OCR
Oxford Cambridge and RSA

GCE

Further Mathematics B MEI

Y420/01: Core Pure

A Level

Mark Scheme for June 2023

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

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MARKING INSTRUCTIONS

PREPARATION FOR MARKING
RM ASSESSOR

1. Make sure that you have accessed and completed the relevant training packages for on-screen marking: *RM Assessor Online Training*; *OCR Essential Guide to Marking*.

2. Make sure that you have read and understood the mark scheme and the question paper for this unit. These are posted on the RM Cambridge Assessment Support Portal http://www.rm.com/support/ca

3. Log-in to RM Assessor and mark the **required number** of practice responses ("scripts") and the **number of required** standardisation responses.

   YOU MUST MARK 5 PRACTICE AND 10 STANDARDISATION RESPONSES BEFORE YOU CAN BE APPROVED TO MARK LIVE SCRIPTS.

MARKING

1. Mark strictly to the mark scheme.

2. Marks awarded must relate directly to the marking criteria.

3. The schedule of dates is very important. It is essential that you meet the RM Assessor 50% and 100% (traditional 40% Batch 1 and 100% Batch 2) deadlines. If you experience problems, you must contact your Team Leader (Supervisor) without delay.

4. If you are in any doubt about applying the mark scheme, consult your Team Leader by telephone or the RM Assessor messaging system, or by email.

5. **Annotations**

Annotation	Meaning
✓and ✗	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
E	Explanation mark 1
SC	Special case
^	Omission sign
MR	Misread
BP	Blank Page
Seen	
Highlighting	

Other abbreviations in mark scheme	Meaning
E1	Mark for explaining a result or establishing a given result
dep*	Mark dependent on a previous mark, indicated by *. The * may be omitted if only one previous M mark
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working
AG	Answer given
awrt	Anything which rounds to
BC	By Calculator
DR	This question included the instruction: In this question you must show detailed reasoning.
BP	Blank Page
Seen	
Highlighting	

6. **Subject Specific Marking Instructions**

a. Annotations must be used during your marking. For a response awarded zero (or full) marks a single appropriate annotation (cross, tick, M0 or ^) is sufficient, but not required.

For responses that are not awarded either 0 or full marks, you must make it clear how you have arrived at the mark you have awarded and all responses must have enough annotation for a reviewer to decide if the mark awarded is correct without having to mark it independently.

It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

Award NR (No Response)
- if there is nothing written at all in the answer space and no attempt elsewhere in the script
- OR if there is a comment which does not in any way relate to the question (e.g. 'can't do', 'don't know')
- OR if there is a mark (e.g. a dash, a question mark, a picture) which isn't an attempt at the question.

Note: Award 0 marks only for an attempt that earns no credit (including copying out the question).

If a candidate uses the answer space for one question to answer another, for example using the space for 8(b) to answer 8(a), then give benefit of doubt unless it is ambiguous for which part it is intended.

b. An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not always be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.

If you are in any doubt whatsoever you should contact your Team Leader.

c. The following types of marks are available.

M

A suitable method has been selected and applied in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using

some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.
A method mark may usually be implied by a correct answer unless the question includes the DR statement, the command words "Determine" or "Show that", or some other indication that the method must be given explicitly.

A
Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

B
Mark for a correct result or statement independent of Method marks.

E
A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

d. When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.

e. The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only – differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

f. Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.)
We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so.
- When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value.
- When a value is not given in the paper accept any answer that agrees with the correct value to 2 s.f. unless a different level of accuracy has been asked for in the question, or the mark scheme specifies an acceptable range.
  NB for Specification A the rubric specifies 3 s.f. as standard, so this statement reads "3 s.f".

Follow through should be used so that only one mark in any question is lost for each distinct accuracy error.
Candidates using a value of 9.80, 9.81 or 10 for g should usually be penalised for any final accuracy marks which do not agree to the value found with 9.8 which is given in the rubric.

g. Rules for replaced work and multiple attempts:
- If one attempt is clearly indicated as the one to mark, or only one is left uncrossed out, then mark that attempt and ignore the others.
- If more than one attempt is left not crossed out, then mark the last attempt unless it only repeats part of the first attempt or is substantially less complete.
- if a candidate crosses out all of their attempts, the assessor should attempt to mark the crossed out answer(s) as above and award marks appropriately.

h. For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A or B mark in the question. Marks designated as cao may be awarded as long as there are no other errors.
If a candidate corrects the misread in a later part, do not continue to follow through. E marks are lost unless, by chance, the given results are established by equivalent working. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

i. If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers, provided that there is nothing in the wording of the question specifying that analytical methods are required such as the bold “In this question you must show detailed reasoning”, or the command words “Show” or “Determine”. Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.

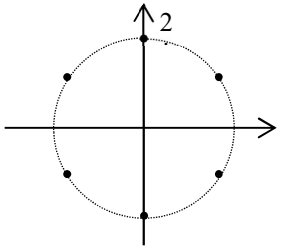
j. If in any case the scheme operates with considerable unfairness consult your Team Leader.

Question			Answer	Marks	AO	Guidance
1	(a)	(i)	$a - \mathrm{i}b$	B1 [1]	1.2	
1	(a)	(ii)	$\mathrm{i}z = -b + a\mathrm{i}$ so $\mathrm{Re}(\mathrm{i}z) = -b$	M1 A1 [2]	1.1 1.1	
1	(b)	(i)	**DR** $\frac{5+\sqrt{3}\mathrm{i}}{2-\sqrt{3}\mathrm{i}} = \frac{(5+\sqrt{3}\,\mathrm{i})\,(2+\sqrt{3}\,\mathrm{i})}{(2-\sqrt{3}\,\mathrm{i})\,(2+\sqrt{3}\,\mathrm{i})}$ $= \frac{7+7\sqrt{3}\mathrm{i}}{7}$ $= 1+\sqrt{3}\mathrm{i}$	M1 A1 [2]	1.1a 1.1	 an intermediate step must be seen before final answer
1	(b)	(ii)	$\lvert 1+\sqrt{3}\mathrm{i}\rvert = 2$ $\arg(1+\sqrt{3}\,\mathrm{i}) = \frac{\pi}{3}$ so $w = 2(\cos\frac{\pi}{3} + \mathrm{i}\sin\frac{\pi}{3})$	B1ft B1 [2]	1.1 1.1	for either their modulus or argument soi cao. Allow 60°

Question			Answer	Marks	AO	Guidance
2			**DR**			
			Normal to plane is $-\mathbf{i} + 3\mathbf{j} + 2\mathbf{k}$	**B1**	**1.1a**	soi
			Angle between $3\mathbf{i} + 2\mathbf{j} + \mathbf{k}$ and $-\mathbf{i} + 3\mathbf{j} + 2\mathbf{k}$ is θ $\cos\theta = \frac{3\times(-1)+2\times3+1\times2}{\sqrt{3^2+2^2+1^2}\sqrt{(-1)^2+3^2+2^2}} = \frac{5}{\sqrt{14}\sqrt{14}}$	**M1**	**1.1**	use of scalar product formula with their normal seen
			$\Rightarrow \theta = 69.07\ldots$	**A1**	**1.1**	or $1.2\ldots$ rads or $\arccos\frac{5}{14}$
			$90 -$ their θ	**M1**	**1.1**	or $\frac{\pi}{2} -$ their θ
			so angle with plane is 20.9°	**A1**	**2.2a**	or 0.365 rads
			Alternative method 1			
			Normal to plane is $-\mathbf{i} + 3\mathbf{j} + 2\mathbf{k}$	**B1**		soi
			Angle between $3\mathbf{i} + 2\mathbf{j} + \mathbf{k}$ and the plane is θ $\sin\theta = \frac{3\times(-1)+2\times3+1\times2}{\sqrt{3^2+2^2+1^2}\sqrt{(-1)^2+3^2+2^2}} = \frac{5}{\sqrt{14}\sqrt{14}}$	**M2**		
			$\theta = 20.9°$	**A2**		or 0.365 rads
			Alternative method 2			
			Normal to plane is $-\mathbf{i} + 3\mathbf{j} + 2\mathbf{k}$	**B1**		soi
			Angle between $3\mathbf{i} + 2\mathbf{j} + \mathbf{k}$ and $-\mathbf{i} + 3\mathbf{j} + 2\mathbf{k}$ is θ $\sin\theta = \frac{\left\lvert\begin{pmatrix}3\\2\\1\end{pmatrix}\times\begin{pmatrix}-1\\3\\2\end{pmatrix}\right\rvert}{\sqrt{3^2+2^2+1^2}\sqrt{(-1)^2+3^2+2^2}} = \frac{\left\lvert\begin{pmatrix}1\\-7\\11\end{pmatrix}\right\rvert}{\sqrt{14}\sqrt{14}}$	**M1**		complete method with vector product seen
			$\Rightarrow \theta = 69.07\ldots$	**A1**		or $1.2\ldots$ rads or $\arcsin\frac{\sqrt{171}}{14}$
			$90 -$ their θ	**M1**		or $\frac{\pi}{2} -$ their θ
			so angle with plane is 20.9°	**A1**		or 0.365 rads
				[5]		

Question			Answer	Marks	AO	Guidance
3	(a)		$\frac{1}{r(r+2)} = \frac{A}{r} + \frac{B}{(r+2)}$			
			$1 = A(r+2) + Br$	M1	1.1	
			$r = 0 \Rightarrow A = \frac{1}{2}, \quad r = -2 \Rightarrow B = -\frac{1}{2}$	A1	1.1	
			$\sum_{r=1}^{n} \frac{1}{r(r+2)} = \frac{1}{2}\sum_{r=1}^{n}\left(\frac{1}{r} - \frac{1}{r+2}\right)$			
			$= k\left[1 - \frac{1}{3} + \frac{1}{2} - \frac{1}{4} + \frac{1}{3} - \frac{1}{5} + \ldots + \frac{1}{n} - \frac{1}{n+2}\right]$	M1	1.1	enough terms to show consistent cancellation in their series
			$= \frac{1}{2}\left[1 + \frac{1}{2} - \frac{1}{n+1} - \frac{1}{n+2}\right]$	A1	1.1	
			$= \frac{3}{4} - \frac{2n+3}{2(n+1)(n+2)}$	A1	1.1	
				[5]		
3	(b)		$\frac{3}{4}$	B1	2.2a	
				[1]		

Question			Answer	Marks	AO	Guidance
4	(a)	(i)	$f'(x) = (1+2x)^{-\frac{1}{2}}$ $f''(x) = -(1+2x)^{-\frac{3}{2}}$	B1 B1 [2]	1.1 1.1	
4	(a)	(ii)	$f(0) = 1, f'(0) = 1, f''(0) = -1$ $1 + x - \frac{1}{2}x^2$	 M1 A1 [2]	 1.1 1.1	 Their f(0), f'(0) and f''(0) evaluated and substituted into Maclaurin Must come from correct expressions for $f'(x)$, $f''(x)$; cannot come from binomial expansion. Ignore subsequent terms.
4	(b)		$\sqrt{1+2\times\frac{1}{8}}$ or $1+\frac{1}{8}-\frac{1}{2}\left(\frac{1}{8}\right)^2$ $\Rightarrow \sqrt{5} \approx \frac{143}{64}$	M1 A1 [2]	3.1a 2.2a	using $x = \frac{1}{8}$ in their expansion **AG**

Question			Answer	Marks	AO	Guidance
5	(a)		**DR** Let $z = r(\cos\theta + \mathrm{i}\sin\theta)$ or $z = re^{i\theta}$ $z^6 = 64(\cos\pi + \mathrm{i}\sin\pi)$ or $64e^{i\pi}$ $\Rightarrow r = 2$ $z = 2e^{i\pi/6}, 2e^{i\pi/2}, 2e^{5i\pi/6}, 2e^{-i\pi/6}, 2e^{-i\pi/2}, 2e^{-5i\pi/6}$	**M1** **B1** **A1** **A1** **[4]**	**1.1** **1.1** **2.5** **1.1**	condone $-\pi$ for π soi 1 correct all correct or $2e^{7i\pi/6}, 2e^{3i\pi/2}, 2e^{11i\pi/6}$
5	(b)			**M1** **A1** **A1** **[3]**	**1.1** **1.1** **1.1**	six roots lying on approximate circle centre O forming an approximate regular hexagon root at 2i or -2i oe indicated. If part (a) contains incorrect roots do not award final A1.

Question			Answer	Marks	AO	Guidance
6	(a)		**DR** **MN** = $\begin{pmatrix}0 & 1\\2 & 0\end{pmatrix}$ or $\begin{pmatrix}0 & 1\\1 & 0\end{pmatrix}\begin{pmatrix}2 & 0\\0 & 1\end{pmatrix} = \begin{pmatrix}0 & 1\\2 & 0\end{pmatrix}$ **NM** = $\begin{pmatrix}0 & 2\\1 & 0\end{pmatrix}$ or $\begin{pmatrix}2 & 0\\0 & 1\end{pmatrix}\begin{pmatrix}0 & 1\\1 & 0\end{pmatrix} = \begin{pmatrix}0 & 2\\1 & 0\end{pmatrix}$ so not commutative	**M1** **A1*** **A1** **[3]**	**1.1a** **1.1** **2.2a**	both **MN** and **NM** calculated both correct dep A1*
6	(b)	(i)	**M** is reflection in $y = x$	**B1** **[1]**	**1.1**	
6	(b)	(ii)	**N** is stretch parallel to the x-axis scale factor 2	**M1** **A1** **[2]**	**1.1** **1.1**	
6	(c)		order of transformations matters	**B1** **[1]**	**2.2a**	must refer to transformations not just matrices
6	(d)		$\begin{pmatrix}2 & 0\\0 & 1\end{pmatrix}\begin{pmatrix}x\\y\end{pmatrix} = \begin{pmatrix}2x\\y\end{pmatrix}$ or $\begin{pmatrix}2 & 0\\0 & 1\end{pmatrix}\begin{pmatrix}x\\mx+c\end{pmatrix} = \begin{pmatrix}2x\\mx+c\end{pmatrix}$ y-coordinate unchanged so lines parallel to x-axis invariant	**M1** **A1** **[2]**	**2.1** **2.2a**	Allow SC1 for correct geometrical argument, e.g. stretch in x-direction leaves y-coordinates unchanged www. Must refer to invariant lines.

Question			Answer	Marks	AO	Guidance
7	(a)		A: $r = a$, $\theta = 0$ B: $r = -a$, $\theta = \pi/2$ C: $r = 3a$, $\theta = 3\pi/2$	**B1** **B1** **B1** **[3]**	**1.1** **1.1** **1.1**	or $\theta = 2\pi$
7	(b)		$\sin\theta > \frac{1}{2}$ $\frac{1}{6}\pi, \frac{5}{6}\pi$ $\frac{1}{6}\pi < \theta < \frac{5}{6}\pi$	**M1** **A1** **A1** **[3]**	**3.1a** **1.1** **1.1**	Allow $\sin\theta = \frac{1}{2}$ (or $< \frac{1}{2}$ or $\leq \frac{1}{2}$ or $\geq \frac{1}{2}$) both condone ≤ for <

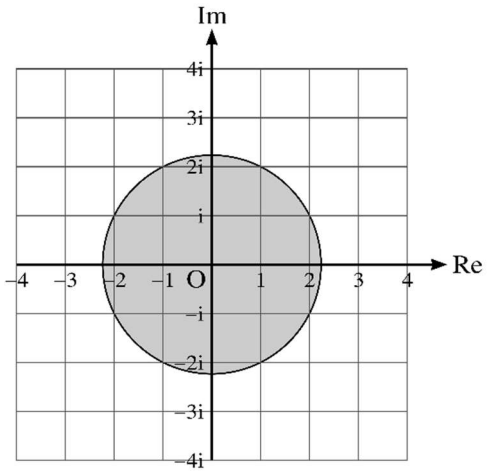
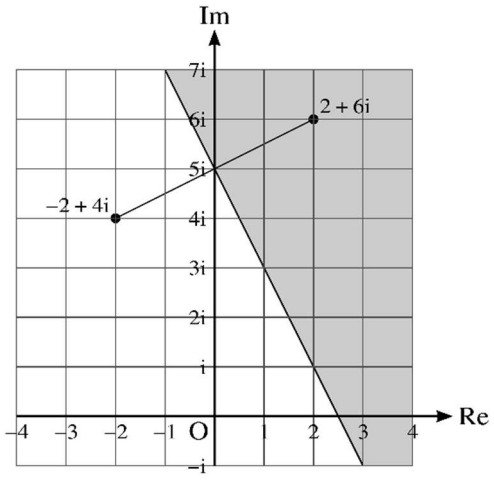
Question			Answer	Marks	AO	Guidance
8			when $n = 1$, $8^n - 3^n = 5$ div by 5	**B1**	**2.1**	
			[Assume true when $n = k$] so $8^k = 3^k + 5m$	**M1**	**2.1**	or $3^k = 8^k - 5m$ or $8^k - 3^k = 5m$ or $8^k - 3^k$ div 5
			$8^{k+1} - 3^{k+1} = 8(3^k + 5m) - 3\times3^k$	**M1**	**2.1**	assumption used
			$= 5\times3^k + 40m = 5(3^k + 8m)$ div by 5	**A1**	**2.2a**	successful completion $3^k = 8^k - 5m$ used $\Rightarrow 5(8^k + 3m)$ div 5 www $8^k - 3^k = 5m$ used $\Rightarrow 5(8m + 3^k)$ div 5 www
			so if true for $n = k$ then true for $n = k+1$			
			As true for $n = 1$, true for all n.	**A1**	**2.4**	must receive all previous marks for this to be awarded
			Alternative method			
			when $n = 1$, $8^n - 3^n = 5$ div by 5	**B1**		
			[Assume true when $n = k$] so $u_k = 8^k - 3^k = 5m$	**M1**		
			$u_{k+1} - u_k = 8^{k+1} - 3^{k+1} - (8^k - 3^k)$	**M1**		considering difference between u_{k+1} and u_k
			$= 2(8^k - 3^k) + 5(8^k)$			
			$= 2(5m) + 5(8^k) = 5(2m + 8^k)$ div by 5	**A1**		
			so if true for $n = k$ then true for $n = k+1$			
			As true for $n = 1$, true for all n.	**A1**		must receive all previous marks for this to be awarded
				[5]		

Question			Answer	Marks	AO	Guidance
9			$k\int_0^{\frac{2\pi}{n}} \sin^2 nt \, \mathrm{d}t = \frac{1}{2}k\int_0^{\frac{2\pi}{n}} (1-\cos 2nt)\mathrm{d}t$	M1* A1	3.1a 1.1	use of double angle formula for $\sin^2 nt$
			$= \frac{1}{2}k\left[t - \frac{1}{2n}\sin 2nt\right]_0^{\frac{2\pi}{n}}$	M1dep	1.1	$\left[t - \frac{1}{2n}\sin 2nt\right]$
			$= \frac{1}{2}a^2\frac{2\pi}{n} = \frac{\pi a^2}{n}$	A1	1.1	www
			mean value of $I^2 = \frac{\pi a^2}{n} \Big/ \frac{2\pi}{n} = \frac{a^2}{2}$	M1	1.1	for dividing by $\frac{2\pi}{n}$
			$\Rightarrow$ RMS value $= \frac{a}{\sqrt{2}}$	A1	2.2a	www **AG**
			Alternative method			
			$\frac{1}{\left(\frac{2\pi}{n}\right)}k\int_0^{\frac{2\pi}{n}} \sin^2 nt \, \mathrm{d}t = \frac{n}{2\pi}k\int_0^{\frac{2\pi}{n}} \sin^2 nt \, \mathrm{d}t$	M1	1.1	for dividing their integral by $\frac{2\pi}{n}$
			$= \frac{1}{2}\times\frac{n}{2\pi}k\int_0^{\frac{2\pi}{n}} (1-\cos 2nt)\mathrm{d}t$	M1* A1	3.1a 1.1	use of double angle formula for $\sin^2 nt$
			$= \frac{n}{4\pi}k\left[t - \frac{1}{2n}\sin 2nt\right]_0^{\frac{2\pi}{n}}$	M1dep	1.1	$\left[t - \frac{1}{2n}\sin 2nt\right]$
			$= \frac{a^2 n}{4\pi}\left(\frac{2\pi}{n}\right) = \frac{a^2}{2}$	A1	1.1	www
			$\Rightarrow$ RMS value $= \frac{a}{\sqrt{2}}$	A1	2.2a	www **AG**
				[6]		

Question			Answer	Marks	AO	Guidance
10	(a)		$\alpha+\beta+\alpha+\beta=4 \quad [\Rightarrow \alpha+\beta=2]$	B1	3.1a	
			$\alpha\beta+(\alpha+\beta)\alpha+(\alpha+\beta)\beta=7$ $\Rightarrow \alpha^2+\beta^2+3\alpha\beta=7$	B1	1.1	or $\alpha\beta+2\alpha+2\beta=7$ or $\alpha\beta+2(\alpha+\beta)=7$
			$x+\frac{3}{x}=2$ or $3x(2-x)+(2-x)^2+x^2=7$	M1	3.1a	substitution which could lead to a quadratic in α or β or x
			$\Rightarrow x^2-2x+3=0$	A1	1.1	could be in α or β
			$\Rightarrow x=\frac{2\pm\sqrt{-8}}{2}=1\pm i\sqrt{2}$	M1	1.1	a method to solve their quadratic
			so roots are $1+i\sqrt{2}$, $1-i\sqrt{2}$ and 2	A1 [6]	2.2a	
10	(b)		$[c=]-6$	B1 [1]	2.2a	

Question			Answer	Marks	AO	Guidance
11			$\frac{dy}{dx} - 2y\frac{\sinh x}{\cosh x} = 1$	B1	3.1a	$\frac{dy}{dx} - 2y\tanh x = 1$
			IF is $e^{\int -\frac{2\sinh x}{\cosh x}\,dx}$	M1	2.1	or $e^{\int -2\tanh x\ dx}$. Integral must come from an attempt to get $\frac{dy}{dx}$ on its own
			$= e^{-2\ln\cosh x} = \left(e^{\ln \operatorname{sech} x}\right)^2 = \operatorname{sech}^2 x$	A1	2.2a	
			$\frac{d}{dx}(y\operatorname{sech}^2 x) = \operatorname{sech}^2 x$	M1	2.1	or multiplying through by their IF
			$y\operatorname{sech}^2 x = \int \operatorname{sech}^2 x\,dx + c = \tanh x + c$	A1	1.1	
			substituting $x = 0,\ y = 1$ gives $c = 1$	M1	1.1	substituting $x = 1$ and $y = 1$ to lead to a value for c
			$y = \cosh^2 x\,(\tanh x + 1)$	A1	2.2a	oe, e.g. $\cosh x\,(\sinh x + \cosh x)$ or $e^x \cosh x$
				[7]		

Question			Answer	Marks	AO	Guidance
12			Considering $\left(z-\frac{1}{z}\right)^5$	M1	3.1a	
			$32\text{i}\sin^5\theta$	B1	1.1	seen at any stage
			$=z^5-5z^3+10z-10\frac{1}{z}+5\frac{1}{z^3}-\frac{1}{z^5}$	M1	1.1	expansion of $\left(z-\frac{1}{z}\right)^5$
			$=z^5-\frac{1}{z^5}-5\left(z^3-\frac{1}{z^3}\right)+10\left(z-\frac{1}{z}\right)$	A1	2.1	correct expansion with z^n, $\frac{1}{z^n}$ terms paired and factorised
			Using $z^n-\frac{1}{z^n}=2\text{i}\sin n\theta$ with sum of terms	M1	2.1	FT their expansion
			$=2\text{i}\sin 5\theta-10\text{i}\sin 3\theta+20\text{i}\sin\theta$	A1	1.1	i must appear in each term
			$\Rightarrow\sin^5\theta=\frac{1}{16}\sin 5\theta-\frac{5}{16}\sin 3\theta+\frac{5}{8}\sin\theta$	A1	2.2a	www
			Alternative method 1			
			Considering $\left(\text{e}^{\text{i}\theta}-\text{e}^{-\text{i}\theta}\right)^5$	M1		
			$32\text{i}\sin^5\theta$	B1		
			$=\text{e}^{5\text{i}\theta}-5\text{e}^{3\text{i}\theta}+10\text{e}^{\text{i}\theta}-10\text{e}^{-\text{i}\theta}+5\text{e}^{-3\text{i}\theta}-\text{e}^{-5\text{i}\theta}$	M1		expansion of $\left(\text{e}^{\text{i}\theta}-\text{e}^{-\text{i}\theta}\right)^5$
			$=\text{e}^{5\text{i}\theta}-\text{e}^{-5\text{i}\theta}-5\left(\text{e}^{3\text{i}\theta}-\text{e}^{-3\text{i}\theta}\right)+10(\text{e}^{\text{i}\theta}-\text{e}^{-\text{i}\theta})$	A1		correct expansion with $\text{e}^{\text{i}\theta}$, $\text{e}^{-\text{i}\theta}$ terms paired and factorised
			Using $\text{e}^{\text{i}\theta}-\text{e}^{-\text{i}\theta}=2\text{i}\sin n\theta$ with sum of terms	M1		FT their expansion
			$=2\text{i}\sin 5\theta-10\text{i}\sin 3\theta+20\text{i}\sin\theta$	A1		i must appear in each term
			$\Rightarrow\sin^5\theta=\frac{1}{16}\sin 5\theta-\frac{5}{16}\sin 3\theta+\frac{5}{8}\sin\theta$	A1		www
			Alternative method 2			
			Equating Im components of $(\cos\theta+\text{i}\sin\theta)^5$			using binomial expansion and de Moivre's theorem
			$\sin 5\theta=5\cos^4\theta\sin\theta-10\cos^2\theta\sin^3\theta+\sin^5\theta$	B1		
			$=5(1-\sin^2\theta)^2\sin\theta-10(1-\sin^2\theta)\sin^3\theta+\sin^5\theta$	M1*		correct expression for $\sin 5\theta$ and substituting in $\cos^2\theta=1-\sin^2\theta$
			$\sin 5\theta=16\sin^5\theta-20\sin^3\theta+5\sin\theta$	A1		or $16\sin^5\theta=\sin 5\theta+20\sin^3\theta-5\sin\theta$ or any correct rearrangement
			Equating Im components of $(\cos\theta+\text{i}\sin\theta)^3$			using binomial expansion and de Moivre's theorem
			$\sin 3\theta=3\cos^2\theta\sin\theta-\sin^3\theta$	M1*		correct expression for $\sin 3\theta$ in terms of $\sin\theta$ and $\cos\theta$
			$\sin^3\theta=\frac{3}{4}\sin\theta-\frac{1}{4}\sin 3\theta$	A1		or $\sin 3\theta=3\sin\theta-4\sin^3\theta$ or any correct rearrangement
			$\Rightarrow 16\sin^5\theta=\sin 5\theta+20\left(\frac{3}{4}\sin\theta-\frac{1}{4}\sin 3\theta\right)-5\sin\theta$	M1dep		substituting expression for $\sin^3\theta$ into $\sin^5\theta$.
			$\Rightarrow\sin^5\theta=\frac{1}{16}\sin 5\theta-\frac{5}{16}\sin 3\theta+\frac{5}{8}\sin\theta$	A1		www
				[7]		

Question			Answer	Marks	AO	Guidance
13	(a)	(i)		**M1** **A1** **A1** **[3]**	**1.1** **1.1** **1.1**	circle, centre O radius $\sqrt{5}$ shaded inside (oe). Candidates may shade the region that is not required, but should clearly indicate that what they have shaded is not required.
13	(a)	(ii)		**M1** **A1** **A1** **[3]**	**1.1** **1.1** **1.1**	(–2, 4) and (2, 6) identified perpendicular bisector of (–2, 4) and (2, 6) shaded on RHS of line (oe). Candidates may shade the region that is not required, but should clearly indicate that what they have shaded is not required.

Question			Answer	Marks	AO	Guidance
13	(b)		gradient = –2	M1	1.1	
			passing through (0, 5)	B1	3.1a	
			equation $y = -2x + 5$	A1	1.1	oe. Allow inequality. Could be obtained from diagram in (a).
			circle is $x^2 + y^2 = 5$	B1	3.1a	allow inequality
			$x^2 + (5 - 2x)^2 = 5$	M1	2.1	or $\left(\frac{5}{2} - \frac{y}{2}\right)^2 + y^2 = 5$. Must be an equation.
			$\Rightarrow 5x^2 - 20x + 20 = 0$	M1	1.1	simplifying to a three-term quadratic equation
			$\Rightarrow x = 2$ [only]	A1*	2.2a	or $y = 1$ [only]
			[unique solution is] $z = 2 + i$	A1dep	3.2a	
			Alternative method			
			$(x + 2)^2 + (y - 4)^2 = (x - 2)^2 + (y - 6)^2$	M1		squaring both sides of equations or inequality
				M1		expanding all four sets of brackets
			$y = -2x + 5$	A1		oe. Allow inequality.
			circle is $x^2 + y^2 = 5$	B1		allow inequality
			$x^2 + (5 - 2x)^2 = 5$	M1		or $\left(\frac{5}{2} - \frac{y}{2}\right)^2 + y^2 = 5$. Must be an equation.
			$\Rightarrow 5x^2 - 20x + 20 = 0$	M1		simplifying to a three term quadratic equation
			$\Rightarrow x = 2$ [only]	A1*		or $y = 1$ [only]
			[unique solution is] $z = 2 + i$	A1dep		
				[8]		

Question			Answer	Marks	AO	Guidance
14	(a)		$\begin{vmatrix} k & 0 & -1 \\ -1 & k & 2 \\ 2k & 2 & 3 \end{vmatrix} = k(3k-4) - 1(-2-2k^2)$	M1	1.1	considering correct determinant
				M1	1.1	finding determinant using any row or column
			$= 5k^2 - 4k + 2$	A1	1.1	
			discriminant $= 16 - 40 = -24 < 0$	M1	3.1a	oe, e.g. completing the square, considering quadratic formula or showing no real roots
			so determinant is never zero $\Rightarrow$ planes always meet at a point	A1	2.2a	www. Both statements required.
				[5]		
14	(b)		$\mathbf{M}^{-1} = \frac{1}{5k^2-4k+2}\begin{pmatrix} 3k-4 & -2 & k \\ 4k+3 & 5k & -2k+1 \\ -2-2k^2 & -2k & k^2 \end{pmatrix}$	M1	1.1	at least 5 cofactors correct (need not be in matrix)
				A1	1.1	all cofactors correct
				M1	1.1	cofactor matrix transposed
				M1	3.1a	Multiplying by $\frac{1}{\text{their determinant}}$
				A1	1.1	correct inverse
			$\mathbf{M}^{-1}\begin{pmatrix} 2 \\ 1 \\ 0 \end{pmatrix} = \frac{1}{5k^2-4k+2}\begin{pmatrix} 6k-10 \\ 13k+6 \\ -4k^2-2k-4 \end{pmatrix}$	M1	1.1	finding $\mathbf{M}^{-1}\begin{pmatrix} 2 \\ 1 \\ 0 \end{pmatrix}$
			$\left(\frac{6k-10}{5k^2-4k+2}, \frac{13k+6}{5k^2-4k+2}, \frac{-4k^2-2k-4}{5k^2-4k+2}\right)$	A2,1,0	1.1, 1.1	Award A1 for one of x, y or z coordinates correct or all three correct FT their determinant
				[8]		

Question			Answer	Marks	AO	Guidance
15			**DR** $1 + 2x - x^2 = -(x^2 - 2x) + 1 = -(x-1)^2 + 2$	**M1** **A1**	**3.1a** **1.1**	completing the square
			$\left[\arcsin\frac{x-1}{k}\right]_1^2$	**M1**	**2.1**	
			$= \left[\arcsin\frac{x-1}{\sqrt{2}}\right]_1^2$	**A1**	**2.1**	
			$= \arcsin\left(\frac{1}{\sqrt{2}}\right) - \arcsin 0 = \frac{\pi}{4}$	**A1**	**2.2a**	substitution or evaluation of both limits must be seen
			Alternative method $1 + 2x - x^2 = -(x^2 - 2x) + 1 = -(x-1)^2 + 2$	**M1** **A1**		completing the square
			Let $u = x - 1$ $\int_0^1 \frac{1}{\sqrt{2-u^2}}\,\mathrm{d}u$	**M1**		complete substitution including limits
			$= \left[\arcsin\frac{u}{\sqrt{2}}\right]_0^1$	**A1**		
			$= \arcsin\left(\frac{1}{\sqrt{2}}\right) - \arcsin 0 = \frac{\pi}{4}$	**A1**		substitution or evaluation of both limits must be seen
				[5]		

Question			Answer	Marks	AO	Guidance
16			Distance from point to plane $= \frac{\lvert 2\times4+1\times1+0\times2\rvert}{\sqrt{2^2+1^2+2^2}}$	M1*	3.1a	
			= 3 units	A1	1.1	
			Line is $\mathbf{r} = 3\mathbf{i}+\mathbf{j}-5\mathbf{k}+\boldsymbol{\lambda}(2\mathbf{i}+b\mathbf{j}+3\mathbf{k})$	M1	3.1a	
			$\overrightarrow{\boldsymbol{AP}} = \mathbf{i}+5\mathbf{k}$	A1	2.1	or $-\overrightarrow{\boldsymbol{AP}}$. Could be seen as part of distance calculation.
			$\overrightarrow{\boldsymbol{AP}} \times \boldsymbol{d} = (\mathbf{i}+5\mathbf{k}) \times (2\mathbf{i}+b\mathbf{j}+3\mathbf{k})$	M1	2.1	or $\boldsymbol{d} \times \overrightarrow{\boldsymbol{AP}}$
			$= -5b\mathbf{i}+7\mathbf{j}+b\mathbf{k}$	A1	2.1	
			dist from P to line			
			$\frac{\lvert -5b\mathbf{i}+7\mathbf{j}+b\mathbf{k}\rvert}{\lvert\boldsymbol{d}\rvert} = \frac{\sqrt{26b^2+49}}{\sqrt{13+b^2}}$	M1*	3.1a	
				A1	1.1	
			so $\frac{26b^2+49}{13+b^2} = 9 \Rightarrow 26b^2+49 = 117+9b^2$	M1dep	2.1	equating the two distances
			$\Rightarrow b = 2$	A1	3.2a	
			Alternative method 1			
			Distance from point to plane $= \frac{\lvert 2\times4+1\times1+0\times2\rvert}{\sqrt{2^2+1^2+2^2}}$	M1*		
			= 3 units	A1		
			Line is $\mathbf{r} = 3\mathbf{i}+\mathbf{j}-5\mathbf{k}+\lambda(2\mathbf{i}+b\mathbf{j}+3\mathbf{k})$	M1		
			$(2\lambda-1)\mathbf{i}+b\lambda\mathbf{j}+(3\lambda-5)\mathbf{k}$	A1		vector from P to a point on the line
			$\begin{pmatrix}2\lambda-1\\ b\lambda\\ 3\lambda-5\end{pmatrix}\cdot\begin{pmatrix}2\\ b\\ 3\end{pmatrix} = 0$	M1*		
			$\lambda = \frac{17}{13+b^2}$	A1		
			dist from P to line	M1		substituting λ into $\lvert\overrightarrow{\boldsymbol{AP}}\rvert$
			$\sqrt{\left(2\left(\frac{17}{13+b^2}\right)-1\right)^2+\left(b\left(\frac{17}{13+b^2}\right)\right)^2+\left(3\left(\frac{17}{13+b^2}\right)-5\right)^2}$			
			$= \frac{\sqrt{26b^4+387b^2+637}}{13+b^2}$	A1		simplified
			So $\frac{26b^4+387b^2+637}{(13+b^2)^2} = 9$	M1dep		equating the two distances
			$\Rightarrow 17b^4+153b^2-884 = 0$			
			$\Rightarrow b = 2$	A1		

Question	Answer	Marks	AO	Guidance
	Alternative method 2			
	Distance from point to plane = $\frac{\lvert 2\times 4+1\times 1+0\times 2\rvert}{\sqrt{2^2+1^2+2^2}}$	**M1***		
	= 3 units	**A1**		
	Line is $\mathbf{r} = 3\mathbf{i} + \mathbf{j} - 5\mathbf{k} + \lambda(2\mathbf{i} + b\mathbf{j} + 3\mathbf{k})$	**M1**		
	$(2\lambda - 1)\mathbf{i} + b\lambda\mathbf{j} + (3\lambda - 5)\mathbf{k}$	**A1**		vector from P to a point on the line
	$\sqrt{(2\lambda-1)^2 + (b\lambda)^2 + (3\lambda-5)^2}$	**M1***		finding magnitude of this vector
	$\sqrt{(13+b^2)\lambda^2 - 34\lambda + 26}$	**A1**		expanding and simplifying
	$\sqrt{(13+b^2)\lambda^2 - 34\lambda + 26} = 3$	**M1dep**		setting distances equal
	$(13+b^2)\lambda^2 - 34\lambda + 17 = 0$	**A1**		correct quadratic equation = 0.
	So $(-34)^2 - 4(13+b^2)(17) = 0$	**M1**		setting discriminant equal to 0
	$\Rightarrow b = 2$	**A1**		
	Alternative method 3			
	Distance from point to plane = $\frac{\lvert 2\times 4+1\times 1+0\times 2\rvert}{\sqrt{2^2+1^2+2^2}}$	**M1***		
	= 3 units	**A1**		
	Line is $\mathbf{r} = 3\mathbf{i} + \mathbf{j} - 5\mathbf{k} + \lambda(2\mathbf{i} + b\mathbf{j} + 3\mathbf{k})$	**M1**		
	$\overrightarrow{AP} = \mathbf{i} + 5\mathbf{k}$	**A1**		or $-\overrightarrow{AP}$. Could be seen as part of distance calculation.
	$\begin{pmatrix}1\\0\\5\end{pmatrix}\cdot\begin{pmatrix}2\\b\\3\end{pmatrix} = \left\lvert\begin{pmatrix}1\\0\\5\end{pmatrix}\right\rvert\left\lvert\begin{pmatrix}2\\b\\3\end{pmatrix}\right\rvert\cos\theta$	**M1**		scalar product formula with $\overrightarrow{AP}\cdot\boldsymbol{d}$ to find a value for $\cos\theta$
	$1\times 2 + 5\times 3 = \sqrt{1^2+5^2}\sqrt{2^2+b^2+3^2}\cos\theta$	**M1**		evaluating scalar product and magnitudes
	$\cos\theta = \frac{17}{\sqrt{26}\sqrt{13+b^2}}$	**A1**		expression for $\cos\theta$
	$\sqrt{26}\cos\theta = \frac{17}{\sqrt{13+b^2}}$	**M1***		expression for the distance from (3, 1, -5) to the foot of the perpendicular to the line
	$26 - \left(\frac{17}{\sqrt{13+b^2}}\right)^2 = 3^2$	**M1dep**		using their value correctly with Pythagoras oe to lead to a value for b
	$\Rightarrow b = 2$	**A1**		
		[10]		

Question			Answer	Marks	AO	Guidance
17	(a)	(i)	$\frac{d^2x}{dt^2} = k\frac{dx}{dt} - a\frac{dy}{dt}$	M1*	3.1a	differentiate $\frac{dx}{dt}$ wrt t
			$= k\frac{dx}{dt} - a(ky - bx)$	M1dep	1.1	substitution for $\frac{dy}{dt}$
			$= k\frac{dx}{dt} + abx - k\left(kx - \frac{dx}{dt}\right)$	M1dep	3.1a	substitution for y
			$\frac{d^2x}{dt^2} - 2k\frac{dx}{dt} + (k^2 - n^2)x = 0$	A1	2.1	correct differential equation = 0. Could see ab instead of n^2.
			AE $m^2 - 2km + (k^2 - n^2) = 0 \Rightarrow m = k \pm n$	M1	2.1	giving and solving their AE
			Hence GS is $x = Ae^{(k+n)t} + Be^{(k-n)t}$	A1	2.3	**AG** www
			Alternative method			
			$y = \frac{k}{a}x - \frac{1}{a}\frac{dx}{dt} \Rightarrow \frac{dy}{dt} = \frac{k}{a}\frac{dx}{dt} - \frac{1}{a}\frac{d^2x}{dt^2}$	M1*		differentiate y wrt t
			$\frac{k}{a}\frac{dx}{dt} - \frac{1}{a}\frac{d^2x}{dt^2} = ky - bx$	M1dep		substitution for $\frac{dy}{dt}$
			$\frac{k}{a}\frac{dx}{dt} - \frac{1}{a}\frac{d^2x}{dt^2} = k\left(\frac{k}{a}x - \frac{1}{a}\frac{dx}{dt}\right) - bx$	M1dep		substitution for y
			$\frac{d^2x}{dt^2} - 2k\frac{dx}{dt} + (k^2 - n^2)x = 0$	A1		correct differential equation = 0. Could see ab instead of n^2.
			AE $m^2 - 2km + (k^2 - n^2) = 0 \Rightarrow m = k \pm n$	M1		giving and solving their AE
			Hence GS is $x = Ae^{(k+n)t} + Be^{(k-n)t}$	A1		**AG** www
				[6]		
17	(a)	(ii)	$\frac{dx}{dt} = A(k+n)e^{(k+n)t} + B(k-n)e^{(k-n)t}$	M1	2.1	differentiation of x must be seen
			$y = \frac{n}{a}\left(-Ae^{(k+n)t} + Be^{(k-n)t}\right)$	A1	2.2a	may not be factorised but must be simplified
				[2]		

Question			Answer	Marks	AO	Guidance
17	(b)	(i)	$n = \sqrt{0.004} = 0.02 \Rightarrow k + n = 0.035$ and $k - n = -0.005$	M1	1.1	all three values established
			$x_0 = A + B, \quad y_0 = -\frac{1}{2}(A - B)$ $\Rightarrow A = \frac{1}{2}(x_0 - 2y_0), \quad B = \frac{1}{2}(x_0 + 2y_0)$	M1	3.3	a method to find both A and B (ft their y) from expressions for x_0 and y_0
			$x = \frac{1}{2}(x_0 - 2y_0)\mathrm{e}^{0.035t} + \frac{1}{2}(x_0 + 2y_0)\mathrm{e}^{-0.005t}$	A1	2.2a	**AG** dependent upon both M1s
			Alternative method			
			$n = \sqrt{0.004} = 0.02 \Rightarrow k + n = 0.035, k - n = -0.005$	M1		all three values established
			$\frac{\mathrm{d}x}{\mathrm{d}t} = 0.015x_0 - 0.04y_0, \frac{\mathrm{d}x}{\mathrm{d}t} = 0.035A - 0.005B$ $\Rightarrow A = \frac{1}{2}(x_0 - 2y_0), \quad B = \frac{1}{2}(x_0 + 2y_0)$	M1		a method to find both A and B from two expressions for $\frac{\mathrm{d}x}{\mathrm{d}t}$
			$x = \frac{1}{2}(x_0 - 2y_0)\mathrm{e}^{0.035t} + \frac{1}{2}(x_0 + 2y_0)\mathrm{e}^{-0.005t}$	A1 [3]		**AG** dependent upon both M1s
17	(b)	(ii)	$y = \frac{1}{2}\left(-\frac{1}{2}(x_0 - 2y_0)\mathrm{e}^{0.035t} + \frac{1}{2}(x_0 + 2y_0)\mathrm{e}^{-0.005t}\right)$ $= \frac{1}{4}(x_0 + 2y_0)\mathrm{e}^{-0.005t} - \frac{1}{4}(x_0 - 2y_0)\mathrm{e}^{0.035t}$	B1 [1]	2.2a	**AG** first step or equivalent substitution must be seen
17	(c)	(i)	$x = -50\mathrm{e}^{0.875} + 550\mathrm{e}^{-0.125}$, $y = 275\mathrm{e}^{-0.125} + 25\mathrm{e}^{0.875}$	M1	1.1	for either may be implied by awrt 365 or 303
			$x = 365, y = 302$	A1 [2]	2.2b	for both correct allow $y = 303$

Question			Answer	Marks	AO	Guidance
17	(c)	(ii)	**DR** $-50e^{0.035t} + 550e^{-0.005t} = 275e^{-0.005t} + 25e^{0.035t}$ $275e^{-0.005t} = 75e^{0.035t}$ $0.04t = \ln\left(\frac{11}{3}\right)$ $t = 32.5$, so numbers equal after about 32 or 33 years	**M1** **M1** **M1** **A1** **[4]**	**3.1b** **2.1** **3.1a** **2.2a**	equating $\boldsymbol{x}$ and $\boldsymbol{y}$ with $\boldsymbol{x_0}$, $\boldsymbol{y_0}$ substituted collecting like terms oe. Taking logs for a single term in $\boldsymbol{t}$.
17	(c)	(iii)	x does become zero, as $550e^{-0.005t} \to 0$ as t increases, and $-50e^{0.035t}$ is always negative y is the sum of two positive terms, so is never zero	**M1** **A1** **B1** **[3]**	**3.4** **3.4** **3.5a**	M1 for correct conclusion with some explanation A1 for complete explanation (e.g. $x = 0$ at $t = 59.94...$) reason must be given, e.g. $y = 0$ when $t = 25\ln(-11)$ which is undefined or $e^{0.04t} = -11$ has no solution. Implied by M1A1 without further working seen unless incorrect conclusion for y.
17	(d)	(i)	$x_0 = 2y_0$	**B1** **[1]**	**3.5b**	oe. Subscripts must be seen.
17	(d)	(ii)	$x = Ce^{-0.005t}$, $y = \frac{1}{2}Ce^{-0.005t}$ so both population numbers tend to zero	**M1** **A1** **[2]**	**3.3** **2.4**	oe; e.g. C is $\frac{1}{2}(\boldsymbol{x_0} + \boldsymbol{2y_0})$ or $\boldsymbol{2y_0}$ or $\boldsymbol{x_0}$ oe, e.g. both species disappear. Must be supported by explanation.

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