Oxford Cambridge and RSA

A Level Physics B (Advancing Physics)

H557/02 Scientific literacy in physics

Wednesday 21 June 2017 – Morning

Time allowed: 2 hours 15 minutes

You must have:
- the Insert (inserted)
- the Data, Formula and Relationships booklet (sent with general stationery)

You may use:
- a scientific or graphical calculator
- a ruler (cm/mm)

First name	
Last name	StemUp Model Solution

Centre number						Candidate number				

INSTRUCTIONS
- The Insert will be found inside this document.
- Use black ink. You may use an HB pencil for graphs and diagrams.
- Complete the boxes above with your name, centre number and candidate number.
- Answer **all** the questions.
- Write your answer to each question in the space provided. If additional space is required, use the lined page(s) at the end of this booklet. The question number(s) must be clearly shown.
- Do **not** write in the barcodes.

INFORMATION
- The total mark for this paper is **100**.
- The marks for each question are shown in brackets **[ ]**.
- This document consists of **24** pages.

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SECTION A

Answer **all** the questions.

1 This question is about notes produced by a flute.

A flute is an instrument that produces standing waves with displacement antinodes (A) at both ends. The nodes (N) and antinodes for the lowest note possible for a flute of length *L* are shown in Fig. 1.1.

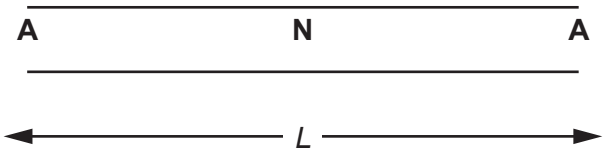

Fig. 1.1

(a) Explain how standing waves are formed in air.

Waves travel along the tube and reflect from the ends of the tube. The incident and reflected waves superpose (interfere) as they pass through one another. Antinodes (A) form where the waves superpose in phase and nodes (N) form where they superpose in antiphase. **[3]**

(b) Mark the antinodes and nodes on Fig. 1.2 for a note of **twice** the frequency of the note indicated in Fig. 1.1. Explain your answer.

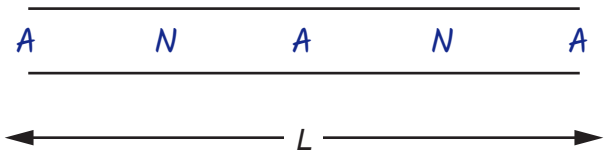

Fig. 1.2

The speed of sound is the same, so for twice the frequency the wavelength must be halved ($v = f\lambda$ with v constant): a full wavelength now fits in L, giving A N A N A. **[2]**

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(c) The velocity of sound in air v is given by the equation $v = \sqrt{\frac{kp}{\rho}}$ where p is the pressure of the gas, ρ is the density of the gas and k is a constant.

Use the expression $pV = nRT$ and the expression for density, $\rho = \frac{m}{V}$, to show that $v = \sqrt{\frac{kRT}{M}}$ where $M = \frac{m}{n}$ is the mass of one mole of air.

$pV = nRT$ and $\rho = m/V$, so $p/\rho = pV/m = nRT/m$

$M = m/n$, so $p/\rho = RT/M$

$v = \sqrt{(kp/\rho)} = \sqrt{(kRT/M)}$

[2]

(d) A flute of length L sounds a note of 262 Hz at a temperature of 293 K. Calculate the frequency of the note from the same length flute when the temperature of the air in the flute has increased to 303 K. The change in length of the flute caused by this temperature rise is negligible.

λ is fixed by the length of the flute and $v = f\lambda$, so $f \propto v \propto \sqrt{T}$

$f_{303} / 262 = \sqrt{(303 / 293)} = 1.017$

$f_{303} = 1.017 \times 262 = 266$ Hz

frequency at 303 K = ...266..... Hz **[3]**

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2 This question is about charging a capacitor in a circuit with two resistors in series.

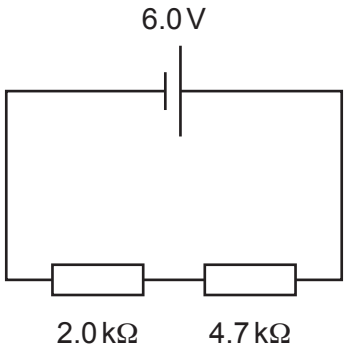

Fig. 2.1

(a) Show that the p.d. across the 4.7 kΩ resistor in the circuit in Fig. 2.1 is about 4 V, assuming that the cell has zero internal resistance.

$V = 6.0 \times 4.7 / (2.0 + 4.7) = 6.0 \times 4.7 / 6.7$

$V = 4.2$ V (4.21 V), which is about 4 V

[2]

(b) A student changes the circuit as shown in Fig. 2.2

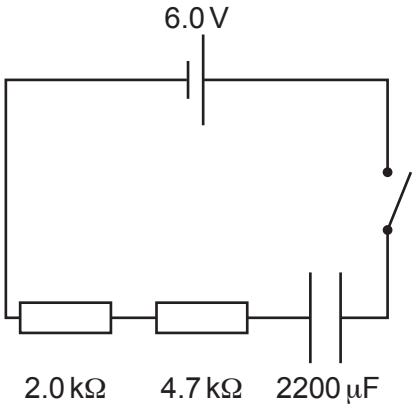

Fig. 2.2

Show that the time constant of the circuit is about 15 s.

total $R = 2.0 + 4.7 = 6.7$ kΩ

$RC = 6.7 \times 10^3\ \Omega \times 2200 \times 10^{-6}$ F

$RC = 14.7$ s, which is about 15 s

[2]

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(c) The graph in Fig. 2.3 shows how the p.d. across the capacitor varies with time up to 5 *RC*. Add a line to the graph that shows how the p.d. across the **4.7 kΩ resistor** varies with time.

Add another line to show how the p.d. across the **2.0 kΩ resistor** varies with time. Label the lines.

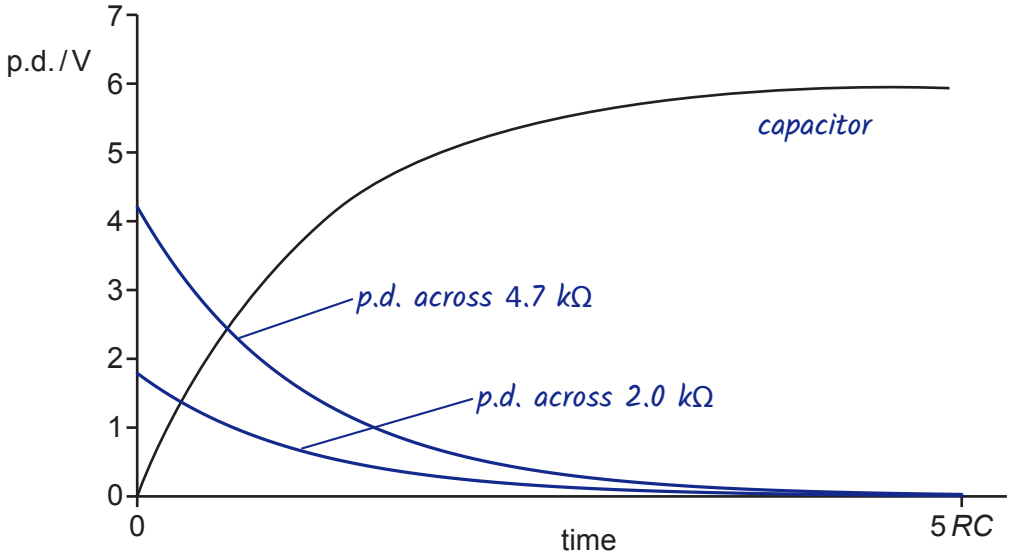

Fig. 2.3

[2]

(d) Calculate the time it takes from the start of the charging for the p.d across the capacitor to reach 5.0 V.

$V_C = V_0(1 - e^{-t/RC})$

$5.0 = 6.0(1 - e^{-t/RC})$, so $e^{-t/RC} = 1 - 5/6 = 1/6$

$-t/RC = \ln(1/6) = -1.79$

$t = 1.79 \times 14.7 = 26.3$ s

time = ...26.3..... s **[4]**

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3 This question is about the force on a sail of a land yacht, a small vehicle that is powered by the wind.

Fig. 3.1

(a) Explain how air particles exert a pressure on a sail and why, when no wind is blowing, the sail experiences the same pressure on both sides.

Air particles are in constant random motion. When they collide with the sail they bounce off, so the particles and the sail experience a change of momentum. The force on the sail is the rate of change of momentum and pressure is force per unit area. With no wind, very large numbers of particles hit both sides, with equal numbers of collisions per second on each side, so the force and pressure are the same on both sides. **[3]**

(b) A sail has an area $8.0\,m^2$. A wind of velocity $18.0\,m\,s^{-1}$ strikes the sail at 90° to the surface of the sail. It is assumed that the velocity of the wind falls to zero when it strikes the sail.

Calculate the force on the sail and suggest why the assumption may not be accurate.

density of air = $1.2\,kg\,m^{-3}$

air hitting sail in 1 s: $m = \rho A v = 1.2 \times 8.0 \times 18.0 = 172.8$ kg

$F = \Delta p/\Delta t = 172.8\ kg\ s^{-1} \times 18.0\ m\ s^{-1} = 3110$ N

The assumption is suspect: if all the air stopped at the sail there would be a build-up of air there; in reality particles bounce off the sail and the sail starts moving.

force on sail = *3110* N **[4]**

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(c) A constant force of 300 N strikes the sail of a land yacht at an angle of 50° to the direction of motion of the vehicle as shown in Fig. 3.2. The mass of the yacht and rider is 135 kg.

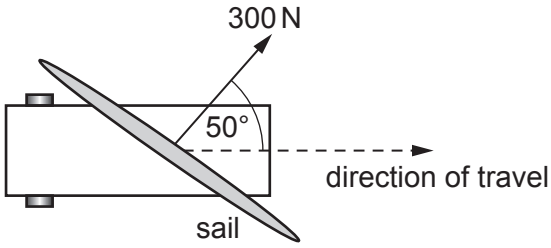

Fig. 3.2

Calculate the time for the land yacht to travel 50 m in the direction shown. The yacht starts from rest. Ignore resistive forces.

accelerating force = 300 cos 50° = 193 N

$a = F/m = 193 / 135 = 1.43\ m\ s^{-2}$

$s = ½at^2$, so $t = \sqrt{(2s/a)} = \sqrt{(2 \times 50 / 1.43)}$

t = 8.4 s

time = ...8.4..... s **[4]**

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SECTION B

Answer **all** the questions.

4 This question is about the New Horizons spacecraft mission to the dwarf planet Pluto.

In July 2015, the Long Range Reconnaissance Imager (LORRI) sent the image shown in Fig. 4.1a.

Fig. 4.1a

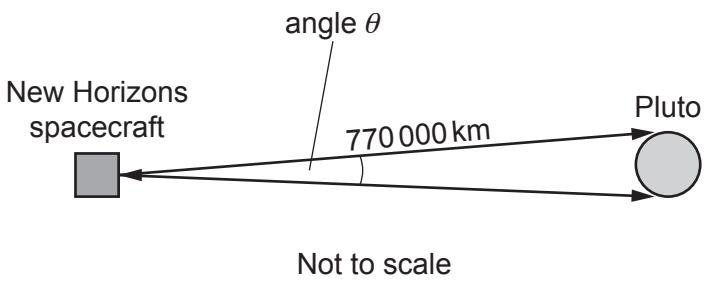

Fig. 4.1b

(a) It takes 4.5 hours for the radio signal from the spacecraft at Pluto to reach the Earth. Calculate the distance of the spacecraft from Earth when the signal was transmitted.

$d = ct = 3.0 \times 10^8 \times 4.5 \times 60 \times 60$

$d = 4.9 \times 10^{12}$ m

distance = ...4.9×10^{12}.... m **[2]**

(b) The square image is 1024 pixels wide. The diameter of Pluto is 2700 km.

(i) Calculate the resolution of the image in km pixel^{-1}.

width of image = 45 mm; diameter of Pluto on image = 27 mm

pixels across Pluto = (27 / 45) × 1024 = 614

resolution = 2700 km / 614 pixels = 4.4 km pixel^{-1}

resolution = ...4.4.... km pixel^{-1} **[3]**

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(ii) The image in Fig. 4.1a was taken at a distance of 770 000 km. The **angular** resolution of LORRI is 5×10^{-6} radian per pixel. This means that each pixel covers an angle of 5×10^{-6} radian. By calculating how many radians Pluto subtends (angle θ in Fig. 4.1b), test whether the value for angular resolution agrees with your value for the resolution in **(b)(i).** Comment on your answer.

θ = 2700 km / 770 000 km = 3.5×10^{-3} rad

pixels across Pluto = $3.5 \times 10^{-3} / 5 \times 10^{-6}$ = 700

resolution = 2700 km / 700 pixels = 3.9 km $pixel^{-1}$

This is the same order of magnitude as, and close to, my value of 4.4 km $pixel^{-1}$ from (b)(i), so the values broadly agree. The difference arises because it is difficult to judge exactly where the edge of Pluto is on Fig. 4.1a, so the number of pixels across its diameter is uncertain.

[4]

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(c)* New Horizons is powered by a radioisotope thermal generator. This produces electrical power from the thermal energy of decaying plutonium-238.

Explain why solar power is not used for this spacecraft. Use the data below to calculate the energy released per second at launch and the reduction in energy released per second when New Horizons reached Pluto. Comment on your results.

Data:

Mean Sun-Pluto distance = 40 × mean Sun-Earth distance

Amount of plutonium-238 carried by spacecraft: 36 mol

Number of plutonium-238 nuclei in one mole: $6.0 \times 10^{23}\,\text{mol}^{-1}$

Half-life of plutonium-238: 87.7 years (2.8×10^{9} s)

Energy released in the decay of one plutonium nucleus: 5.6 MeV

Journey time to Pluto: 9 years

Solar power is not used because sunlight intensity falls with the inverse square of distance from the Sun ($I \propto 1/r^2$). At Pluto r is 40 times larger, so the intensity is $1/40^2 = 1/1600$ of that at Earth: solar cells would give 1600 times less power, far too little.

At launch: $N = 36 \times 6.0 \times 10^{23} = 2.2 \times 10^{25}$ nuclei

$\lambda = \ln 2 / t_{½} = 0.693 / 2.8 \times 10^{9}$ s $= 2.5 \times 10^{-10}$ s^{-1}

activity $A = \lambda N = 2.5 \times 10^{-10} \times 2.16 \times 10^{25} = 5.4 \times 10^{15}$ Bq

power $= 5.4 \times 10^{15} \times 5.6$ MeV s^{-1} $= 3.0 \times 10^{16}$ MeV s^{-1} $= 3.0 \times 10^{16} \times 1.6 \times 10^{-13}$ J s^{-1} = 4800 W

At Pluto: fraction left $= (½)^{9/87.7} = 0.93$, so power $= 0.93 \times 4790 = 4460$ W ≈ 4500 W

Reduction in energy per second = 4790 − 4460 ≈ 330 W, a drop of less than 10% (about 7%).

So the RTG output falls by under 10% over the 9 year journey, while solar power would fall by a factor of 1600: the power loss from the RTG is far less than from the Sun, so the RTG is the sensible choice.

[6]

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5 This question is about the Boltzmann factor, $f = e^{-E/kT}$.

Fig. 5.1 shows how the Boltzmann factor varies with temperature for three processes: **A**, **B** and **C**.

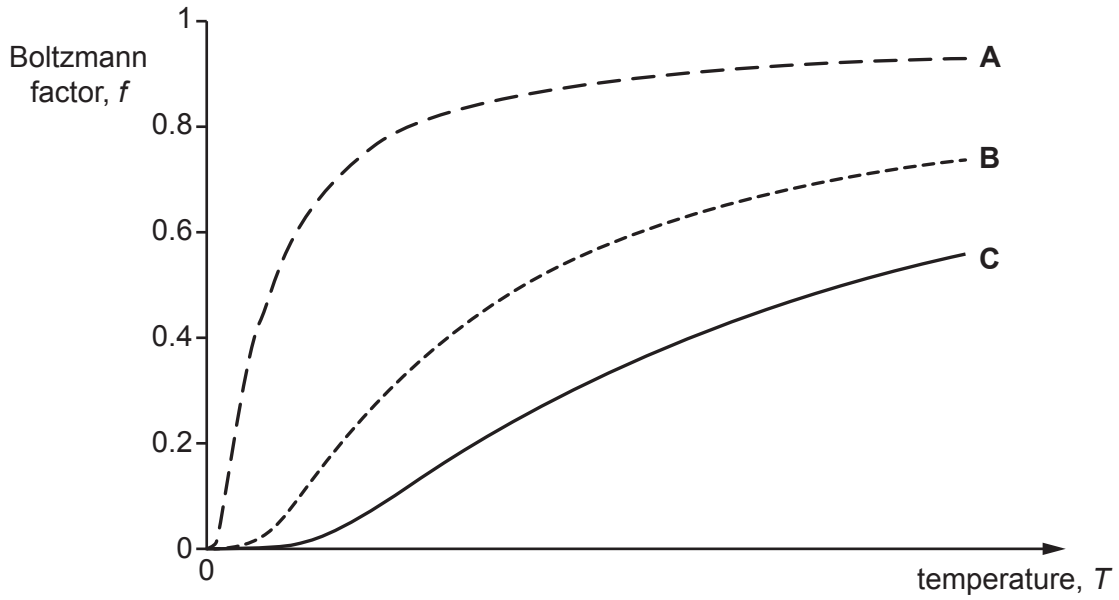

Fig. 5.1

(a) Explain how the graphs in Fig. 5.1 show that line **C** represents the process with the greatest activation energy *E*.

The Boltzmann factor gives the proportion of particles with enough energy (at least E) to undergo the process. A greater E makes E/kT larger, so $e^{-E/kT}$ is smaller: fewer particles have enough energy at any temperature. At every temperature C has the smallest f, so fewest particles can take part and C has the greatest activation energy.

..... **[3]**

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(b) This part of the question is about the evaporation of liquids; the process in which molecules of the liquid gain sufficient energy to enter into the vapour.

(i) The Boltzmann factor for water molecules escaping the liquid and entering the vapour state is 4.9×10^{-8} at 310 K.

Calculate the activation energy required for a water molecule to escape into the vapour state at this temperature.

$f = e^{-E/kT}$, so $\ln f = -E/kT$

$E = -kT \ln f = -1.38 \times 10^{-23} \times 310 \times \ln(4.9 \times 10^{-8})$

$E = 1.38 \times 10^{-23} \times 310 \times 16.8 = 7.2 \times 10^{-20}$ J

activation energy = 7.2×10^{-20} J **[3]**

(ii) Explain how particles with an average energy lower than the activation energy gain enough energy to escape into the vapour.

Particles exchange energy in random collisions with each other. Some particles gain energy in several successive collisions (they get "lucky") until they have at least the activation energy and escape.

[2]

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(iii)* The activation energy for a molecule of ethyl alcohol to escape into the vapour state is 6.6×10^{-20} J.

Calculate the Boltzmann factor at 310 K for this process and use ideas from the question to explain why a drop of ethyl alcohol feels colder on the skin than a drop of water.

$f = e^{-E/kT} = \exp(-6.6 \times 10^{-20} / (1.38 \times 10^{-23} \times 310))$

$f = e^{-15.4} = 2.0 \times 10^{-7}$

This is about 4 times the Boltzmann factor for water at the same temperature ($2.0 \times 10^{-7} / 4.9 \times 10^{-8} \approx 4$).

The rate of evaporation depends on the Boltzmann factor, the fraction of molecules with enough energy to escape, so about 4 times as many alcohol molecules escape per second: alcohol evaporates much faster than water.

The molecules that escape are the most energetic ones, so evaporation lowers the average kinetic energy of the molecules left in the drop. Quicker evaporation means the average energy, and so the temperature, of the remaining liquid falls more quickly.

The skin is the source of energy for the molecules in the drop, so energy is transferred from the skin to the cooler liquid more quickly. The skin loses energy faster, so alcohol feels colder than water.

[6]

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6 This question is about muon decay. Muons are charged leptons. They are formed by cosmic rays interacting with the upper atmosphere.

The decay equation of a negative muon, μ^- is:

$$\mu^- \rightarrow e^- + \bar{\nu} + \nu$$

where $\bar{\nu} + \nu$ represent an antineutrino and a neutrino respectively.

(a) Explain how the decay equation shows that charge and lepton number are both conserved and name one other property that is conserved in the decay.

Charge: −1 on the left and −1 on the right, as the neutrinos are neutral,

Lepton number: the neutrino (+1) and antineutrino (−1) sum to zero, and

the muon and electron each have +1, so +1 on each side. Momentum (or

mass-energy) is also conserved. **[3]**

(b) The maximum total energy of the particles formed from the muon is about 106 MeV.

Show that this suggests that the mass of the muon is about 200 times that of an electron.

electron: $E = m_e c^2 = 9.11 \times 10^{-31} \times (3.0 \times 10^8)^2 = 8.2 \times 10^{-14}$ J

8.2×10^{-14} J / 1.6×10^{-13} J MeV^{-1} = 0.51 MeV

muon rest energy ≈ 106 MeV: m_μ / m_e = 106 / 0.51 = 207 ≈ 200

[3]

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(c) Muons travel through the atmosphere at 98% of the speed of light.
The half-life of a muon at rest is about 1.5×10^{-6} s. Show that about 0.0005% of the original muons will remain after travelling 8 km through the atmosphere, ignoring relativistic effects.

time = 8000 / (0.98 × 3.0 × 10^8) = 2.7 × 10^{-5} s

number of half-lives = 2.72 × 10^{-5} / 1.5 × 10^{-6} = 18.1

fraction left = $(½)^{18.1}$ = 3.6 × 10^{-6} = 0.0004% ≈ 0.0005%

[3]

(d) **(i)** In a measurement it is found that about 9% of the muons remain after travelling through 8 km of atmosphere.
Explain why a greater number of muons remain than suggested by the non-relativistic calculation in **(b)**.

The muons move at 0.98c, an appreciable fraction of the speed of light, so γ is appreciably greater than 1. In our frame the muon half-life is dilated (t = γτ), so fewer half-lives pass and more muons remain.

..... **[3]**

(ii) Use your answer to **(c)** and the measured value of 9% of muons remaining after passing through 8 km of atmosphere to calculate the relativistic factor γ for the muons.

9% left: $(½)^n$ = 0.09, n = log(1/0.09) / log 2 = 3.47

γ = 18.1 half-lives / 3.47 half-lives = 5.2

relativistic factor γ = ...5.2..... **[3]**

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SECTION C

Answer **all** the questions.

This section is based on the Advance Notice article, which is an insert.

7 State the feature of the diagram in Fig. 1 in the article which shows that the distance scale is logarithmic and suggest a possible **disadvantage** of representing data in this manner.

Equal steps along the distance scale represent equal powers of ten (each step is a factor of 10^3). Disadvantage: it is difficult to interpolate (read off) values between the marked powers of ten.

..... **[2]**

8 The density of silver is 10 500 kg m^{-3}. The mass of one silver atom is 1.8×10^{-25} kg.

Use this data to calculate an estimate for the diameter of an atom of silver, explaining your reasoning and assumptions.

number of atoms per m^3 = $10\ 500 / 1.8 \times 10^{-25} = 5.8 \times 10^{28}$

volume occupied by one atom = $1 / 5.8 \times 10^{28} = 1.7 \times 10^{-29}\ m^3$

Assume the atoms are in a simple cubic lattice with no gaps, each atom filling a cube whose side equals the atom's diameter:

diameter = $(1.7 \times 10^{-29})^{1/3} = 2.6 \times 10^{-10}$ m

diameter of silver atom = 2.6×10^{-10} m **[4]**

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9 This question is about an experiment to estimate the resolution of the human eye.

Two vertical, parallel black lines are drawn on a piece of card. The separation between the lines is 2.0 ± 0.5 mm. The card is fixed to a wall at head height.

A group of students look at the card whilst each covering one eye. They walk back from the card until they can no longer separate the two lines. The distance L between the eye and the card is measured.

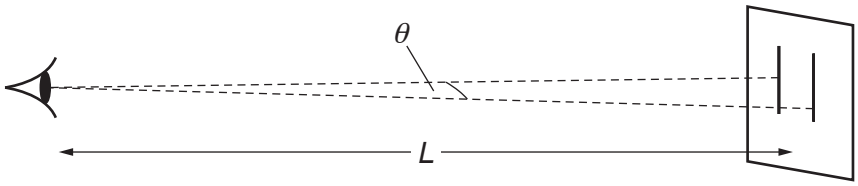

Fig. 9.1

Here are the results from five students:

student	A	B	C	D	E
maximum distance *L* /m	6.2	5.8	6.1	5.9	6.1

(a) **(i)** State the spread of the distance values.

spread = ± .....0.2..... m **[1]**

(ii) A student suggests that the uncertainty in the distance values can be ignored when calculating the minimum angle that can be resolved because of the uncertainty in the separation of the lines on the card. Comment on this suggestion, explaining whether or not you agree.

I agree. The spread in L is ±0.2 m in 6.0 m, about 3%, but the uncertainty in the separation is ±0.5 mm in 2.0 mm, which is 25%. The separation uncertainty is much larger, so the uncertainty in L can be ignored.

..... **[2]**

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(iii) Calculate a value for the minimum angle that can be resolved. Include an estimate of the uncertainty in your value. Explain how you estimated the uncertainty.

mean $L = 6.0$ m: $\theta = s/L = 2.0 \times 10^{-3} / 6.0 = 3.3 \times 10^{-4}$ rad

max $\theta = 2.5 \times 10^{-3} / 5.8 = 4.3 \times 10^{-4}$ rad

min $\theta = 1.5 \times 10^{-3} / 6.2 = 2.4 \times 10^{-4}$ rad

uncertainty $\approx \frac{1}{2}(\text{max} - \text{min}) \approx \pm 1 \times 10^{-4}$ rad

minimum angle that can be resolved = ..3×10^{-4}..... ± ..1×10^{-4}..... rad **[3]**

(b) An approximate value for the minimum resolvable angle θ_{min} can be obtained from the equation $\theta_{min} = \dfrac{\text{wavelength of light}}{\text{diameter of pupil of the eye}}$.

The students estimated the diameter of the pupil to be 3 mm and the wavelength of light to be 5×10^{-7} m. Use the data to estimate the minimum resolvable angle and compare your answer with the value obtained in **(a)(iii)**.

$\theta_{min} = 5 \times 10^{-7} / 3 \times 10^{-3} = 1.7 \times 10^{-4}$ rad ≈ 0.0002 rad

This suggests a slightly better resolution than measured, but it agrees to 1 s.f. with the smallest angle from the experimental data (2.4×10^{-4} rad) once the uncertainty is taken into account.

minimum angle that can be resolved = ...2×10^{-4}..... rad **[2]**

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10 This question is about measuring stellar distances by parallax.

The parallax of the star Sirius is 0.38 arc seconds.

One light year is the distance light travels in one year.

Calculate the distance to Sirius in light years.

Earth-Sun distance = 1 AU = 1.5×10^{11} m
1 year = 3.2×10^{7} seconds

$\theta = 0.38 / 3600 = 1.06 \times 10^{-4}$ degrees $= 1.84 \times 10^{-6}$ rad

$d = 1.5 \times 10^{11} / 1.84 \times 10^{-6} = 8.15 \times 10^{16}$ m

1 ly $= 3.0 \times 10^{8} \times 3.2 \times 10^{7} = 9.6 \times 10^{15}$ m

$d = 8.15 \times 10^{16} / 9.6 \times 10^{15} = 8.5$ light years

distance = ...8.5..... light year **[3]**

11 Explain why turbulence in the atmosphere limits the resolution of ground-based optical telescopes (lines 7–39).

Turbulence causes changing density differences in the air, so different parts of the atmosphere have different refractive indices. Light from the star is refracted and changes direction as it travels through, so the image is distorted (blurred), limiting the resolution.

..... **[2]**

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12* This question is about spectroscopic measurements of stellar distances.

Describe how absorption spectra are formed and how they are useful in establishing the spectral class of a star.
Explain how determining the value for the absolute brightness and apparent brightness of a star can lead to a measurement of the distance to a star.

The following example may help in your explanation:

Star **X** is known to have three times the absolute brightness of star **Y** but both appear to be equally bright in the sky. The distance to star **Y** has been measured as 12 parsecs.

Light (photons of all frequencies) from the hot star passes through the cooler gas in its outer layers. A photon is absorbed only if its energy hf exactly matches the energy difference between two energy levels of an atom, exciting an electron to a higher level. These frequencies are removed, giving dark absorption lines.

Different elements (isotopes) have different energy levels, so different patterns of lines. The position and thickness of the lines identify the spectral class, and stars in a class have a known absolute brightness.

Apparent brightness ∝ absolute brightness / r^2 (inverse-square law): e.g. three times the distance gives 1/9 of the apparent brightness. Comparing absolute and measured apparent brightness therefore gives r.

Example: X and Y appear equally bright, so $3 / r_X^2 = 1 / 12^2$

$r_X^2 = 3 \times 12^2$, so $r_X = 12 \times \sqrt{3} = 20.8$ parsecs

[6]

END OF QUESTION PAPER

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ADDITIONAL ANSWER SPACE

If additional space is required, you should use the following lined page(s). The question number(s) must be clearly shown in the margin(s).

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