



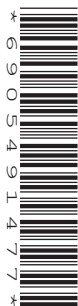
Oxford Cambridge and RSA

A Level Physics B (Advancing physics)

H557/01 Fundamentals of Physics

Monday 4 June 2018 – Afternoon

Time allowed: 2 hours 15 minutes



You must have:

- The Data, Formulae and Relationships Booklet (sent with general stationery)

You may use:

- a scientific or graphical calculator
- a ruler (cm/mm)



First name										
Last name	StemUp Model Solution									
Centre number						Candidate number				

INSTRUCTIONS

- Use black ink. You may use an HB pencil for graphs and diagrams.
- Complete the boxes above with your name, centre number and candidate number.
- Answer **all** the questions.
- Write your answer to each question in the space provided. If additional space is required, use the lined page(s) at the end of this booklet. The question number(s) must be clearly shown.
- Do **not** write in the barcodes.

INFORMATION

- The total mark for this paper is **110**.
- The marks for each question are shown in brackets [].
- Quality of extended responses will be assessed in questions marked with an asterisk (*).
- This document consists of **36** pages.

2
SECTION A

You should spend a maximum of 40 minutes on this section.

Write your answer for each question in the box provided.

Answer **all** the questions.

- 1** Which expression gives a quantity that can be expressed in joules?
- A** $F v$ where F is the force causing a body to move and v is its speed
- B** $I^2 R$ where I is the current flowing through a resistance of value R
- C** $m v$ where m is the mass of a body moving with velocity v
- D** $V I t$ where V is the potential difference across a conductor and I is the current in it for time t .

Your answer

D

[1]

- 2** Which of these ages is estimated correctly?
- A** The Earth is about 4 billion years old.
- B** The Sun is about 14 billion years old.
- C** The Milky Way Galaxy is about 20 billion years old.
- D** The Universe is about 20 billion years old.

Your answer

A

[1]

- 3** How many bits are required to code for 1300 different levels?
- A** 3
- B** 4
- C** 10
- D** 11

Your answer

D

[1]

- 4 An image sent from Pluto to Earth is 1024×1024 pixels. Each pixel is coded by 12 bits. The data is transferred at a rate of 200 bytes per second.

How long does it take to transmit the data?

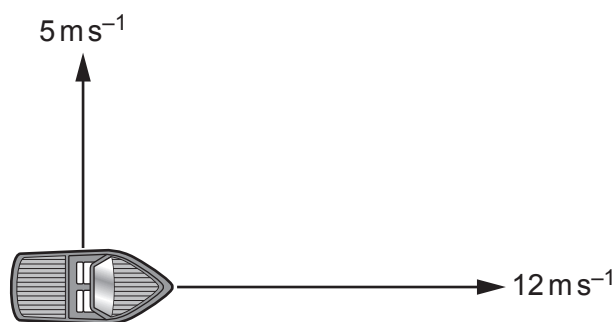
- A 11 minutes
- B 87 minutes
- C 131 minutes
- D 1049 minutes

Your answer

C

[1]

- 5 A boat travels eastwards with a velocity of 12 ms^{-1} . A current from the south pushes the boat northwards at a velocity of 5 ms^{-1} .



What is the magnitude of the resultant velocity of the boat?

- A 7 ms^{-1}
- B 13 ms^{-1}
- C 17 ms^{-1}
- D 169 ms^{-1}

Your answer

B

[1]

- 6 A weight of 20 N is suspended from a steel wire.

What is the extension of the wire?

Data: original length of wire = 2.5 m
 cross-sectional area of wire = $7.0 \times 10^{-8} \text{ m}^2$
 Young Modulus of the wire material = $2.1 \times 10^{11} \text{ Pa}$

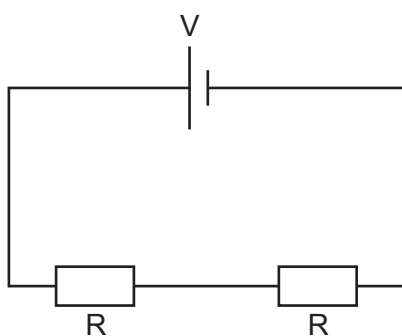
- A 0.0030 m
 B 0.0034 m
 C 0.030 m
 D 0.034 m

Your answer

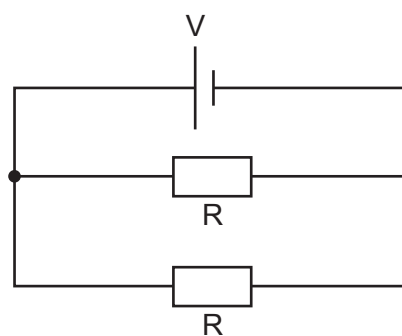
B

[1]

- 7 These two circuits use identical components.
 The cells have zero internal resistance.



circuit 1



circuit 2

What is the ratio $\frac{\text{power dissipated in circuit 1}}{\text{power dissipated in circuit 2}}$?

- A $\frac{1}{4}$
 B $\frac{1}{2}$
 C 2
 D 4

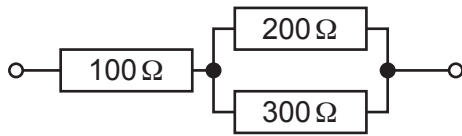
Your answer

A

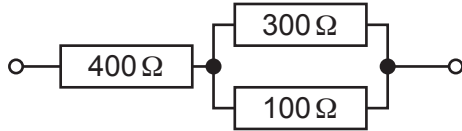
[1]

8 Which combination of resistors gives the **lowest** total resistance?

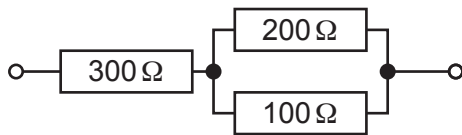
A



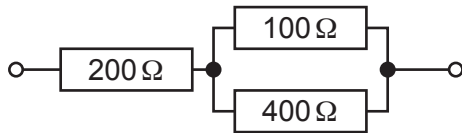
B



C



D

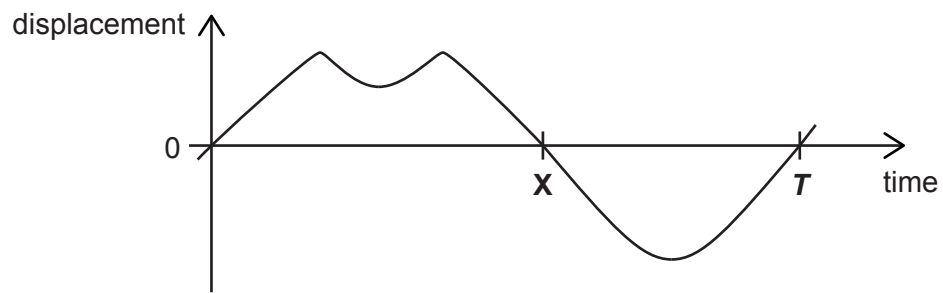


Your answer

A

[1]

- 9 The graph shows the displacement of a body which is oscillating periodically with time period T .



Which statement is correct?

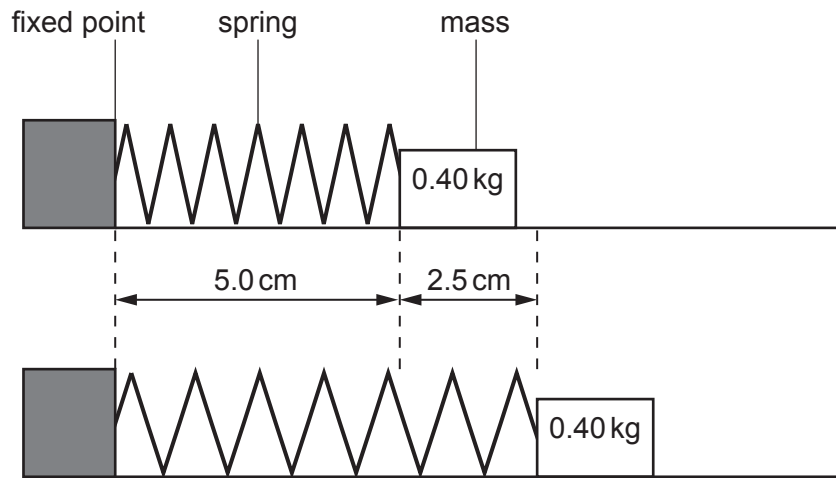
- A The acceleration is zero at time X .
- B The body is performing simple harmonic motion.
- C In each cycle the velocity is zero three times.
- D The body changes direction at X .

Your answer

A

[1]

- 10** The spring in this diagram has a spring constant of 20 N m^{-1} . The mass is pulled away from the fixed point. The spring stretches by 2.5 cm . The mass is then released.



What is the maximum speed reached by the mass?

- A** 0.18 ms^{-1}
B 0.53 ms^{-1}
C 1.25 ms^{-1}
D 3.75 ms^{-1}

Your answer

A

[1]

- 11** An electron is travelling at a speed of $3.1 \times 10^5 \text{ ms}^{-1}$.

What is its kinetic energy in electronvolts?

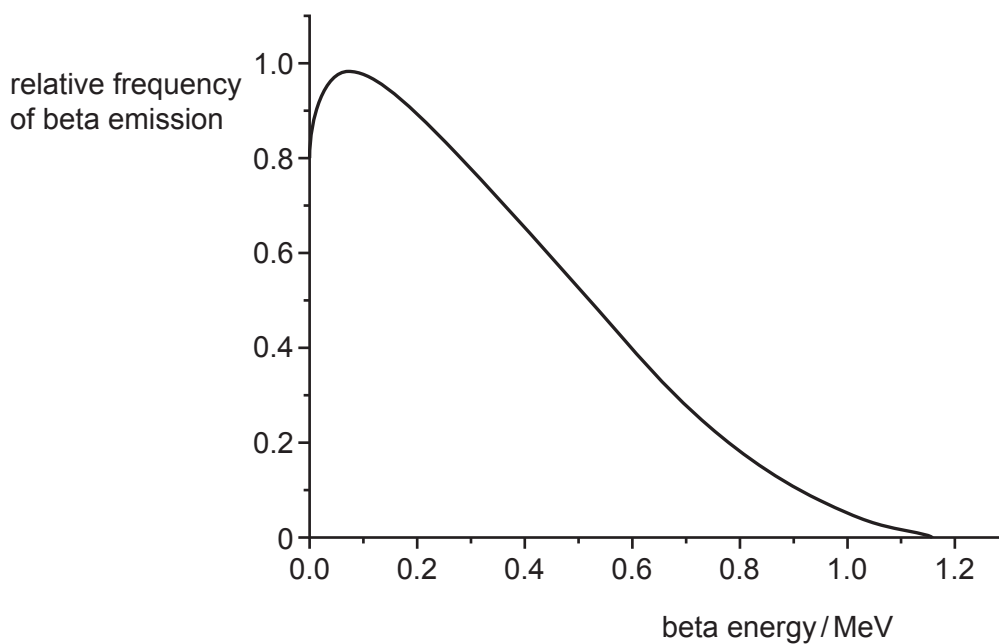
- A** $4.4 \times 10^{-20} \text{ eV}$
B $8.8 \times 10^{-7} \text{ eV}$
C 0.27 eV
D 500 eV

Your answer

C

[1]

12 The diagram shows the beta energy spectrum for emissions from a radioactive isotope.



Which statement is correct?

- A The maximum energy of beta emissions is about 0.1 MeV.
- B More than half the beta particles are emitted with less than half the maximum energy.
- C The “missing energy” in beta emissions is taken by the recoiling nucleus.
- D The most frequent energy of beta emission is about 1.16 MeV.

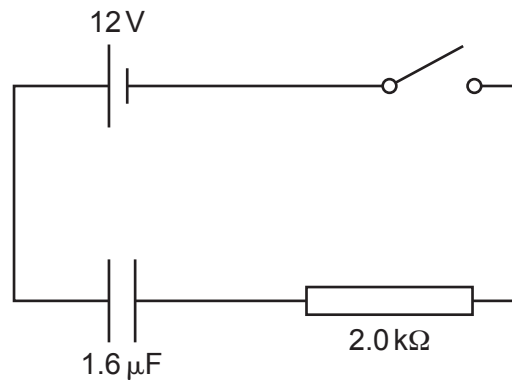
Your answer

B

[1]

The following information is for use in questions 13 and 14.

An uncharged capacitor and a resistor are connected in this circuit.



	current/mA	p.d. across the capacitor/V	p.d. across the resistor/V
A	0	12	0
B	2	8	4
C	3	6	6
D	6	0	12

- 13 Which set of values **A** to **D** above, most closely represents the situation immediately after the switch is closed?

Your answer

D

[1]

- 14 Which set of values **A** to **D** above, most closely represents the situation 3 seconds after the switch is closed?

Your answer

A

[1]

- 15** A liquid flows through a tube containing an electrical heater with a constant voltage.
At a steady state of flow, the liquid leaves the tube at temperature $\Delta\theta$ higher than the liquid entering.

Which change will increase $\Delta\theta$ with no other changes?

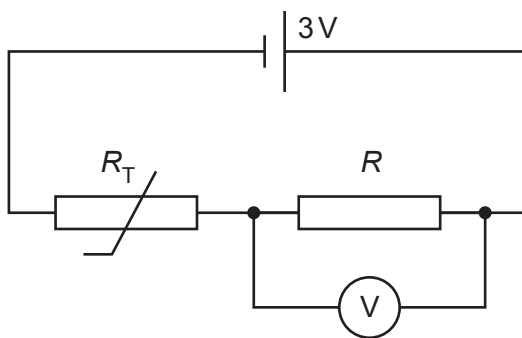
- A** Increasing the flow rate of the liquid.
- B** Changing the liquid to one with a higher specific heat capacity.
- C** Using a heating element of lower resistance.
- D** Decreasing the supply voltage.

Your answer

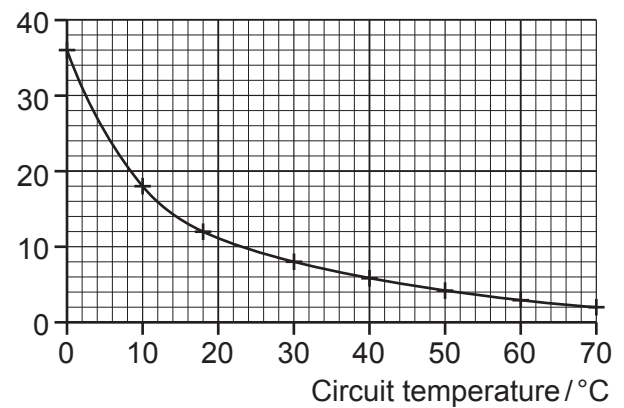
C

[1]

- 16** A thermistor is used in a potential divider circuit.



thermistor resistance $R_T / \text{k}\Omega$



When the circuit temperature is 10°C the reading on the voltmeter is 1.0V .
What is the resistance of the resistor R ?

- A** $6\text{ k}\Omega$
- B** $9\text{ k}\Omega$
- C** $18\text{ k}\Omega$
- D** $36\text{ k}\Omega$

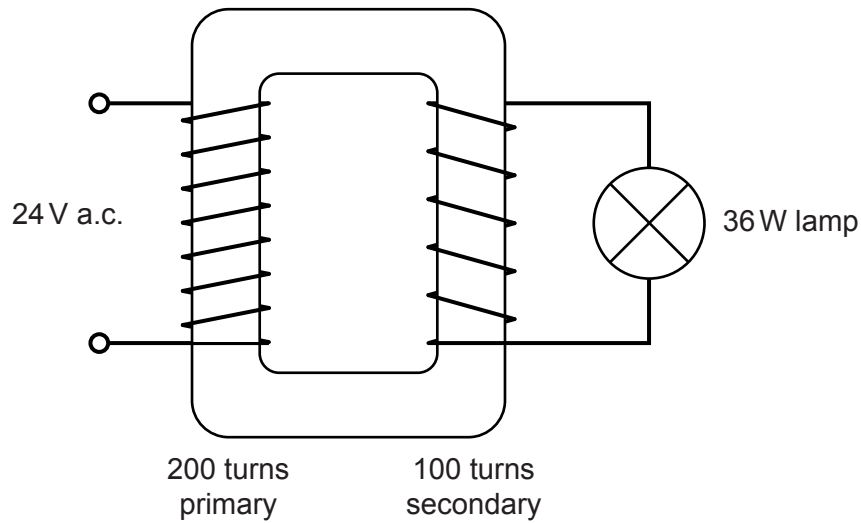
Your answer

B

[1]

The following information is for use in questions 17 and 18.

A transformer runs a 36.0 W lamp from a 24.0 V a.c. supply.



17 What is the current in the secondary coil?

- A 1.5 A
- B 3.0 A
- C 4.0 A
- D 6.0 A

Your answer

B

[1]

18 What is the best estimate for the rate of change of flux in the transformer core?

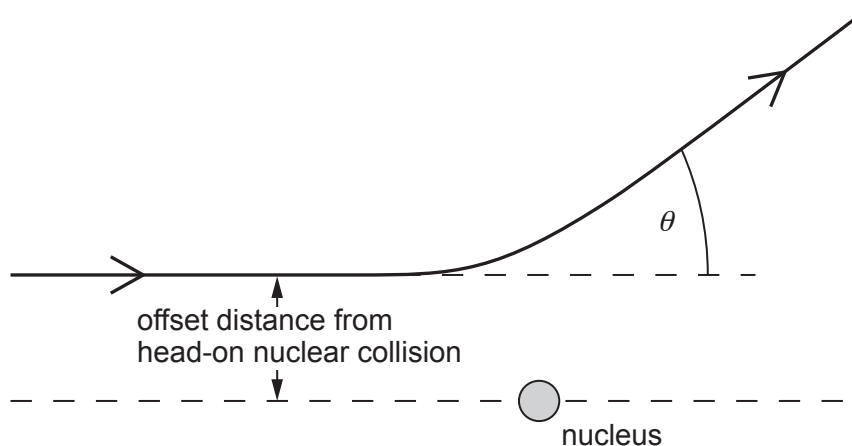
- A 0.12 Wb s^{-1}
- B $0.12 \text{ T m}^{-2} \text{ s}^{-1}$
- C 12 Wb s^{-1}
- D $12 \text{ T m}^{-2} \text{ s}^{-1}$

Your answer

A

[1]

- 19 An α particle approaches an atomic nucleus and is scattered through angle θ . The path of the particle is offset as shown.



Which change on its own would cause the scattering angle θ to increase?

- A Use an α particle with higher kinetic energy.
- B Have a smaller offset distance for the initial trajectory.
- C Use a target nucleus with a smaller charge.
- D Use a target nucleus with a smaller mass.

Your answer

B

[1]

The following information is for use in questions **20** and **21**.

A particle of charge q and mass m travels in a vacuum in a region of constant magnetic flux density B .

It moves at a constant speed v in a circle of radius r .

20 Which expression gives the time for the particle to complete one circle of its motion?

A $\frac{2\pi m}{Bqr}$

B $\frac{2\pi mr}{Bq}$

C $\frac{2\pi m}{Bq}$

D $\frac{Bq}{2\pi m}$

Your answer

C

[1]

21 A proton and an α particle, with the same velocity, enter the region of constant magnetic flux density.

What is the ratio of the radii of their paths, $\frac{r_{\alpha}}{r_{\text{proton}}}$?

A $\frac{1}{4}$

B $\frac{1}{2}$

C 2

D 4

Your answer

C

[1]

22 This table shows the half-lives of three radioactive isotopes.

Isotope	$^{60}\text{cobalt}$	$^{192}\text{iridium}$	$^{210}\text{thallium}$
Half-life	5.3 years	74 days	1.8 minutes

Which statement can be deduced from the information given?

- A The decay constant of thallium is smaller than that of iridium.
- B Because of the difference in half-lives, the energy of the particles emitted from cobalt must be less than the energy of the particles emitted by thallium.
- C The most active source will be thallium.
- D If the number of atoms in the cobalt and iridium sources is initially equal, then the iridium source will have the greater initial activity.

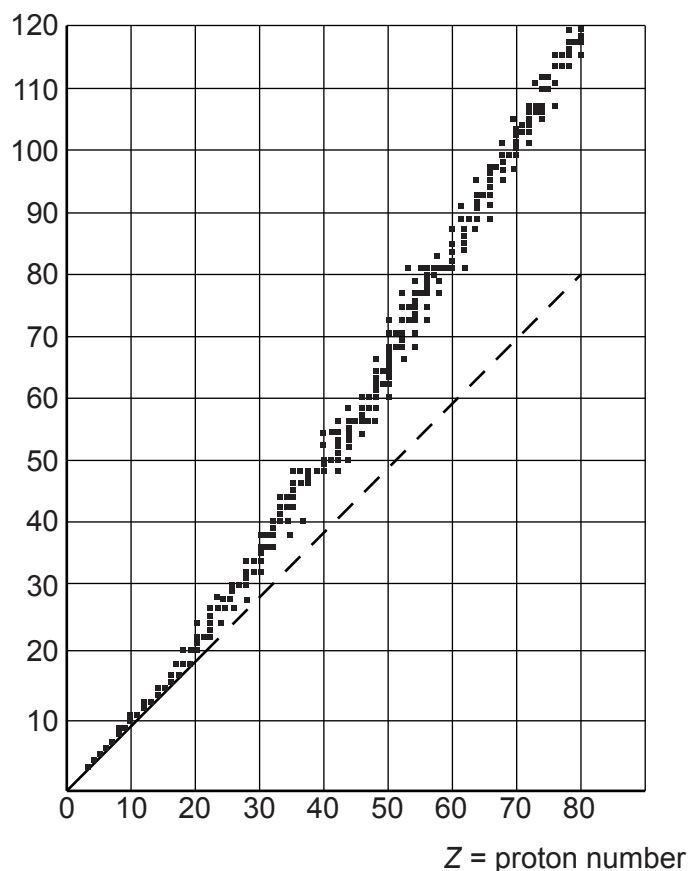
Your answer

D

[1]

23 The graph shows neutron number N plotted against proton number Z for stable nuclei.

N = neutron number



Which statement about stable nuclei is correct?

- A For elements up to about $Z = 50$ $N \approx Z$.
- B Elements with $Z \approx 80$ have more protons than neutrons.
- C Greater $\frac{N}{Z}$ ratio is needed to hold larger nuclei together, because only neutrons take part in the strong nuclear force of attraction to balance electrostatic repulsion.
- D Greater $\frac{N}{Z}$ ratio is needed to hold larger nuclei together because only nearest neighbour nucleons take part in the strong nuclear force of attraction to balance electrostatic repulsion.

Your answer

D

[1]

- 24 A ball is kicked from horizontal ground at a velocity of 15 m s^{-1} at an angle of 20° to the horizontal.

How long will the ball remain in the air before hitting the ground?
Ignore any effects of air resistance.

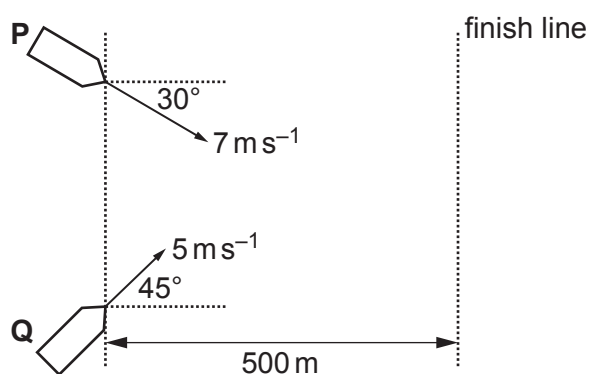
- A 0.5 s
- B 1.0 s
- C 1.4 s
- D 2.9 s

Your answer

B

[1]

- 25 The diagram shows two boats **P** and **Q** sailing at constant velocity towards the finish line.



Which statement is correct?

- A Boat **P** wins by 1.4 s.
- B Boat **Q** wins by 29 s.
- C Boat **P** wins by 59 s.
- D Boat **Q** wins by 198 s.

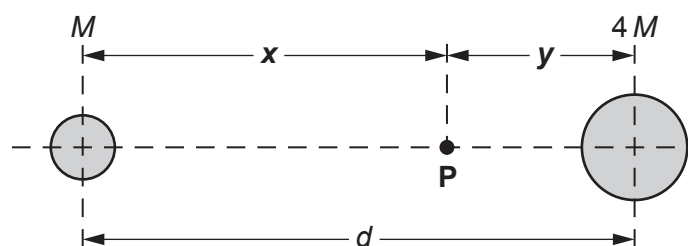
Your answer

C

[1]

The following information is for use in questions 26, 27 and 28.

Two stars of mass M and $4M$ are a distance d apart.
They orbit around their common centre of mass.



The point P , on the line between the centres of the stars, divides the distance d in the ratio $x : y$ as shown.

26 If P is the gravitational neutral point between the stars, which ratio is correct for $x : y$?

- A 1 : 4 B 1 : 2 C 2 : 1 D 4 : 1

Your answer

B

[1]

27 If P is the centre of mass of the two stars, which ratio is correct for $x : y$?

- A 1 : 4 B 1 : 2 C 2 : 1 D 4 : 1

Your answer

D

[1]

28 If P is the point where the gravitational potentials of the two stars are equal, which ratio is correct for $x : y$?

- A 1 : 4 B 1 : 2 C 2 : 1 D 4 : 1

Your answer

A

[1]

- 29 The electric potential at a distance r from a positive point charge Q is 450 V.
The potential increases to 500 V when the distance from the point charge decreases by 1.5 m.

What is the value of r ?

- A 1.5 m
- B 7.9 m
- C 15 m
- D 29 m

Your answer

C

[1]

- 30 The relativistic factor $\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$

Which statement about this factor is correct?

- A At the speed of sound γ is close to zero.
- B $\gamma \rightarrow 1$ as $v \rightarrow c$.
- C γ predicts the time dilation factor so that moving clocks run slower as $v \rightarrow c$.
- D γ^2 is the factor by which the total energy of a moving particle is greater than its rest energy.

Your answer

C

[1]

SECTION B

Answer **all** the questions.

- 31** The lens in a digital clock projects the time onto a wall 1.5 m away as shown in **Fig. 31**.

The digital display is 0.030 m from the lens.

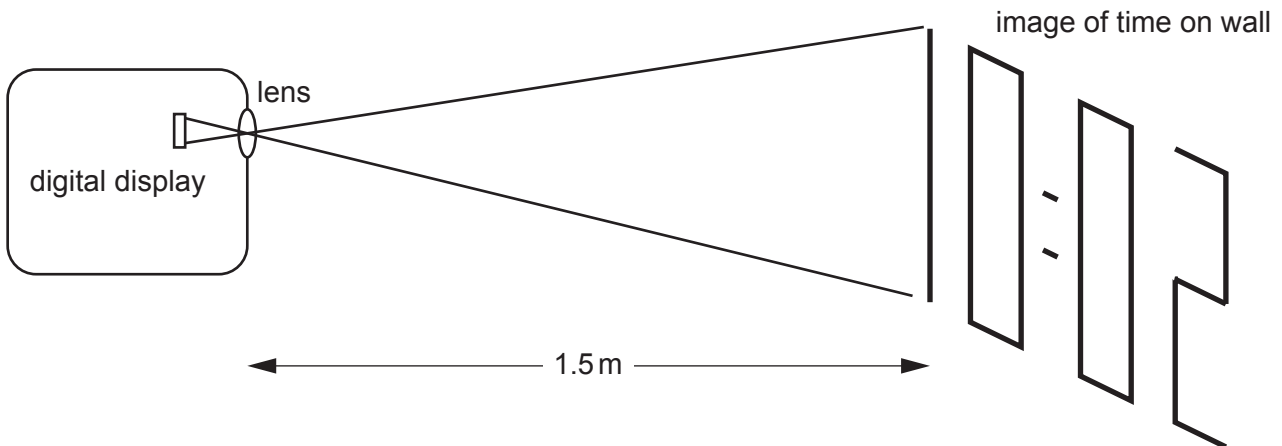


Fig. 31

- (a)** Calculate the power of the lens.

$$\begin{aligned}
 1/v - 1/u &= 1/f = \text{power, with } u = -0.030 \text{ m and } v = +1.5 \text{ m} \\
 \text{power} &= 1/1.5 - 1/(-0.030) \\
 \text{power} &= 0.67 + 33.3 \\
 \text{power} &= 34 \text{ D}
 \end{aligned}$$

power of the lens = ...34..... D [3]

- (b)** State the magnification of the lens in this example.

$$\text{magnification} = v/u = 1.5 \div 0.030$$

magnification = ...50..... [1]

- 32 A video file is downloaded at a rate of 24 Mbits s^{-1} .
The video file is 1.2 Gbytes in size.

(a) Show that the time taken for the file to download is greater than 6 minutes.

$$\begin{aligned} \text{file size} &= 1.2 \times 10^9 \text{ bytes} \times 8 = 9.6 \times 10^9 \text{ bits} \\ \text{time} &= \text{file size} \div \text{rate} = 9.6 \times 10^9 \div 24 \times 10^6 \\ \text{time} &= 400 \text{ s}; \quad 6 \text{ minutes} = 360 \text{ s} \\ 400 \text{ s} &> 360 \text{ s, so the time is greater than 6 minutes (6 min 40 s)} \end{aligned}$$

[2]

- (b) The video file contains a soundtrack sampled at 16.0 kHz.
State and explain the highest frequency of sound that can be recorded on the soundtrack.

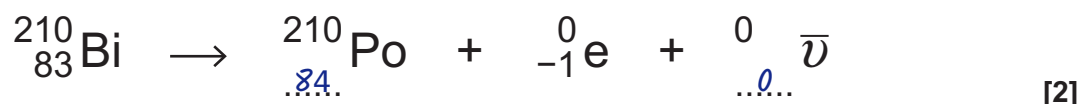
highest frequency 8.0 kHz

There must be at least two samples in every cycle of the sound wave to pick up its variation, so $f = 16.0 \div 2 = 8.0 \text{ kHz}$.

[2]

- 33 The radioactive isotope $^{210}_{83}\text{Bi}$ decays by this beta decay.

(a) Complete the decay equation.



[2]

(b) State why an antineutrino is emitted during beta decay.

To conserve lepton number: the electron has lepton number +1, so an antineutrino (-1) is needed to keep the total 0.

[1]

- 34** A solar panel is charging a rechargeable battery, with a resistor R in series.

The values of the internal resistances r , the external resistance R and the e.m.f.s $\mathcal{E}$ at the start of the charging process are shown in **Fig. 34**.

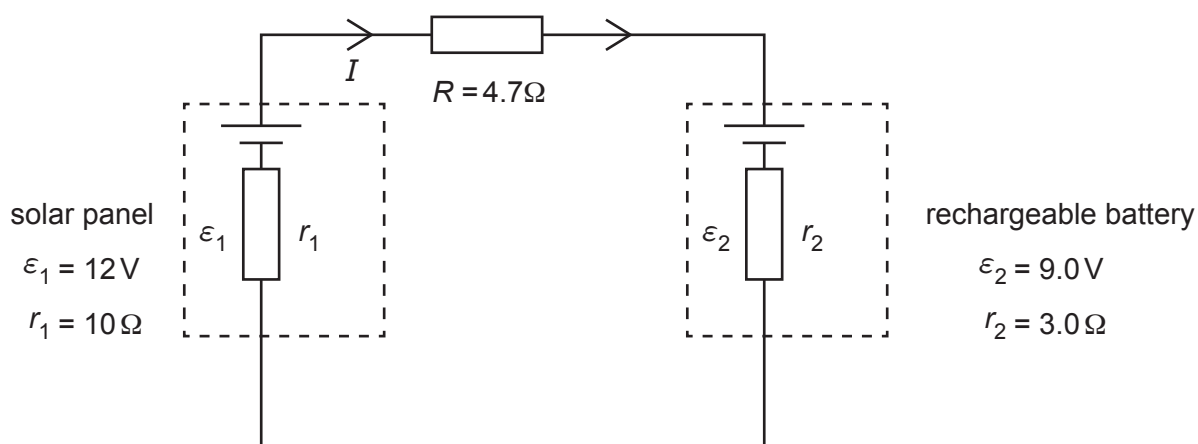


Fig. 34

- (a) Show that the initial current charging the rechargeable battery I is less than 0.2 A.

the e.m.f.s oppose; net e.m.f. = $12 - 9.0 = 3.0\text{ V}$ drives the current

total resistance = $10 + 4.7 + 3.0 = 17.7\ \Omega$

$I = \Sigma \mathcal{E} / \Sigma R = 3.0 \div 17.7$

$I = 0.17\text{ A}$ (0.169 A), which is less than 0.2 A

[2]

- (b) When fully charged, the rechargeable battery has enough charge to deliver an average current of 500 mA for an hour before it is fully discharged.

Estimate the time needed to recharge the battery at the mean charging current of 0.12 A.

$Q = It = 0.50\text{ A} \times 3600\text{ s} = 1800\text{ C}$

$t = Q/I = 0.50 \times 3600 \div 0.12 = 1.5 \times 10^4\text{ s}$

$t = 1.5 \times 10^4 \div 3600 = 4.2\text{ hours}$

time = ...4.2..... hours [2]

- 35 This question is about a model of an atom with one electron. The electron is trapped in a box as shown in Fig. 35. Possible electron kinetic energy levels are plotted as shown.

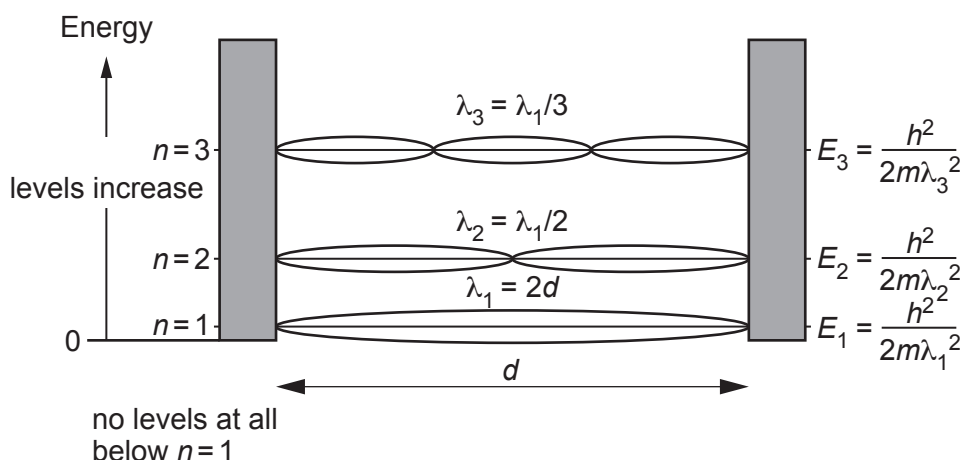


Fig. 35

- (a) Explain how this model gives rise to discrete quantised energy levels for the atom.

The electron is trapped as a standing wave between the walls, so only whole numbers of half wavelength loops fit: $\lambda = 2d/n$, so λ is quantised. The wavelength fixes the momentum $p = h/\lambda$ and so the kinetic energy $E = h^2/2m\lambda^2$; only discrete energy levels are allowed. [2]

- (b) How many different frequencies of photon can be emitted from an atom with 3 energy levels?

Three ($3 \rightarrow 2$, $2 \rightarrow 1$ and $3 \rightarrow 1$) [1]

- (c) The distance d between the walls of the box is about atomic size ≈ 0.10 nm.

Calculate the frequency of the most energetic photon that this model atom could emit.

most energetic photon: $n = 3$ to $n = 1$, so $\Delta E = E_3 - E_1$

$\lambda_1 = 2d = 2.0 \times 10^{-10}$ m; $\lambda_3 = 2d/3 = 6.7 \times 10^{-11}$ m

$E_1 = h^2/2m\lambda_1^2 = 0.60 \times 10^{-17}$ J; $E_3 = 5.4 \times 10^{-17}$ J

$\Delta E = (5.4 - 0.60) \times 10^{-17} = 4.8 \times 10^{-17}$ J = hf

$f = 4.8 \times 10^{-17} \div 6.63 \times 10^{-34} = 7.3 \times 10^{16}$ Hz

frequency = *7.3 x 10¹⁶* Hz [3]

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Turn over for Section C

SECTION C

Answer **all** the questions.

36 This question considers some of the evidence for a Hot Big Bang start to our expanding universe.

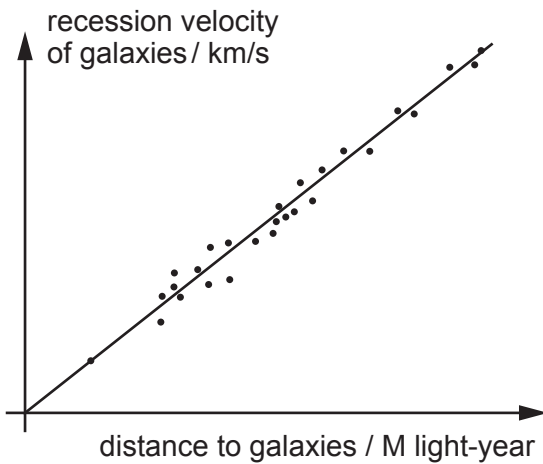


Fig. 36.1

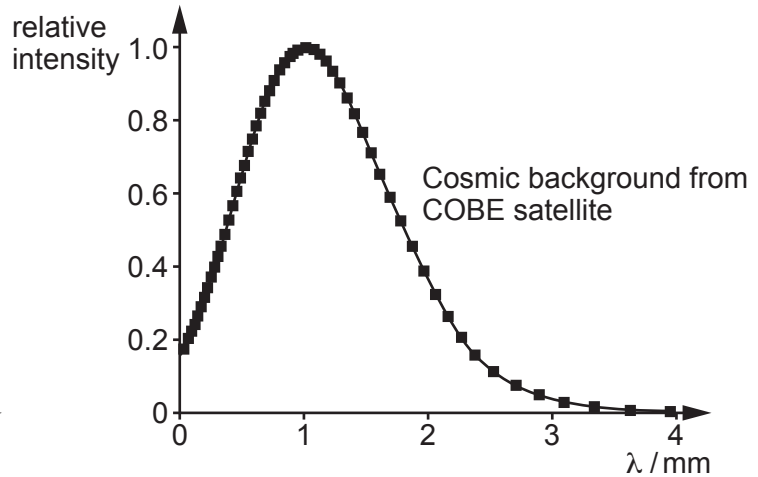


Fig. 36.2

(a) Explain how the graph(s) show evidence that the universe started from:

(i) a big bang expansion

Fig. 36.1 shows recession velocity is proportional to distance (straight line through the origin, $v = H_0 d$).
 Played back in time the galaxies were closer together earlier; at the big bang all the matter was at the same place, rushing outwards. [2]

(ii) a hot state.

Fig. 36.2 shows black body (thermal) radiation in the microwave region, with its peak at about 1 mm.
 Earlier, at the big bang, the radiation was hotter with a much shorter λ (γ -rays); its λ has been stretched by the expansion of space. [2]

- (b) The intensity spectrum of thermal radiation depends on temperature T . Photons at the **peak** of intensity have energy $\varepsilon \approx 5kT$.

Use this approximation and data from **Fig. 36.2** to estimate the temperature of the cosmic microwave background radiation (CMBR).

$$\text{peak of Fig. 36.2 at } \lambda = 1.0 \text{ mm} = 1.0 \times 10^{-3} \text{ m}$$

$$f = c/\lambda = 3.00 \times 10^8 \div 1.0 \times 10^{-3} = 3.0 \times 10^{11} \text{ Hz}$$

$$\varepsilon = hf = 6.63 \times 10^{-34} \times 3.0 \times 10^{11} = 1.99 \times 10^{-22} \text{ J}$$

$$\varepsilon \approx 5kT, \text{ so } T \approx hf / 5k$$

$$T \approx 1.99 \times 10^{-22} \div (5 \times 1.38 \times 10^{-23})$$

$$T \approx 2.9 \text{ K}$$

temperature = ...2.9..... K [4]

37 This question is about propulsion systems for spacecraft.

(a) A solar sail uses the momentum of photons in solar radiation for propulsion.

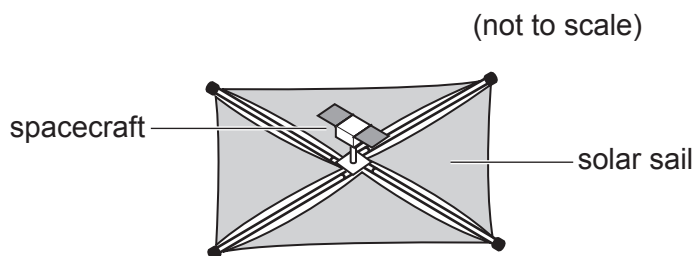


Fig. 37.1

Relativity shows that a photon of energy E has momentum $p = \frac{E}{c}$.

(i) Show that $\frac{E}{c}$ has the units of momentum.

*E/c has units $J \div m\ s^{-1} = kg\ m^2\ s^{-2} \div m\ s^{-1} = kg\ m\ s^{-1}$
 $p = mv$ has units $kg\ m\ s^{-1}$, the same, so E/c has units of momentum*

[1]

(ii) The total photon power of the radiation received from the Sun on a $1.0\ m^2$ area of solar sail is P .

Show that the thrust force T from photon reflection is given by $T = \frac{2P}{c}$.

Assume that the Sun's rays are normal to the sail and all the radiation is reflected.

*each photon is reflected, momentum reversed: $\Delta p = E/c - (-E/c) = 2E/c$
 n photons per second hit the $1.0\ m^2$, so $P = nE$ (energy per second)
 $T = \text{rate of change of momentum} = \Delta p / \Delta t = n \times 2E/c$
 $T = 2nE/c = 2P/c$*

[3]

(iii) The total photon power density is $1400\ W\ m^{-2}$. The 1.0 tonne spacecraft has a $10^6\ m^2$ solar sail.

Calculate the acceleration of the spacecraft.

*$a = T/m = 2PA/mc$
 $a = 2 \times 1400 \times 10^6 \div (1.0 \times 10^3 \times 3.00 \times 10^8)$
 $a = 9.3 \times 10^{-3}\ m\ s^{-2}$*

acceleration = ... 9.3×10^{-3} ms^{-2} [2]

- (b) An ion drive uses the momentum of ions for propulsion. It ionises a gas and uses an accelerating field to accelerate the positive ions to a high velocity.

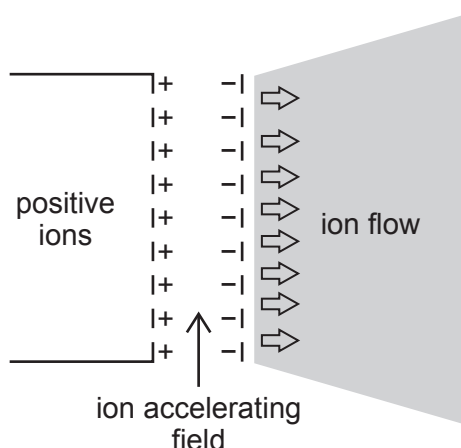


Fig. 37.2

- (i) A positive ion of charge Q and mass m is accelerated through a p.d. V . Show that the momentum per unit mass $\frac{p}{m}$ it gains is given by the expression

$$\frac{p}{m} = \sqrt{2V\left(\frac{Q}{m}\right)}.$$

k.e. gained = electrical p.e. lost: $\frac{1}{2}mv^2 = QV$, so $v = \sqrt{2QV/m}$

momentum per unit mass $p/m = mv/m = v$

so $p/m = \sqrt{2V(Q/m)}$

[2]

- (ii) Discuss an advantage of using ions of hydrogen ${}^1\text{H}^+$ as propellant instead of xenon ${}^{130}\text{Xe}^+$.

${}^1\text{H}^+$ has a much larger Q/m (about 130 times that of Xe^+), so for the same V it gains a much larger p/m : more momentum (thrust) per kg of propellant.

[2]

- (iii) An ion drive with accelerating p.d. $V = 2000\text{ V}$ must produce a thrust of 0.24 N .

Show that the mass flow rate $\frac{\Delta m}{\Delta t}$ is less than $4 \times 10^{-7}\text{ kg s}^{-1}$.

$\frac{Q}{m}$ for ${}^1\text{H}^+$ ions = $9.6 \times 10^7\text{ C kg}^{-1}$.

$T = \Delta p/\Delta t = (\Delta p/\Delta m) \times (\Delta m/\Delta t)$, so $\Delta m/\Delta t = T \div (p/m)$

$p/m = \sqrt{2 \times 2000 \times 9.6 \times 10^7} = 6.2 \times 10^5\text{ m s}^{-1}$

$\Delta m/\Delta t = 0.24 \div 6.2 \times 10^5 = 3.9 \times 10^{-7}\text{ kg s}^{-1}$, less than 4×10^{-7}

[2]

38 A student performs Young's double slit experiment as shown in Fig. 38.1.

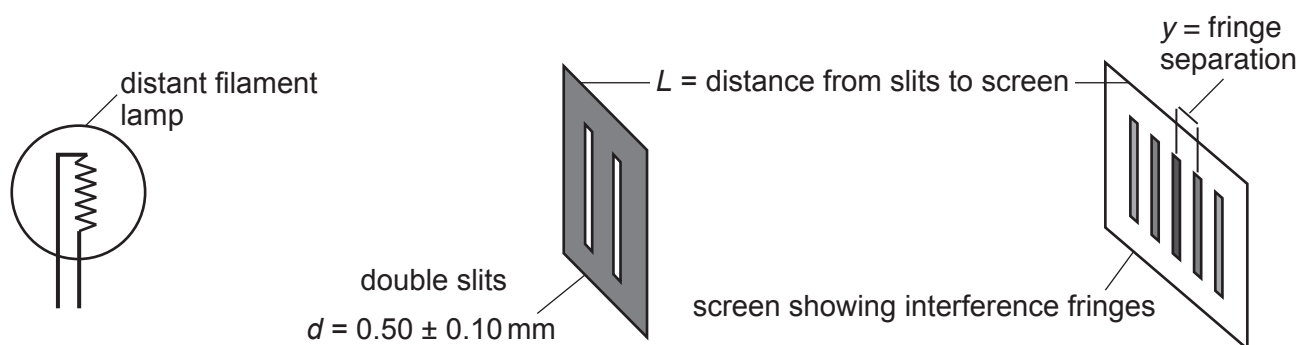


Fig. 38.1

The student investigates how the fringe spacing y varies with the distance L from slits to screen. The student measures the slit separation $d = 0.5 \pm 0.1 \text{ mm}$.

Fig. 38.2 shows the data obtained with uncertainties.

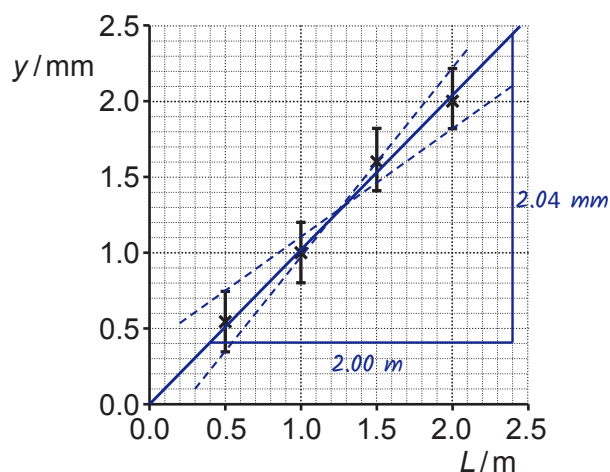


Fig. 38.2

(a) Suggest a reason why only uncertainties in the fringe spacing are shown on the graph.

..The % uncertainty in L (about 1 mm in 1000 mm) is negligible compared.....
 ..with the % uncertainty in y (0.2 mm in 2 mm)..... [1]

- (b) Draw a line of best fit on the graph and measure its gradient with an uncertainty estimate.

best fit line through the origin drawn; from the large triangle:

$$\text{gradient} = \Delta y / \Delta L = 2.04 \times 10^{-3} \text{ m} \div 2.00 \text{ m} = 1.02 \times 10^{-3}$$

steepest line through bars: 1.25×10^{-3} ; shallowest: 0.71×10^{-3}

$$\text{uncertainty} = (1.25 - 0.71) \times 10^{-3} \div 2 \approx 0.3 \times 10^{-3}$$

$$\text{gradient} = \dots 1.0 \times 10^{-3} \dots \pm \dots 0.3 \times 10^{-3} \dots \text{ [3]}$$

- (c) Use the gradient to estimate an average wavelength for the light together with an uncertainty estimate. Make your method clear.

$$y = \lambda L / d, \text{ so gradient} = \lambda / d \text{ and } \lambda = d \times \text{gradient}$$

$$\lambda = 0.50 \times 10^{-3} \times 1.02 \times 10^{-3} = 5.1 \times 10^{-7} \text{ m}$$

$$\% \text{ uncertainty: gradient } 0.3/1.02 = 29\%; \quad d \ 0.10/0.50 = 20\%$$

$$\text{total} \approx 29\% + 20\% = 49\%; \quad \Delta \lambda = 0.49 \times 5.1 \times 10^{-7} = 2.5 \times 10^{-7} \text{ m}$$

$$\text{wavelength} = \dots 5.1 \times 10^{-7} \dots \pm \dots 2.5 \times 10^{-7} \dots \text{ m [3]}$$

- (d) State **one** way in which you could refine or develop this practical design or procedure to reduce uncertainty.

Use a travelling microscope to measure d and y more precisely, measuring across 10 fringes and dividing by 10 [1]

39 (a)* Boyle's Law states that at constant temperature, pressure is proportional to $\frac{1}{\text{volume}}$.

Explain how the random motion of particles gives rise to Boyle's law.

Gas particles move randomly with a spread of speeds (Maxwell-Boltzmann distribution). They travel in straight lines between collisions, with a spread of free path lengths, and collide with each other and the walls at all possible angles in 3-D, so each collision changes a particle's velocity randomly in size and direction (a random walk). When a particle hits a wall its momentum is reversed (change $2mv$), so it exerts a force on the wall. Huge numbers of tiny chaotic collisions per second add up to a steady force per unit area: the pressure. Constant temperature means constant average kinetic energy, so the average speed and the average momentum change per collision stay the same. Pressure $\propto$ (collisions per second per unit area of wall) $\times$ (Δp per collision), and the collision rate is proportional to the number density N/V . If V is halved, N/V doubles, so twice as many particles hit each unit area every second with the same Δp each; p doubles. So $p \propto 1/V$, i.e. $pV = \text{constant}$.

[6]

(b) Here are some data about trace gases in the atmosphere:

H₂ molar mass 2 grams
Xe molar mass 132 grams

- (i) Calculate the ratio: $\frac{\text{speed of hydrogen molecule with average kinetic energy}}{\text{speed of xenon atom with average kinetic energy}}$.

Make your reasoning clear.

at the same T both have the same average kinetic energy:

$$\frac{1}{2}m_H c_H^2 = \frac{1}{2}m_{Xe} c_{Xe}^2 \quad (c = \text{speed with average k.e.})$$

$$c_H/c_{Xe} = \sqrt{(m_{Xe}/m_H)} = \sqrt{(132/2)} = \sqrt{66}$$

$$\text{ratio} = 8.1$$

$$\text{ratio} = \dots\dots\dots 8.1 \dots\dots\dots [3]$$

- (ii) The escape velocity for planet Earth is 11.2 km s⁻¹.

Use the Boltzmann factor to estimate the number of H₂ molecules per mole with sufficient energy to escape the atmosphere and the Earth's gravitational field at a temperature of 288 K.

$$\text{mass of } H_2 \text{ molecule } m = 2 \times 10^{-3} \div 6.02 \times 10^{23} = 3.32 \times 10^{-27} \text{ kg}$$

$$E = \frac{1}{2}mv^2 = \frac{1}{2} \times 3.32 \times 10^{-27} \times (11.2 \times 10^3)^2 = 2.08 \times 10^{-19} \text{ J}$$

$$E/kT = 2.08 \times 10^{-19} \div (1.38 \times 10^{-23} \times 288) = 52.4$$

$$\text{Boltzmann factor} = e^{-E/kT} = e^{-52.4} = 1.7 \times 10^{-23}$$

$$\text{number} = N_A \times e^{-E/kT} = 6.02 \times 10^{23} \times 1.7 \times 10^{-23} \approx 10$$

$$\text{number} = \dots\dots\dots 10 \dots\dots\dots \text{mole}^{-1} [4]$$

- 40 Fig. 40.1 shows a simplified diagram of a d.c. motor with permanent magnets.
 Fig. 40.2 shows the graph of current in the coil against frequency of rotation for this motor.

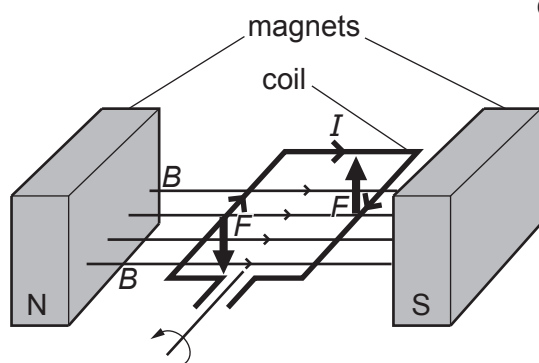


Fig. 40.1

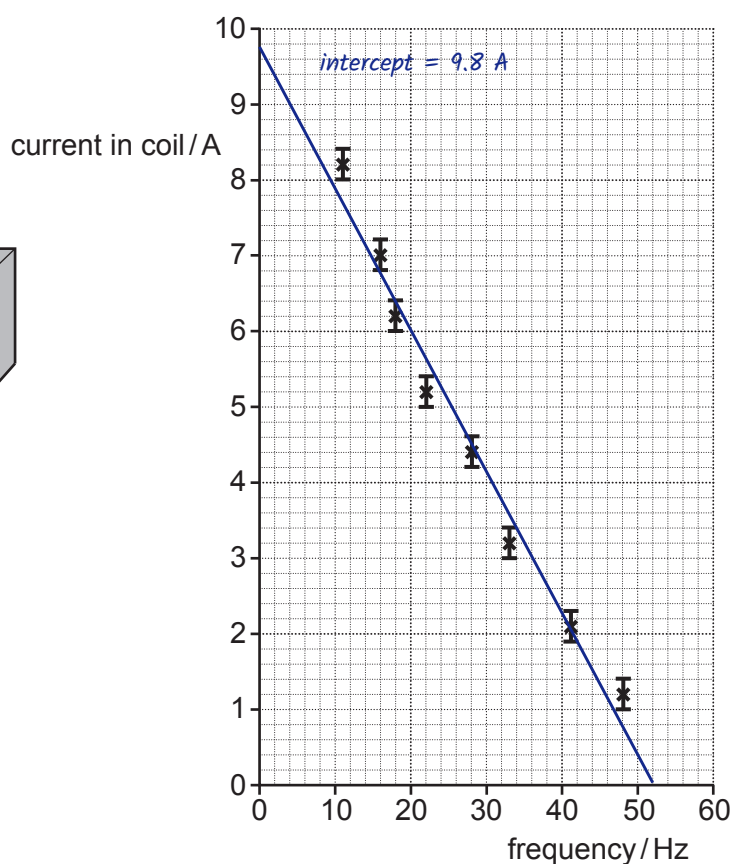


Fig. 40.2

The coil is connected to a 12.0V supply of negligible internal resistance shown in Fig. 40.1. This produces the force to keep the motor turning against a mechanical load.

- (a) Draw a **straight line** of best fit on Fig. 40.2 and use it to predict the current in the coil when the motor is not rotating.
 Use your prediction to calculate the resistance of the coil.

extrapolating the best fit line to $f = 0$ (not rotating, so no back e.m.f.): current = 9.8 A (intercept on the current axis)

$$R = V/I = 12.0 \div 9.8$$

$$R = 1.2 \, \Omega$$

resistance = ...1.2..... Ω [3]

- (b)* This type of d.c. motor is described as a self-regulating device. As more mechanical load is put on the motor it slows down and draws more current from the supply to produce the extra force required.

Use the laws of electromagnetism to explain how this device can act as a self-regulating motor.

When a current flows in the coil in the magnetic field, a force $F = BIL$ acts on each side of the coil, perpendicular to both B and I . The forces on opposite sides are in opposite directions, so they form a couple (torque) that turns the coil.

As the coil rotates it cuts the magnetic flux, so by Faraday's law an e.m.f. is induced: $\varepsilon = -N d\Phi/dt$, the rate of change of flux linkage ($\Phi = BA$), which is proportional to the frequency of rotation.

By Lenz's law (the minus sign) the induced e.m.f. opposes the change causing it, so it acts against the 12.0 V supply: a back e.m.f. The current is $I = (V - \varepsilon)/R$, where R is the coil resistance.

With a light load the motor turns fast, the back e.m.f. is nearly equal to V , so only a small current is drawn (about 1 A at 48 Hz in Fig. 40.2).

When more mechanical load is added the motor slows down. The coil cuts flux more slowly, so the back e.m.f. falls and the current $(V - \varepsilon)/R$ rises. The larger current gives a larger force BIL and torque, so the motor can work harder.

The current adjusts until the torque exactly balances the load, then the motor turns at a new, lower constant rate. If the load is reduced it speeds up, the back e.m.f. rises and the current falls. So the motor regulates its own current to match the load, up to about 9.8 A when stalled.

[6]

41 This question is about the electric field around protons.

- (a) Two protons are separated by $1.0 \times 10^{-9} \text{ m}$ as shown in **Fig. 41.1**. Point **X** is equidistant from each proton as shown.

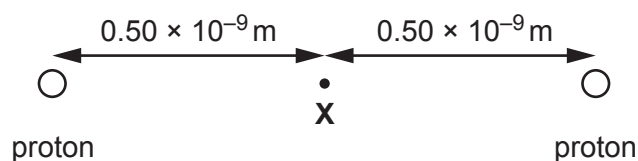


Fig. 41.1 not to scale

- (i) Explain why the electric field strength at **X** is zero.

The fields at X from the two protons are equal in size (same charge, same distance) but opposite in direction, so they add to zero.

[1]

- (ii) Calculate the electric potential at **X**.

$V = kQ/r$ from each proton; potential is a scalar, so add:

$$V = 2 \times 9.0 \times 10^9 \times 1.6 \times 10^{-19} \div 0.50 \times 10^{-9}$$

$$V = 5.8 \text{ V}$$

potential = *5.8* V [2]

Question 41 continues on page 35

- (b) Imagine a third proton is positioned as shown in **Fig. 41.2**.

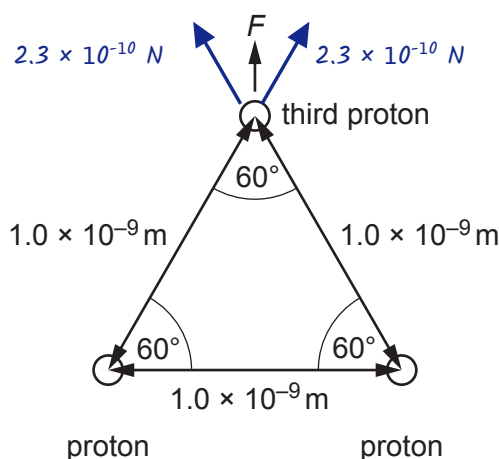


Fig. 41.2 not to scale

- (i) Show that the resultant force F on the third proton is about $4 \times 10^{-10} \text{ N}$ in the direction shown. Explain your reasoning. You may include a diagram in your answer.

$$\text{force from each proton } F = kq^2/r^2 = 9.0 \times 10^9 \times (1.6 \times 10^{-19})^2 \div (1.0 \times 10^{-9})^2$$

$$F = 2.3 \times 10^{-10} \text{ N, repulsive, along each side (shown on Fig. 41.2)}$$

The two forces are equal in size and symmetric about the vertical, so
 their horizontal components ($F \cos 60^\circ$) cancel.
 The vertical components add: $2 \times 2.3 \times 10^{-10} \times \sin 60^\circ = 3.99 \times$
 $10^{-10} \text{ N} \approx 4 \times 10^{-10} \text{ N, vertically upwards as shown.}$ [4]

- (ii) The separation of protons in a lithium ${}^6_3\text{Li}$ nucleus is of the order of 10^{-15} m . Estimate the magnitude of the resultant electric force on a proton in the nucleus if the protons are arranged symmetrically as in **Fig. 41.2**.

$$F \propto 1/r^2, \text{ so multiply by } (10^{-9} \div 10^{-15})^2 = 10^{12}$$

$$F = 3.99 \times 10^{-10} \times 10^{12}$$

$$F = 400 \text{ N}$$

force = ...400..... N [2]

END OF QUESTION PAPER

[illegible]

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