

Please check the examination details below before entering your candidate information

Candidate surname		Other names	
Centre Number		Candidate Number	

Pearson Edexcel International Advanced Level

Time 1 hour 30 minutes

Paper reference **WMA13/01**

Mathematics
International Advanced Level
Pure Mathematics P3

You must have:
 Mathematical Formulae and Statistical Tables (Yellow), calculator

Total Marks

Candidates may use any calculator allowed by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear.
Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 10 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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1. The functions f and g are defined by

$$f(x) = 9 - x^2 \quad x \in \mathbb{R} \quad x \geq 0$$

$$g(x) = \frac{3}{2x+1} \quad x \in \mathbb{R} \quad x \geq 0$$

(a) Write down the range of f

(1)

(b) Find the value of $fg(1.5)$

(2)

(c) Find g^{-1}

(3)



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Question 1 continued

Lined area for writing the answer to Question 1.

(Total for Question 1 is 6 marks)



2.

$$f(x) = \cos x + 2 \sin x$$

(a) Express $f(x)$ in the form $R \cos(x - \alpha)$, where R and α are constants,

$$R > 0 \text{ and } 0 < \alpha < \frac{\pi}{2}$$

Give the exact value of R and give the value of α , in radians, to 3 decimal places.

(3)

$$g(x) = 3 - 7f(2x)$$

(b) Using the answer to part (a),

(i) write down the exact maximum value of $g(x)$,

(ii) find the smallest positive value of x for which this maximum value occurs, giving your answer to 2 decimal places.

(3)



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Question 2 continued

Lined area for writing the answer to Question 2.

(Total for Question 2 is 6 marks)

3.

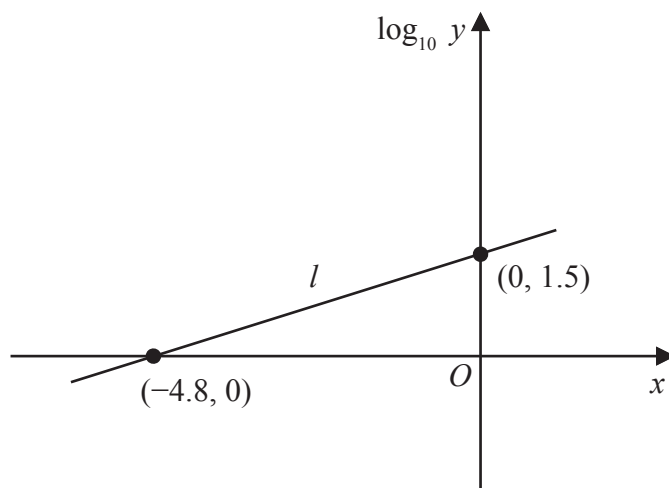


Figure 1

The line l in Figure 1 shows a linear relationship between $\log_{10} y$ and x .

The line passes through the points $(0, 1.5)$ and $(-4.8, 0)$ as shown.

- (a) Write down an equation for l . (2)
- (b) Hence, or otherwise, express y in the form kb^x , giving the values of the constants k and b to 3 significant figures. (3)



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Question 3 continued

Lined area for writing the answer to Question 3.

(Total for Question 3 is 5 marks)



4.

$$f(x) = \frac{2x^4 + 15x^3 + 35x^2 + 21x - 4}{(x+3)^2} \quad x \in \mathbb{R} \quad x > -3$$

(a) Find the values of the constants A , B , C and D such that

$$f(x) = Ax^2 + Bx + C + \frac{D}{(x+3)^2} \quad (4)$$

(b) Hence find,

$$\int f(x) dx \quad (3)$$



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Question 4 continued

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Question 4 continued

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Question 4 continued

Lined area for writing answers.

(Total for Question 4 is 7 marks)



5.

In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

(a) Prove that

$$\cot^2 x - \tan^2 x \equiv 4 \cot 2x \operatorname{cosec} 2x \quad x \neq \frac{n\pi}{2} \quad n \in \mathbb{Z} \quad (4)$$

(b) Hence solve, for $-\frac{\pi}{2} < \theta < \frac{\pi}{2}$

$$4 \cot 2\theta \operatorname{cosec} 2\theta = 2 \tan^2 \theta$$

giving your answers to 2 decimal places.

(5)



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Question 5 continued

Lined area for writing the answer to Question 5.



Question 5 continued

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Question 5 continued

Lined area for writing the answer to Question 5.

(Total for Question 5 is 9 marks)



6.

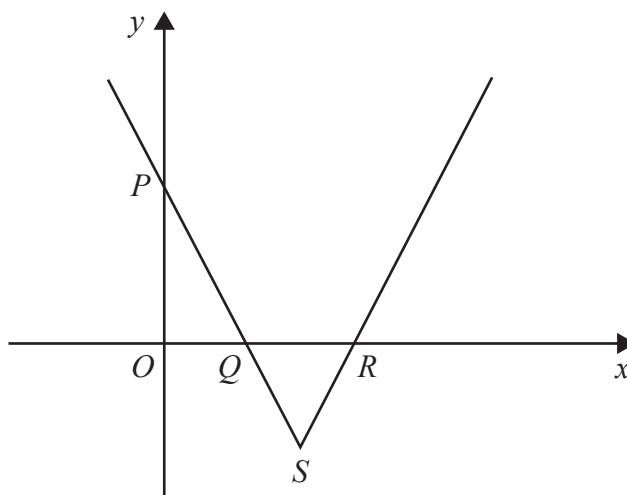


Figure 2

Figure 2 shows a sketch of the graph with equation

$$y = |3x - 5a| - 2a$$

where a is a positive constant.

The graph

- cuts the y -axis at the point P
- cuts the x -axis at the points Q and R
- has a minimum point at S

(a) Find, in simplest form in terms of a , the coordinates of

- point P
- points Q and R
- point S

(4)

(b) Find, in simplest form in terms of a , the values of x for which

$$|3x - 5a| - 2a = |x - 2a|$$

(4)



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Question 6 continued

Lined area for writing the answer to Question 6.



Question 6 continued

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Question 6 continued

Lined area for writing the answer to Question 6.

(Total for Question 6 is 8 marks)



7. The curve C has equation

$$x = 3 \tan \left(y - \frac{\pi}{6} \right) \quad x \in \mathbb{R} \quad -\frac{\pi}{3} < y < \frac{2\pi}{3}$$

(a) Show that

$$\frac{dy}{dx} = \frac{a}{x^2 + b}$$

where a and b are integers to be found.

(4)

The point P with y coordinate $\frac{\pi}{3}$ lies on C .

Given that the tangent to C at P crosses the x -axis at the point Q .

(b) find, in simplest form, the exact x coordinate of Q .

(5)



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Question 7 continued

Lined area for writing the answer to Question 7.



Question 7 continued

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Question 7 continued

Lined area for writing the answer to Question 7.

(Total for Question 7 is 9 marks)



8. Find, in simplest form,

$$\int (2 \cos x - \sin x)^2 dx$$

(5)

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Question 8 continued

Lined area for writing the answer to Question 8.

(Total for Question 8 is 5 marks)



9.

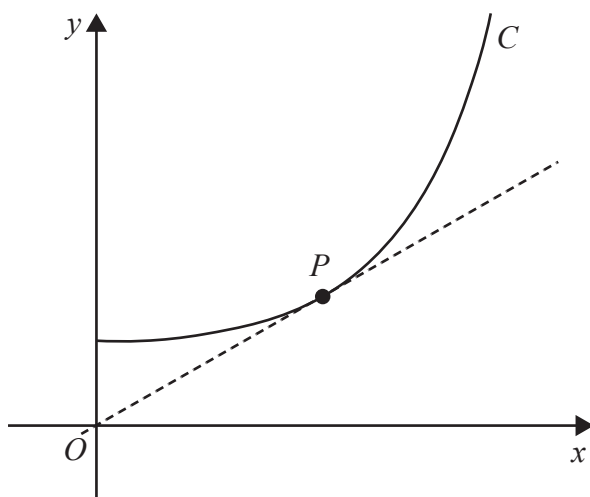


Figure 3

Figure 3 shows a sketch of part of the curve C with equation

$$y = \sqrt{3 + 4e^{x^2}} \quad x \geq 0$$

- (a) Find $\frac{dy}{dx}$, giving your answer in simplest form. (2)

The point P with x coordinate α lies on C .

Given that the tangent to C at P passes through the origin, as shown in Figure 3,

- (b) show that $x = \alpha$ is a solution of the equation (2)
- $$4x^2e^{x^2} - 4e^{x^2} - 3 = 0$$

- (c) Hence show that α lies between 1 and 2 (2)

- (d) Show that the equation in part (b) can be written in the form

$$x = \frac{1}{2}\sqrt{4 + 3e^{-x^2}} \quad (1)$$

The iteration formula

$$x_{n+1} = \frac{1}{2}\sqrt{4 + 3e^{-x_n^2}}$$

with $x_1 = 1$ is used to find an approximation for α .

- (e) Use the iteration formula to find, to 4 decimal places, the value of

(i) x_3

(ii) α

(3)



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Question 9 continued

Lined area for writing the answer to Question 9.



Question 9 continued

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Question 9 continued

Lined area for writing answers.

(Total for Question 9 is 11 marks)



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Question 10 continued

Lined area for writing the answer to Question 10.



Question 10 continued

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(Total for Question 10 is 9 marks)

TOTAL FOR PAPER IS 75 MARKS

