half-life 60 days and initial activity 8.5 MBq.

- (a) Show that the number of atoms of ^{125}I atoms initially present in one seed is about 6×10^{13} .

$$A = \lambda N = (\ln 2 / t_{1/2}) N, \text{ so } N = A t_{1/2} / \ln 2$$

$$t_{1/2} = 60 \times 24 \times 3600 = 5.18 \times 10^6 \text{ s}$$

$$N = 8.5 \times 10^6 \times 5.18 \times 10^6 / 0.693$$

$$N = 6.4 \times 10^{13} \text{ (about } 6 \times 10^{13}\text{)}$$

[2]

- (b) The ^{125}I nucleus emits a γ -ray of energy 35 keV which will be absorbed by about 50 grams of surrounding tissue.

Show that in the first 60 days of irradiation by one implanted seed, the effective dose is about 4 Sv.

quality factor for this radiation = 1

$$\text{in 60 days (one half-life) } N_0 / 2 = 3.2 \times 10^{13} \text{ nuclei decay}$$

$$\text{energy} = 3.2 \times 10^{13} \times 35 \times 10^3 \times 1.6 \times 10^{-19} = 0.18 \text{ J}$$

$$\text{absorbed dose} = 0.18 / 0.050 = 3.6 \text{ Gy; } \times \text{ quality factor } 1$$

$$\text{effective dose} = 3.6 \text{ Sv (about 4 Sv)}$$

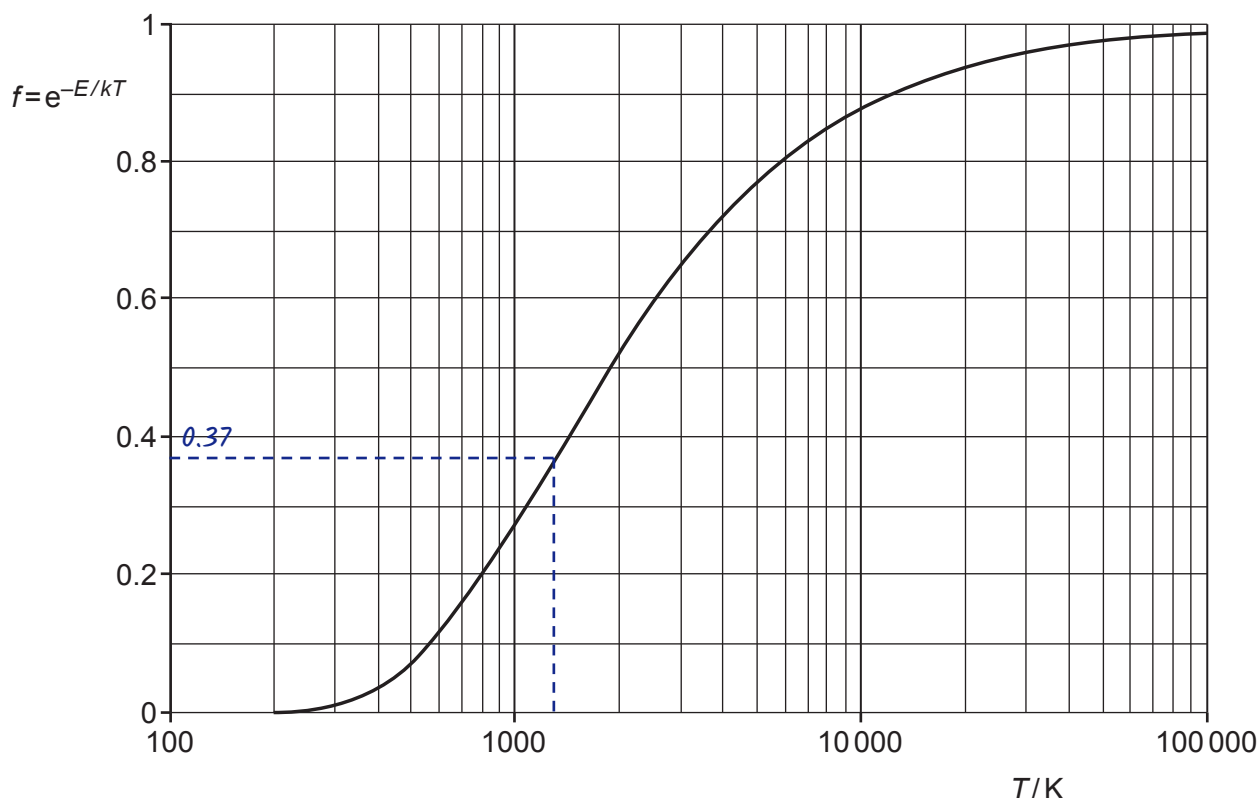
[2]

- (c) Seeds are implanted into cancer masses and remain there for many half-lives.

Suggest why implanting many seeds throughout a 50 gram cancer may be better than implanting one larger seed at its centre.

Cells nearer a seed receive a higher dose than cells farther away (γ -rays absorbed and spread out, $1/r^2$), so many seeds give more even irradiation of the whole cancer. [1]

- 35 The graph shows how the Boltzmann factor f varies with temperature T for a process requiring activation energy E .



- (a) Use the graph to estimate the temperature T when $E = kT$ for this process.

when $E = kT$, $f = e^{-E/kT} = e^{-1} = 0.37$

reading across from $f = 0.37$ to the curve and down:

$T \approx 1300$ K

temperature $T = \dots 1300 \dots$ K [2]

- (b) Explain why the process completes at this temperature, but may occur at a significant rate at temperatures as low as $\frac{T}{20}$.

At T the average molecule has energy $kT = E$, so most can perform the process. At $T/20$, $f = e^{-20} \approx 2 \times 10^{-9}$; only a tiny fraction have enough energy, but there are so many collisions (attempts) per second that the rate is significant. [2]

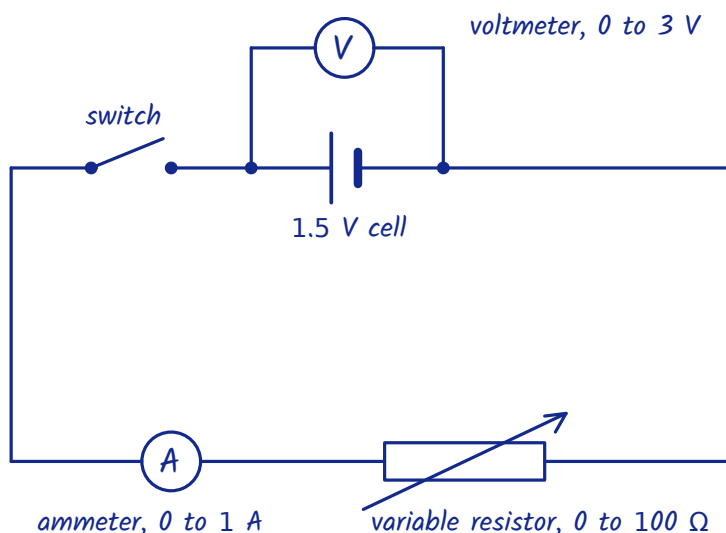
SECTION C

Answer **all** the questions.

36 This question considers the internal resistance of chemical cells.

(a)* Explain how you would practically measure the internal resistance of a 1.5 V cell.

Include in your answer a circuit diagram of components with appropriate values, and your method of what readings to take and how to analyse them to find the internal resistance. [6]



Connect the circuit shown: the cell in series with a switch, an ammeter (0 to 1 A) and a variable resistor (0 to 100 Ω , or at least five fixed resistors from 10 to 100 Ω), with a high resistance voltmeter (0 to 3 V) across the cell terminals.

With the switch open (no current) read the voltmeter: this gives the e.m.f. $\mathcal{E}$. Close the switch with the maximum load resistance and record V and I in a table. Decrease the load resistance in steps so the values of V and I are roughly evenly spaced, taking at least six pairs, down to a very small load.

Open the switch between readings to rest the cell.

Analysis: $V = \mathcal{E} - Ir$. Plot V (y-axis) against I (x-axis) and draw a straight line of best fit. Gradient = $-r$, so $r = -\text{gradient}$ (intercept = $\mathcal{E}$), or calculate $r = (\mathcal{E} - V) / I$ for each pair. Draw the steepest and shallowest lines to estimate the uncertainty in r .

- (b) A lithium-ion rechargeable cell has an e.m.f. of 4.2 V.
The cell is rated at 9 Ah (Ampere × hours).

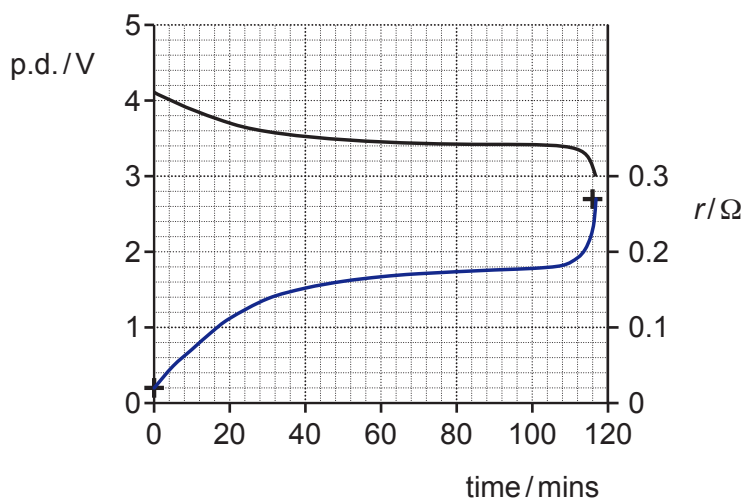
(i) Show that the unit Ah is a unit of charge.

$$\text{charge} = \text{current} \times \text{time}; Q = It$$

$$1 \text{ A h} = 1 \text{ A} \times 3600 \text{ s} = 3600 \text{ A s} = 3600 \text{ C, so A h is a unit of charge}$$

[1]

- (ii) The graph shows the potential difference of the cell against time as it completely discharges at a constant load current of 4.5 A.



The internal resistance of the fully charged cell is 0.02 Ω . The internal resistance rises to 0.27 Ω when the cell is fully discharged.

The resistance scale is at the right side of the graph and the initial and final values are marked with +.

Add a curve to the graph which shows how the internal resistance changes with time.

Assume that any p.d. dropped by the cell is due to its internal resistance.

[2]

- (iii) Estimate the number of moles of lithium Li^+ ions that are needed to store the amount of charge delivered by this cell.

$$\text{one mole} = 6.0 \times 10^{23} \text{ ions}$$

$$N = It / (N_A e) = 4.5 \times 116 \times 60 / (6.0 \times 10^{23} \times 1.6 \times 10^{-19})$$

$$= 31\,300 \text{ C} / 96\,000 \text{ C mol}^{-1} = 0.33 \text{ moles}$$

number of moles = ... 0.33 ... [2]

37 Fig. 37.1 shows trolleys **A** and **B** set up on a friction compensated runway to investigate collisions.

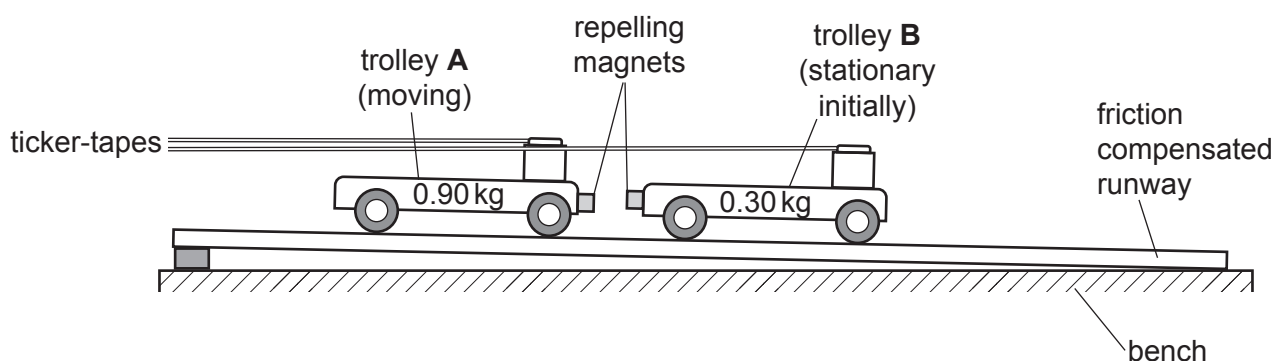


Fig. 37.1

(a) State what is meant by a friction compensated runway.

The runway is tilted slightly so that the component of gravity down the slope balances friction: no resultant force, so a trolley moves at constant speed.

[1]

(b)* Trolley **A** has mass 0.90 kg and trolley **B** has mass 0.30 kg. Trolley **A** travels down the runway at constant speed into the stationary trolley **B**. Repelling magnets fixed to the trolleys ensure they do not make physical contact.

Both trolleys are attached to ticker-tapes onto which 50 dots per second are printed. The ticker-tapes of the collision are shown in Fig. 37.2. The time between printed dots is 0.02 s.

The tapes have been divided into '5-tick strips' before and after the collision representing time intervals of 0.10 s.

ticker-tape **A**



ticker-tape **B**



Fig. 37.2

Analyse the ticker-tapes to compare the motion of the two trolleys. Include discussion of the conservation of momentum and kinetic energy and of the force on each trolley during the collision.

You may assume the collision impulse lasts for 0.060 s. The tape images are life-size.

[6]

Each 5-tick strip is 0.10 s. Tape A before: 80 mm, so $v_A = 0.080 / 0.10 = 0.80 \text{ m s}^{-1}$. Tape A after: 40 mm, so 0.40 m s^{-1} . Tape B after: 120 mm, so $v_B = 1.20 \text{ m s}^{-1}$. A slows down but keeps moving forwards; B starts from rest and moves off faster than A, both at constant speed after the collision.

Momentum: before = $0.90 \times 0.80 = 0.72 \text{ kg m s}^{-1}$. After = $0.90 \times 0.40 + 0.30 \times 1.20 = 0.36 + 0.36 = 0.72 \text{ kg m s}^{-1}$. Momentum is conserved (within the uncertainty of the measurements), as it should be in all collisions.

Kinetic energy: before = $\frac{1}{2} \times 0.90 \times 0.80^2 = 0.288 \text{ J}$. After = $\frac{1}{2} \times 0.90 \times 0.40^2 + \frac{1}{2} \times 0.30 \times 1.20^2 = 0.072 + 0.216 = 0.288 \text{ J}$. KE is also conserved (within uncertainty), so the collision is perfectly elastic. KE is not always conserved in collisions, only in elastic ones.

Forces: by Newton's third law the forces on A and B are equal in size and opposite in direction. Force on B = $\Delta(mv) / \Delta t = 0.30 \times 1.20 / 0.060 = 6.0 \text{ N}$ forwards (to the right). Force on A = $0.90 \times (0.40 - 0.80) / 0.060 = -6.0 \text{ N}$, so 6.0 N backwards (to the left).

Additional answer space if required

.....

.....

.....

.....

.....

.....

- (c) A high-pressure fire hose has a tapered nozzle as shown in **Fig. 37.3**.

The nozzle is reduced from diameter $D_1 = 75 \text{ mm}$ to diameter $D_2 = 25 \text{ mm}$.
Water enters the nozzle at point **E** at velocity v_1 and leaves at point **F** with velocity v_2 .

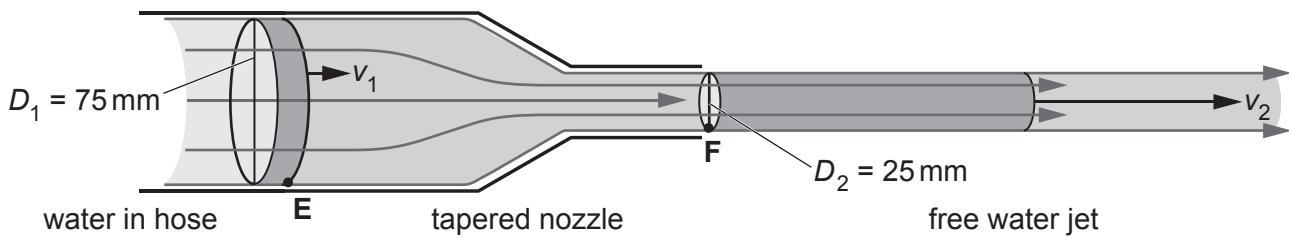


Fig. 37.3

- (i) Explain why $v_2 = 9 v_1$.

Water is incompressible, so the volume flow rate Av must stay constant through the nozzle.
 $A \propto D^2$. $D_2 = D_1 / 3$, so $A_2 = A_1 / 9$. Then $A_1 v_1 = (A_1 / 9) v_2$, so $v_2 = 9 v_1$. [2]

- (ii) The hose can deliver $0.020 \text{ m}^3 \text{ s}^{-1}$ of water.

Calculate the velocity v_1 of water entering the nozzle.

$$\text{volume flow rate} = A_1 v_1 = (\pi D_1^2 / 4) v_1 = 0.020$$

$$v_1 = 0.020 \times 4 / (\pi \times 0.075^2) = 0.020 / 4.42 \times 10^{-3}$$

$$v_1 = 4.53 \text{ m s}^{-1}$$

$$v_1 = \dots 4.5 \dots \text{ ms}^{-1} \quad [2]$$

- (iii) Show that the force on the nozzle is about 700 N.

Use $0.020 \text{ m}^3 \text{ s}^{-1}$ is equivalent to 20 kg s^{-1} for water

$$\text{force} = \text{rate of change of momentum of water in nozzle} = (\Delta m / \Delta t) \Delta v$$

$$= 20 \times (v_2 - v_1) = 20 \times (9 - 1) \times 4.53$$

$$= 20 \times 8 \times 4.53 = 724 \text{ N (about 700 N)}$$

[2]

38 (a) This question is about the electric field strength E near to a proton leading to the Bohr model for the hydrogen atom.

- (i) Show by calculation that E is about $1 \times 10^{12} \text{ V m}^{-1}$ at distance $40 \times 10^{-12} \text{ m}$ from the centre of the proton.

$$\begin{aligned}
 E &= ke / r^2 \\
 &= 8.98 \times 10^9 \times 1.6 \times 10^{-19} / (40 \times 10^{-12})^2 \\
 &= 0.90 \times 10^{12} \text{ V m}^{-1} \text{ (about } 1 \times 10^{12} \text{ V m}^{-1})
 \end{aligned}$$

[2]

- (ii) Fig. 38.1 shows the electric field strength E near to a proton.

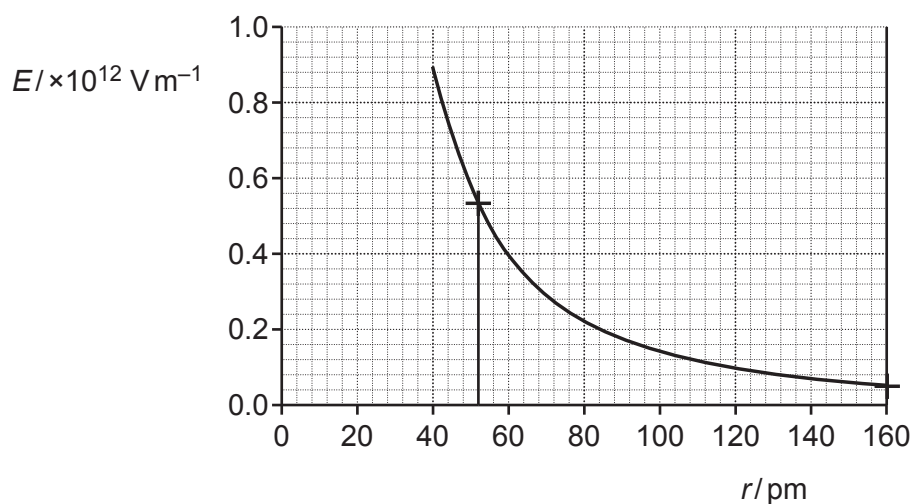


Fig. 38.1

Use any two points on the graph to show that the electric field strength E follows an inverse square law with distance r (a law of the form: $E \propto 1/r^2$).

$$\begin{aligned}
 40 \text{ pm: } Er^2 &= 0.90 \times 10^{12} \times (40 \times 10^{-12})^2 = 1.44 \times 10^{-9} \\
 80 \text{ pm: } Er^2 &= 0.22 \times 10^{12} \times (80 \times 10^{-12})^2 = 1.41 \times 10^{-9} \\
 Er^2 &\text{ is (sensibly) constant, so } E \propto 1/r^2
 \end{aligned}$$

[2]

- (iii) State what the area under the graph between two r values represents and make an estimate of its value between the marked r values 52 and 160 pm.

Area represents potential difference, ΔV

$$\begin{aligned}
 \Delta V &= ke (1/r_1 - 1/r_2) = 8.98 \times 10^9 \times 1.6 \times 10^{-19} \times (1/52 - 1/160) \times 10^{12} \\
 &= 27.7 - 9.0 = 18.7 \text{ V (by counting squares: 1 big square = 4 V)}
 \end{aligned}$$

value of area = 19 units V [2]

- (b) In the Bohr model of the atom the electron travels at speed v in a circular orbit of radius r around the proton as shown in **Fig. 38.2**.

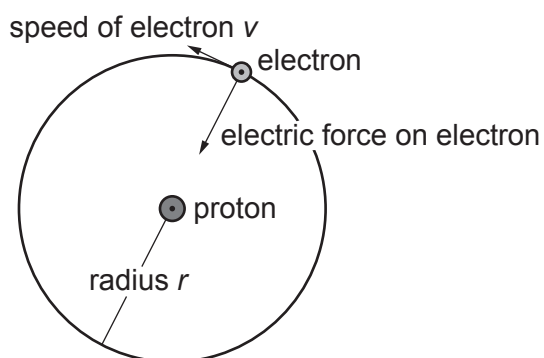


Fig. 38.2

- (i) Show that the kinetic energy of the electron in orbit is $\frac{k e^2}{2r}$

where k is the electric force constant $= 1/4\pi\epsilon_0$.

$$\text{centripetal force} = \text{electric force: } mv^2 / r = ke^2 / r^2$$

$$\text{so } mv^2 = ke^2 / r, \text{ and } KE = \frac{1}{2}mv^2 = ke^2 / 2r$$

[1]

- (ii) **Fig. 38.3** shows the variation of kinetic energy and potential energy of the electron with the radius of its orbit r .

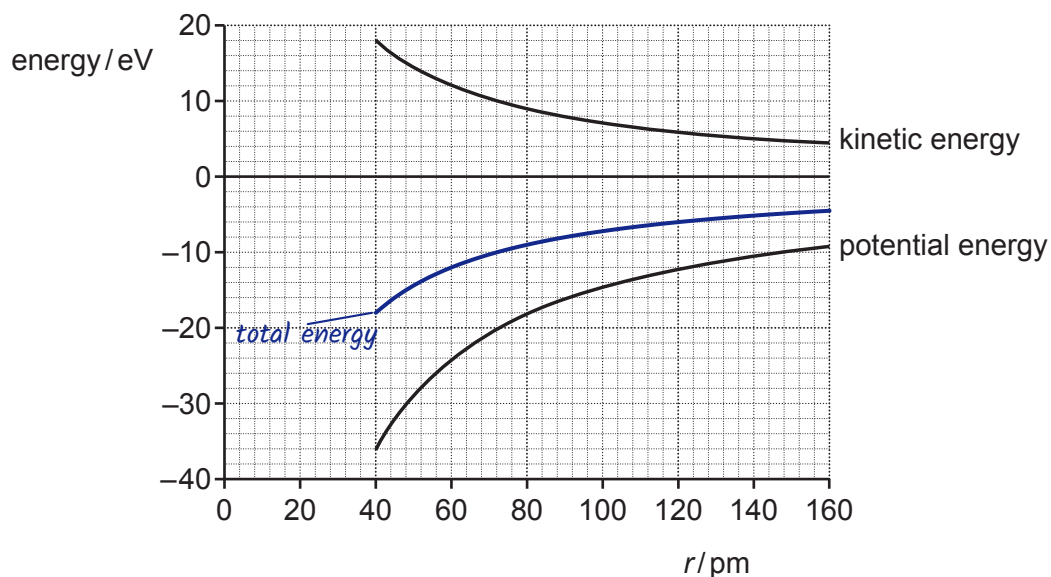


Fig. 38.3

The total energy of the electron in orbit is:

kinetic energy + potential energy ($E_{\text{total}} = E_{\text{kinetic}} + E_{\text{potential}}$).

Show that the total energy of the orbit = $\frac{-k e^2}{2r}$ and sketch the graph on **Fig. 38.3**.

$$E_{\text{potential}} = -ke^2 / r, \text{ so } E_{\text{total}} = ke^2 / 2r - ke^2 / r = -ke^2 / 2r$$

graph: mirror image of the kinetic energy curve ($-E_{\text{kinetic}}$), drawn on Fig. 38.3

[2]

- (iii) Accelerating electrons emit electromagnetic radiation.

Suggest why Bohr had to introduce the quantisation principle of allowed energy levels into his model atom.

..Otherwise the orbiting (accelerating) electron would radiate energy.....

..continuously, so its orbit would decay and it would spiral into the proton.....

[1]

- (iv) In Bohr's quantised model the radius of orbit for the ground state of the electron (lowest total energy) is given by the equation:

$$r = \frac{\epsilon_0 h^2}{\pi m e^2} \quad \text{where } m \text{ and } e \text{ are the mass and charge of the electron.}$$

Show that the potential of an electron in the ground state is about -14 V .

$$r = \epsilon_0 h^2 / \pi m e^2$$

$$= 8.85 \times 10^{-12} \times (6.63 \times 10^{-34})^2 / (\pi \times 9.11 \times 10^{-31} \times (1.6 \times 10^{-19})^2)$$

$$r = 5.3 \times 10^{-11} \text{ m} = 53 \text{ pm}$$

$$E_{\text{total}} = -ke^2 / 2r = -8.98 \times 10^9 \times (1.6 \times 10^{-19})^2 / (2 \times 5.3 \times 10^{-11})$$

$= -2.2 \times 10^{-18} \text{ J} = -13.6 \text{ eV}$, so 14 eV is needed to remove the electron to infinity
the potential (energy per unit charge) is about -14 V (14 V ionisation potential)

[2]

- 39 This question is about a rotating field motor which has a permanent magnet rotor and a stator of three coils as shown in **Fig. 39.1a** and **b**.

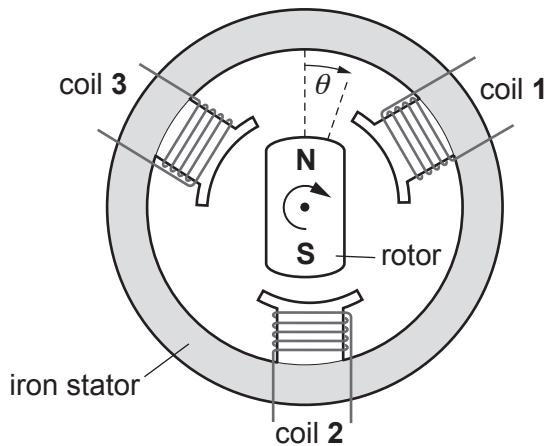


Fig. 39.1a

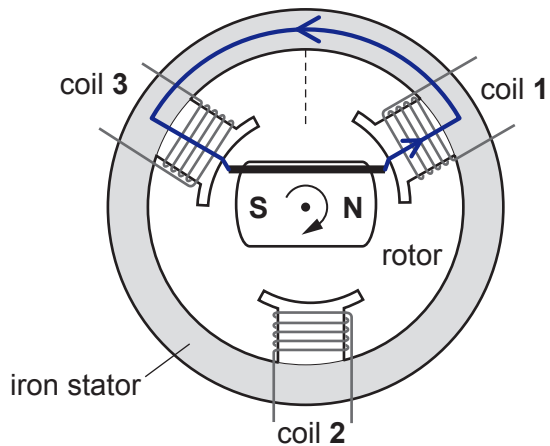


Fig. 39.1b

The control circuit switches the d.c. supply voltage to each coil between positive, off and negative. Only **two** of the **three** coils are switched on at any time.

A positive voltage makes the stator pole of that coil a **N** magnetic pole.

The angle of rotation of the magnet from the vertical start position is θ as shown in **Fig. 39.1a**.

- (a) (i) Explain why the rotor will turn clockwise when coil 1 pole is a **S** and coil 2 pole is a **N** and coil 3 is off.

*Coil 1 (S) attracts the rotor N pole, so the magnet turns to align with.....
the flux between coils 1 and 2 (about $\theta = 30^\circ$): clockwise. [1]*

- (ii) In **Fig. 39.1b** the rotor has rotated 90° aligning between coils 3 and 1. Coil 2 is off, coil 1 pole is a **S** and coil 3 pole is a **N**.

Complete the path of the **single** flux loop ——— started inside the rotor. Show the flux direction.

[2]

(b) Explain each of the following design features of the motor:

- 1 The stator is made of iron.
- 2 The stator is laminated (made of layers of iron separated by thin layers of insulator).
- 3 The air gap between the rotor magnet and the coil poles is kept as small as possible.

- 1 *Iron is easily magnetised, so it makes a much stronger (stator) field: it increases the permeance of the flux path.*
- 2 *Laminations reduce eddy currents in the iron, so there are smaller heating (energy) losses.*
- 3 *To get more flux for the same coil current, as air gaps reduce the permeance of the magnetic circuit.*

[3]

(c) For this motor, suggest how to control each of the following.

- 1 The rate of rotation of the rotor.
- 2 The force that acts to turn the rotor.

- 1 *Alter the frequency of switching the coils (faster switching gives faster rotation).*
- 2 *Alter the size of the current in the stator coils (the supply voltage), or use pulse width modulation.*

[2]

40 This question is about deriving the universal ideal gas law.

For a gas at constant absolute temperature T and pressure P the density is constant. This tells us that the number of particles N is proportional to the volume V of the gas. $N \propto V$.

Fig. 40 shows graphical evidence obtained from experiments on air, varying the pressure P , volume V , and temperature θ , when **all** other variables except the ones plotted are kept constant.

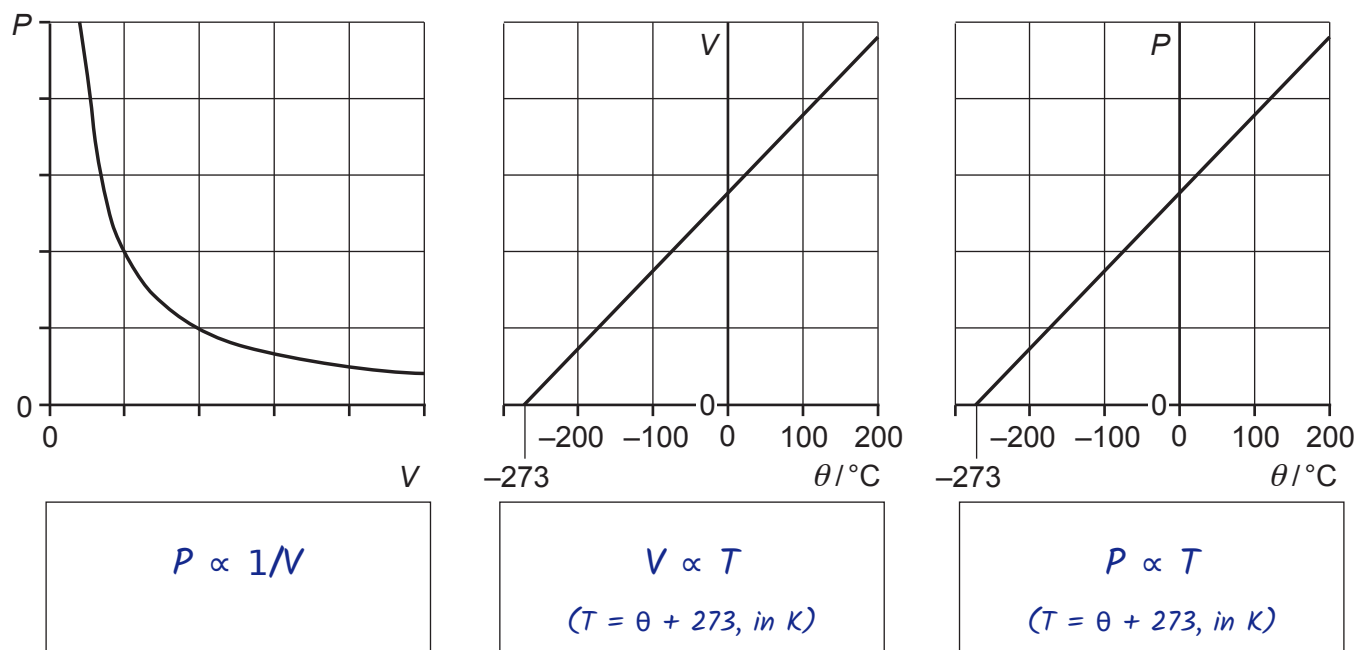


Fig. 40

(a) (i) Write in the box below each graph of **Fig. 40** the proportionality relationship shown. [2]

(ii) Combine all the proportionality relationships into one equation using the Boltzmann constant k .

$$PV / T = \text{constant, and at fixed } P \text{ and } T \text{ the constant} \propto N \text{ (as } V \propto N)$$

$$\text{so } PV / T = Nk, \text{ giving } PV = NkT$$

[1]

(iii) For **one** mole of gas at standard temperature and pressure (STP):

$$T = 273 \text{ K} \quad P = 101 \text{ kPa} \quad V = 22.4 \text{ litres.}$$

Calculate the value of the Boltzmann constant to **3** significant figures using this data.

Show your working to **4** significant figures.

$$k = PV / NT = 101 \times 10^3 \times 22.4 \times 10^{-3} / (6.02 \times 10^{23} \times 273)$$

$$k = 1.377 \times 10^{-23} \text{ J K}^{-1}$$

$$\text{Boltzmann constant} = \dots 1.38 \times 10^{-23} \dots \text{ J K}^{-1} \quad [1]$$

- (b) (i) Calculate the root mean square speed for helium gas at 300 K.

molar mass for helium = $4.0 \times 10^{-3} \text{ kg}$

$$\frac{1}{2}mc^2 = \frac{3}{2}kT, \text{ so } c_{rms} = \sqrt{3kT / m} = \sqrt{3RT / M}$$

$$c_{rms} = \sqrt{3 \times 8.31 \times 300 / 4.0 \times 10^{-3}}$$

$$c_{rms} = \sqrt{1.87 \times 10^6}$$

$$c_{rms} = 1.37 \times 10^3 \text{ m s}^{-1}$$

speed = ...1.37... $\times 10^3$ ms^{-1} [2]

- (ii) A typical speed for an air molecule at 300 K is about $4 \times 10^3 \text{ ms}^{-1}$.

Explain why the scent from an air freshener may take several minutes to reach across a room of still air.

..The scent molecules collide with air molecules very often (about 10^9
 ..times per second), so the mean free path is very small (about 10^{-7} m).....
 ..Each collision changes the direction randomly, so the molecules follow a.....
 ..random walk and diffuse (spread) only slowly..... [2]

- 41 This question is about neutron stability and the β -decay process.
This table shows the properties of the free particles that combine to form atoms.

Particle	Symbol	Mass / u	Half-life $t_{1/2}$ / s
electron	${}^0_{-1}\text{e}$	0.000549	stable ∞
proton	${}^1_1\text{p}$	1.007276	stable ∞
neutron	${}^1_0\text{n}$	1.008665	650

- (a) (i) Calculate the maximum energy available when a free neutron decays into a proton and a β -particle.

$$1 \text{ u} = 931 \text{ MeV}$$

$$\Delta m = 1.008665 - (1.007276 + 0.000549) = 0.000840 \text{ u}$$

$$E = 0.000840 \times 931 \quad \text{energy} = \dots 0.782 \dots \text{ MeV} \quad [2]$$

- (ii) The β -particles from neutron decay have a spectrum of energies up to this maximum value as shown in Fig. 41.1.

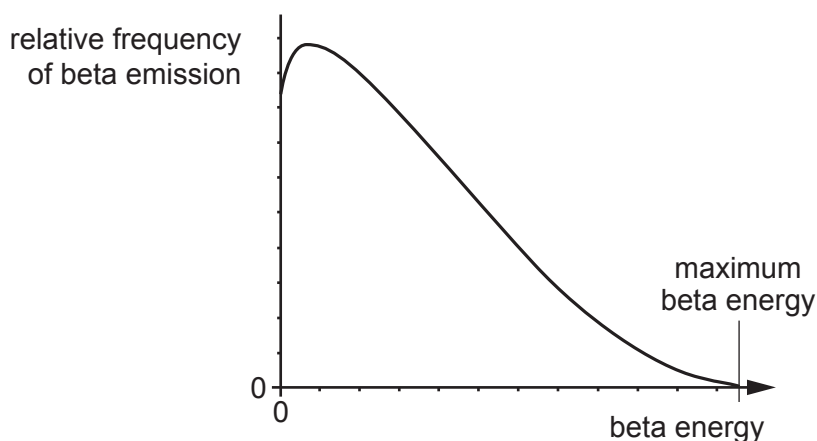


Fig. 41.1

State why the beta particles are emitted with a range of energies.

The energy is shared with an (anti)neutrino, a particle of tiny rest mass and zero charge. [1]

- (iii) Estimate the number of neutrons that would decay in one second from a sample of 10^4 free neutrons.

$$A = \lambda N = (\ln 2 / t_{1/2}) N = (0.693 / 650) \times 10^4$$

$$A = 10.7 \text{ s}^{-1}, \text{ so about 11 neutrons decay per second}$$

number per second = ...11..... [2]

- (iv) A down quark has electric charge of $-\frac{1}{3}e$ and an up quark has electric charge $+\frac{2}{3}e$.

State what is happening in terms of quarks during β -decay.

A down quark changes into an up quark ($udd \rightarrow uud$), so a neutron becomes a proton. [1]

- (b) Neutrons bound in nuclei can be either stable or unstable, see **Fig. 41.2** showing the neutron number N against proton number Z for the light nuclei. All known β -emitters and stable nuclides are plotted within the range (including the free neutron). The line $N = Z$ has been drawn as a guide.

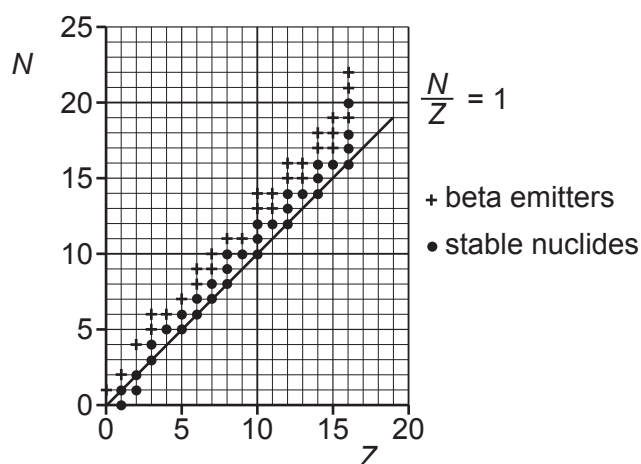


Fig. 41.2

State what this evidence broadly shows about the stability of neutrons in light nuclei.

Neutrons are stable in light nuclei with N close to Z ($N/Z \approx 1$); neutron-rich nuclei ($N/Z > 1$) are unstable and β^- decay to become closer to $N = Z$. [1]

END OF QUESTION PAPER

[illegible]

stemup.co.uk