Please check the examination details below before entering your candidate information

Candidate surname	Other names
StemUp Model Solution	

Pearson Edexcel Level 3 GCE

Centre Number	Candidate Number

Monday 18 May 2020

Afternoon (Time: 1 hour 45 minutes)	Paper Reference **9PH0/01**

Physics

Advanced

Paper 1: Advanced Physics I

You must have:
Scientific calculator, ruler, protractor.

Total Marks

Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Answer the questions in the spaces provided
  – *there may be more space than you need.*

Information

- The total mark for this paper is 90.
- The marks for **each** question are shown in brackets
  – *use this as a guide as to how much time to spend on each question.*
- You may use a scientific calculator.
- In questions marked with an **asterisk** (*), marks will be awarded for your ability to structure your answer logically, showing how the points that you make are related or follow on from each other where appropriate.
- The list of data, formulae and relationships is printed at the end of this booklet.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- You are advised to show your working in calculations including units where appropriate.

Turn over ▶

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Answer All questions.

All multiple choice questions must be answered with a cross ☒ in the box for the correct answer from A to D. If you change your mind about an answer, put a line through the box ☒ and then mark your new answer with a cross ☒.

1 Which of the following is an example of a scalar quantity?

☐ **A** displacement

☒ **B** energy

☐ **C** momentum

☐ **D** velocity

(Total for Question 1 = 1 mark)

2 Which row of the table summarises the mass and charge of an antineutron?

	Mass / u	Charge / e
☐ **A**	0	0
☐ **B**	0	−1
☒ **C**	1	0
☐ **D**	1	+1

(Total for Question 2 = 1 mark)

3 The distance between a proton and an electron is r. The electrostatic force is F.

The distance between the proton and electron is doubled.

Which of the following is equal to the electrostatic force at this separation?

☐ **A** $2F$

☐ **B** $\frac{F}{2}$

☐ **C** $\frac{F}{3}$

☒ **D** $\frac{F}{4}$

(Total for Question 3 = 1 mark)

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4 Which of the following is a base SI unit?

- ☒ **A** ampere
- ☐ **B** coulomb
- ☐ **C** joule
- ☐ **D** newton

(Total for Question 4 = 1 mark)

5 A high-energy proton can interact with a photon to produce two particles.

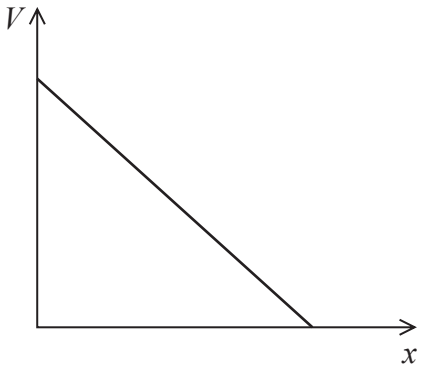
Which of the following could be the two particles produced?

- ☐ **A** $n + \pi^0$
- ☒ **B** $n + \pi^+$
- ☐ **C** $\pi^0 + \pi^+$
- ☐ **D** $\pi^- + \pi^+$

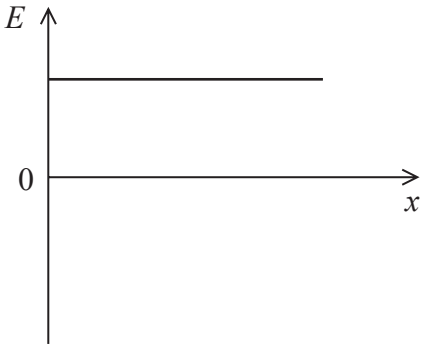
(Total for Question 5 = 1 mark)

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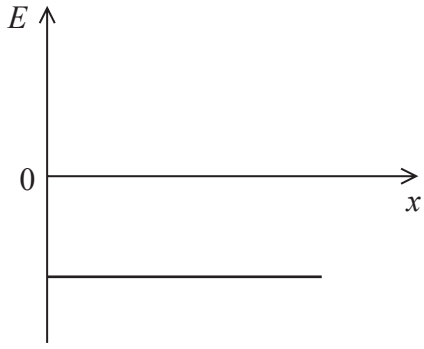
6 The graph shows how an electric potential V varies with distance x.



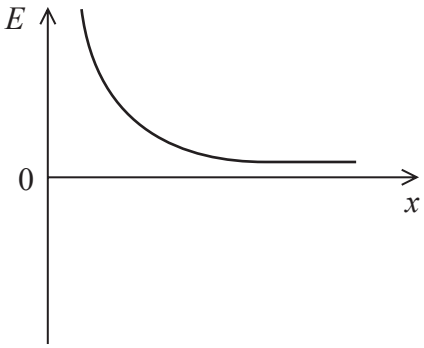
Which of the following shows the corresponding variation of electric field strength E with x?



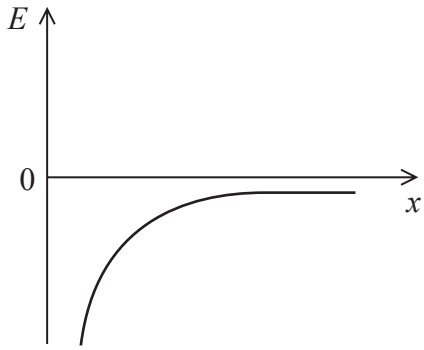
☒ **A**



☒ **B**



☒ **C**



☒ **D**

(Total for Question 6 = 1 mark)

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7 The intensity of light incident on a light dependent resistor (LDR) can vary both its electrical resistance R and the number of charge carriers per unit volume n. The light intensity on an LDR is increased.

Which row of the table describes the effect on R and n?

	R	n
☒ **A**	decreases	decreases
☒ **B**	decreases	increases
☒ **C**	increases	decreases
☒ **D**	increases	increases

(Total for Question 7 = 1 mark)

8 A proton has a mass of 1.67×10^{-27} kg.

Which of the following shows the conversion of this mass to GeV/c^2 ?

☒ **A** $\dfrac{1.67 \times 10^{-27} \times 1.60 \times 10^{-10}}{(3.00 \times 10^{8})^2}$

☒ **B** $\dfrac{1.67 \times 10^{-27} \times 1.60 \times 10^{-19}}{(3.00 \times 10^{8})^2}$

☒ **C** $\dfrac{1.67 \times 10^{-27} \times (3.00 \times 10^{8})^2}{1.60 \times 10^{-10}}$

☒ **D** $\dfrac{1.67 \times 10^{-27}}{1.60 \times 10^{-10} \times (3.00 \times 10^{8})^2}$

(Total for Question 8 = 1 mark)

9 The blade of a lawnmower rotates at a speed of 50 revolutions per second.

Which of the following is the angular speed of the blade in rads s^{-1}?

☒ **A** 7.96

☒ **B** 15.9

☒ **C** 157

☒ **D** 314

(Total for Question 9 = 1 mark)

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10 Two gliders, X and Y, are placed on an air track. The gliders are pushed towards each other as shown.



mass of X = 0.5 kg mass of Y = 1.0 kg

The gliders collide and continue to move after the collision.

Which row of the table could show the velocities of X and Y, in $m\,s^{-1}$, after the collision?

	X	Y
☒ **A**	−1.0	0.5
☐ **B**	−1.0	−0.5
☐ **C**	−2.0	−1.0
☐ **D**	−2.0	2.0

(Total for Question 10 = 1 mark)

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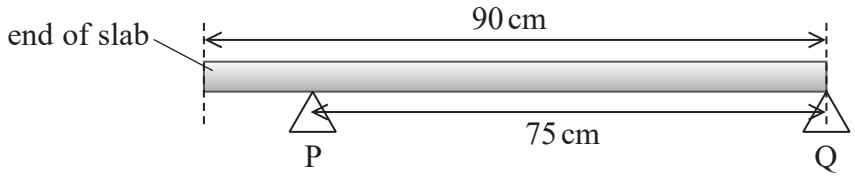
11 A uniform paving slab is to be used as a garden step.

(a) State what is meant by the centre of gravity of an extended body.

(1)

The centre of gravity is the point through which the (whole) weight of the body acts.

(b) The paving slab has a weight of 310 N and a length of 90 cm and will be supported at two points, P and Q, as shown. The distance between P and Q will be 75 cm.



This might be unsafe because a person who places all their weight at the end of the slab might tip the slab.

A person of mass 70 kg stands at the end of the slab.

Deduce whether the slab will tip.

(4)

Taking moments about P: the person is 15 cm (0.15 m) from P.

Moment of person = mg × d = 70 kg × 9.81 N kg^{-1} × 0.15 m = 103 N m

The weight of the uniform slab acts at its centre, 45 cm from the end, so 30 cm from P.

Moment of slab = 310 N × 0.30 m = 93 N m

The moment of the person's weight (103 N m) is larger than the moment of the weight of the slab (93 N m), so the slab will tip.

(Total for Question 11 = 5 marks)

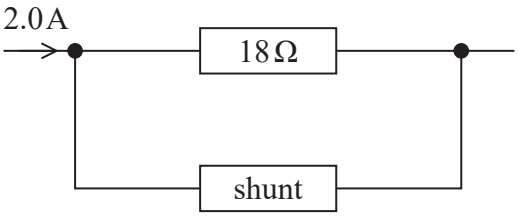
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12 Analogue ammeters were used before digital meters became widely available.
The analogue ammeter shown will measure a maximum current of 1.0 mA and has a resistance of 18 Ω.



(Source: © David J. Green/Alamy Stock Photo)

The analogue ammeter can be adapted to measure a larger current by adding a resistor, known as a shunt, in parallel with the ammeter. The arrangement is shown below.
The analogue ammeter is represented by the 18 Ω resistor.



The maximum current through the 18 Ω resistor remains as 1.0 mA.

(a) Show that the shunt would need to have a resistance of about 0.01 Ω to adapt this ammeter to read up to a maximum current of 2.0 A.

(3)

p.d. across the ammeter: $V = IR = 1.0 \times 10^{-3}\ A \times 18\ \Omega = 0.018\ V$

This is also the p.d. across the shunt (in parallel).

Current through the shunt = $2.0\ A - 0.001\ A = 1.999\ A$

$R = V/I = 0.018\ V \div 1.999\ A = 9.0 \times 10^{-3}\ \Omega \approx 0.01\ \Omega$

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(b) A shunt of this resistance was usually made from Manganin wire.

Calculate the length of Manganin wire of radius 0.95 mm required to make this shunt.

resistivity of Manganin = $4.55 \times 10^{-7}\ \Omega\,m$

(3)

$A = \pi r^2 = \pi \times (0.95 \times 10^{-3}\ m)^2 = 2.84 \times 10^{-6}\ m^2$

$R = \rho l / A$ so $l = RA/\rho$

$l = (9.0 \times 10^{-3}\ \Omega \times 2.84 \times 10^{-6}\ m^2) \div 4.55 \times 10^{-7}\ \Omega\ m$

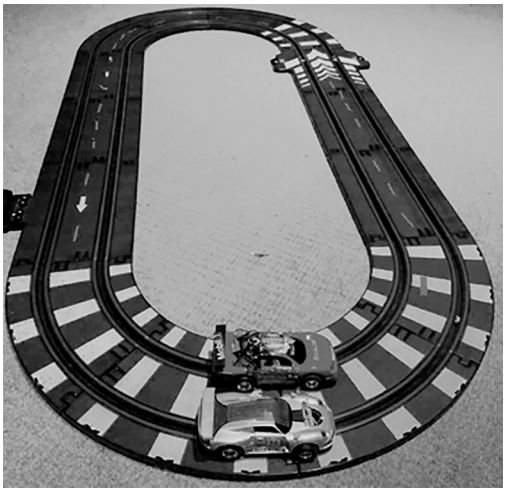
$l = 0.056\ m$

Length = $0.056\ m$

(Total for Question 12 = 6 marks)

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13 The photograph shows a model racing car set. The curved parts of the track are semicircular. The car makes electrical contact with the track using metal brushes underneath the car.



(a) There is a maximum speed for the car to stay on the curved part of the track. Explain why the car will slip off the curved part of the track if the car exceeds the maximum speed.

(3)

To move in a circle a resultant force is required, acting towards the centre of the circle (centripetal force $F = mv^2/r$).

This force is provided by friction between the car (brushes) and the track.

As v increases the force required increases, until it exceeds the maximum friction, so the car slides off the track.

(b) The following measurements are made for a car starting at rest on a straight piece of track.

distance travelled = 1.2 m

time taken = 0.77 s

(i) Show that the final velocity of the car is about 3 m s^{-1}.

Assume the acceleration is constant.

(2)

$s = (u + v)t/2$ so $1.2\ m = (0 + v)/2 \times 0.77\ s$

$v = 2 \times 1.2\ m \div 0.77\ s = 3.1\ m\ s^{-1}$ (about $3\ m\ s^{-1}$)

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(ii) The final velocity calculated in (b)(i) is the maximum velocity before the car slips off the track.

Calculate the maximum horizontal force between the curved part of the track and the car.

mass of car = 0.050 kg

radius of curved part of track = 0.042 m

(2)

$F = mv^2/r = 0.050\ kg \times (3.1\ m\ s^{-1})^2 \div 0.042\ m$

$F = 11.4\ N$

Maximum horizontal force = 11 N

(c) The cars are controlled separately and so can be raced, with one car on the inner lane and the other on the outer lane. The cars are identical. Each car is raced at its highest speed for that lane.

Explain why the outcome of the race is difficult to predict.

(3)

The car on the inner lane covers a smaller distance around the track.

But the inner lane has a smaller radius of curvature, and the maximum horizontal (friction) force is the same for both identical cars,

so from $v = \sqrt{(Fr/m)}$ the maximum speed is greater for the car on the outer lane. So the outcome is unclear.

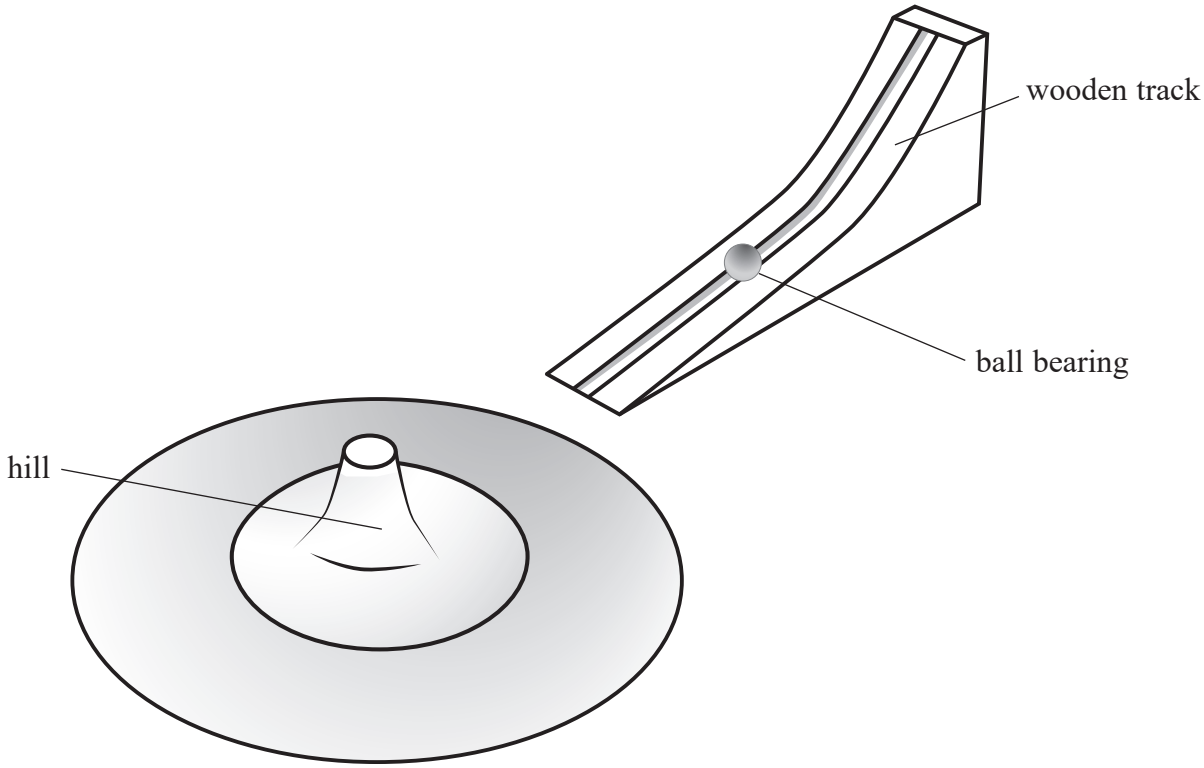
(Total for Question 13 = 10 marks)

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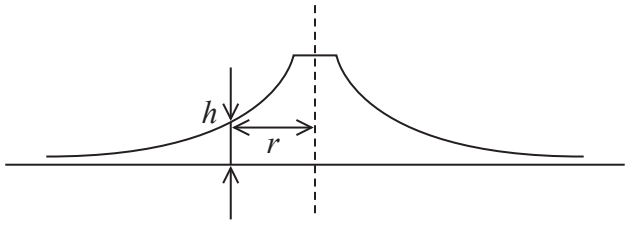
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14 The diagram shows a model used to demonstrate alpha particle scattering. A ball bearing is set rolling on a wooden track. The track is positioned so that the ball bearing rolls onto a metal sheet with a curved surface known as a 'hill'.



The diagram shows a vertical cross-section through the hill. The surface is curved so that the height of a point h on the curved surface is inversely proportional to the distance r from the centre of the hill.



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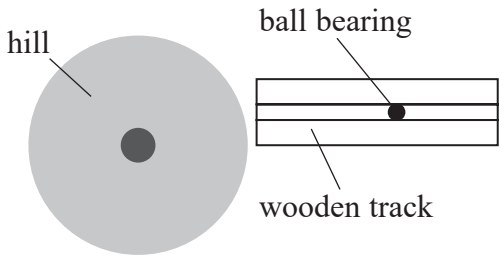
(a) Explain why the hill is suitable as a model for the electric field surrounding the nucleus of an atom.

(3)

The curved surface is (analogous to) a radial field, centred on the centre of the hill, like the field around a nucleus.

As $h \propto 1/r$, the gravitational potential (energy) of the ball bearing on the hill $\propto 1/r$, which compares with $V \propto 1/r$ around a point charge (the nucleus), so the ball is repelled like the positive alpha particle.

(b) A plan view of the arrangement is shown.



The wooden track is moved to different positions and the ball bearing is released.

Describe the results of the alpha particle scattering experiment and how these can be demonstrated by moving the wooden track to different positions.

(4)

Most alpha particles passed straight through undeflected: shown by aiming the ball bearing so that it misses (or just touches) the edge of the hill.

Some alpha particles were deflected through small angles: shown by aiming the ball bearing close to (but not along) the centre line of the hill.

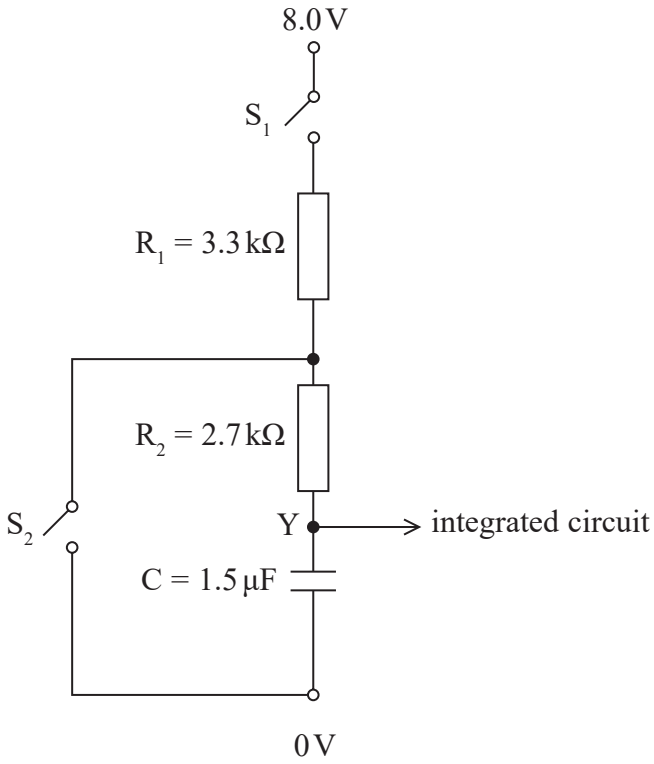
A few alpha particles were deflected through large angles (more than 90°) or reflected straight back: shown by aiming the ball bearing directly at the centre of the hill.

(Total for Question 14 = 7 marks)

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15 The properties of capacitors make them useful in timing circuits.

The following circuit is used to provide an input Y to an integrated circuit.



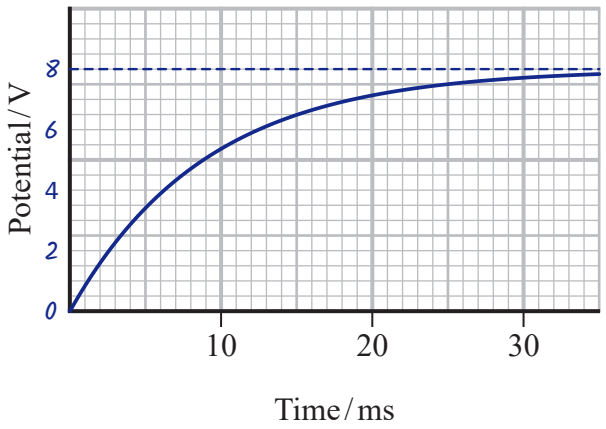
(a) Initially the capacitor is uncharged. The switch S_1 is closed.

Sketch a graph to show how the potential at point Y varies with time.

(3)

Time constant = RC = (3.3 + 2.7) × 10^3 Ω × 1.5 × 10^{-6} F = 9.0 ms

At t = 9 ms, V = 0.63 × 8.0 V = 5.1 V; rises towards a maximum of 8.0 V.



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(b) When the potential at Y is 8.0 V, the switch S_2 is closed.

(i) Calculate the time taken for the potential at Y to decrease to 2.0 V.

(3)

Capacitor discharges through R_2 only: $RC = 2700\ \Omega \times 1.5 \times 10^{-6}\ F = 4.05 \times 10^{-3}\ s$

$V = V_0 e^{-t/RC}$ so $\ln(V_0/V) = t/RC$: $\ln(8.0/2.0) = \ln 4 = t/4.05\ ms$

$t = 4.05\ ms \times \ln 4 = 5.6\ ms$

Time taken = 5.6 ms

(ii) Calculate the energy stored on the capacitor when the potential at Y is 2.0 V.

(2)

$W = \frac{1}{2}CV^2 = \frac{1}{2} \times 1.5 \times 10^{-6}\ F \times (2.0\ V)^2$

$W = 3.0 \times 10^{-6}\ J$

Energy stored = 3.0×10^{-6} J

(c) When the potential at Y is 2.0 V, the switch S_2 is opened.

Calculate the power dissipated by the resistance R_1 when the potential at Y is 2.0 V.

(3)

p.d. across R_1 and R_2 together = 8.0 V − 2.0 V = 6.0 V

$I = V/R = 6.0\ V \div (3.3 + 2.7) \times 10^3\ \Omega = 1.0 \times 10^{-3}\ A$

$P = I^2R = (1.0 \times 10^{-3}\ A)^2 \times 3300\ \Omega$

$P = 3.3 \times 10^{-3}\ W$

Power dissipated = 3.3×10^{-3} W

(Total for Question 15 = 11 marks)

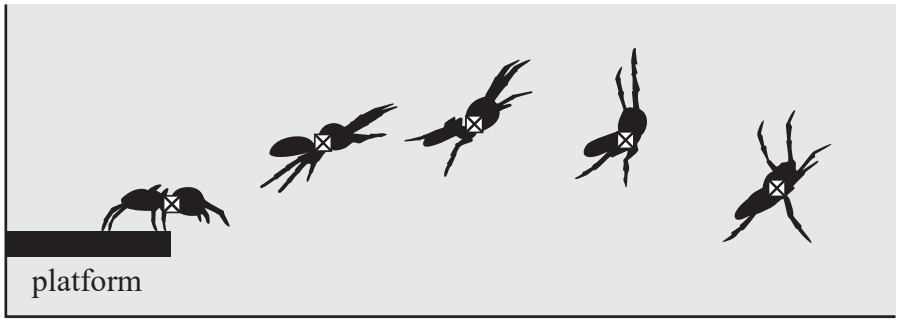
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16 Scientists have been studying a type of jumping spider that can jump up to six times its body length.

(a) The scientists photographed a spider at 0.02s intervals, during a jump. The picture is taken from the photograph and is shown actual size.



(i) Deduce whether the images show that the motion in the *x*-direction is independent of the motion in the *y*-direction. You should take measurements using the cross marking the centre of gravity of the spider.

(4)

Horizontal distance between successive images = 2.0 cm each time (0.02 s apart).

The distances between images are the same in the x direction, so the horizontal velocity is constant.

Vertical distances between successive images: 0.8 cm up, 0.25 cm up, 0.2 cm down, 0.65 cm down, so they vary: the vertical velocity is changing.

The velocity in the x direction is constant while the y velocity changes, so the x motion is independent of the y motion.

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(ii) Show that the initial velocity of the spider at the start of the jump is about 1 m s^{-1}. You should take measurements using the cross marking the centre of gravity of the spider.

(5)

Maximum height of the cross above its starting position = 1.1 cm = 0.011 m

Vertical: $v^2 = u^2 + 2as$ with $v = 0$ at the top:

$0 = u_V^2 - 2 \times 9.81\ m\ s^{-2} \times 0.011\ m$, so $u_V = 0.46\ m\ s^{-1}$

Horizontal: 4 intervals = 0.08 s, horizontal distance = 8.0 cm = 0.08 m

$v_H = d/t = 0.08\ m \div 0.08\ s = 1.0\ m\ s^{-1}$

Resultant initial velocity $v = \sqrt{(u_V^2 + v_H^2)} = \sqrt{(0.46^2 + 1.0^2)}$

$v = 1.1\ m\ s^{-1}$ (about 1 m s^{-1})

(iii) The spider achieves this jump by extending its two back legs by 3.0 mm.

Calculate the average force the spider exerts in each leg to achieve the jump.

mass of spider = 150 mg

(3)

Work done by both legs = kinetic energy gained: $2 \times F \times \Delta s = \frac{1}{2}mv^2$

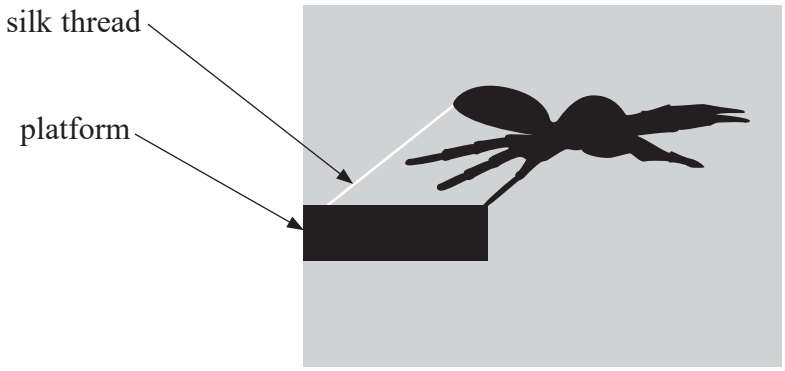
$2 \times F \times 0.0030\ m = \frac{1}{2} \times 150 \times 10^{-6}\ kg \times (1.1\ m\ s^{-1})^2$

$F = 9.1 \times 10^{-5}\ J \div 0.0060\ m = 0.015\ N$

Average force = 0.015 N

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(b) Just as the spider starts the jump, it fixes a silk thread to the platform. It is thought that the thread acts as a safety line in case the spider falls.



A student makes the comment:

'If the silk thread can withstand a tension equal to the weight of the spider then this safety system should work.'

Deduce whether this statement is correct.

(2)

When the thread stops the falling spider it must decelerate the spider, so the tension = mass of spider × deceleration (ma) plus the weight of the spider ($T = mg + ma$), so the tension needed is greater than the weight: the statement is incorrect.

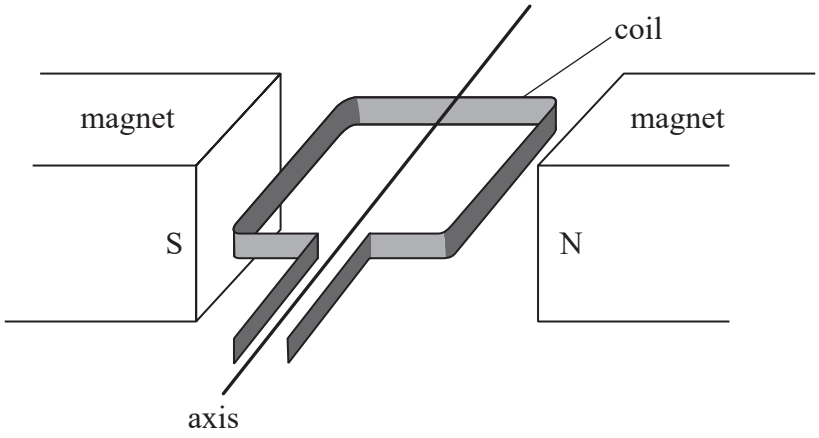
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17 Hybrid electric vehicles (HEV) use the same device both as a generator to charge the car battery and as an electric motor to support the propulsion system. A simplified diagram of the device is shown. The coil can rotate freely around the axis.



*(a) Describe how the device can be used as both a generator and an electric motor.

(6)

Generator: the coil has to be rotated (turned by the wheels/engine) in the magnetic field between the magnets.

As it rotates the sides of the coil cut the magnetic flux, so there is a rate of change of flux linkage with the coil.

By Faraday's law this induces an e.m.f. across the coil, which drives a current to charge the battery.

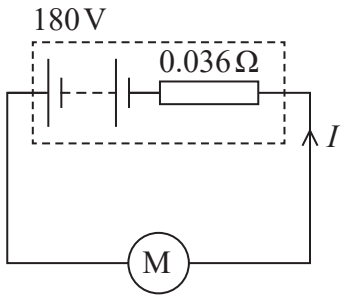
Motor: a current is provided to the coil from the battery.

The sides of the coil that are perpendicular to the magnetic field have a current in them, so there is a force on each side ($F = BIl$), in opposite directions.

These two forces provide a moment (couple) about the axis, so the coil rotates and drives the wheels.

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(b) The circuit diagram shows a car battery connected to an electric motor for a HEV. The battery has an electromotive force (e.m.f.) 180 V and internal resistance 0.036 Ω.



The motor has a maximum power of 88 kW.

(i) Show that the current I drawn by the electric motor when operating at this power would be given by the equation

$$0.036I^2 - 180I + 88\,000 = 0$$

(3)

Power delivered to the motor: $P = IV$

Terminal p.d. $V = \varepsilon - Ir = 180 - 0.036I$

$88\ kW = 88\,000\ W = I \times (180 - 0.036I) = 180I - 0.036I^2$

so $0.036I^2 - 180I + 88\,000 = 0$

(ii) Solving the equation above produces an answer of $I = 550$ A. At maximum power, the car can accelerate from rest to sixty miles per hour in under 7 s.

The maximum charge capacity of the battery within this HEV is 6.1 amp-hour.

Deduce whether the battery could maintain this current for up to 7 s.

(2)

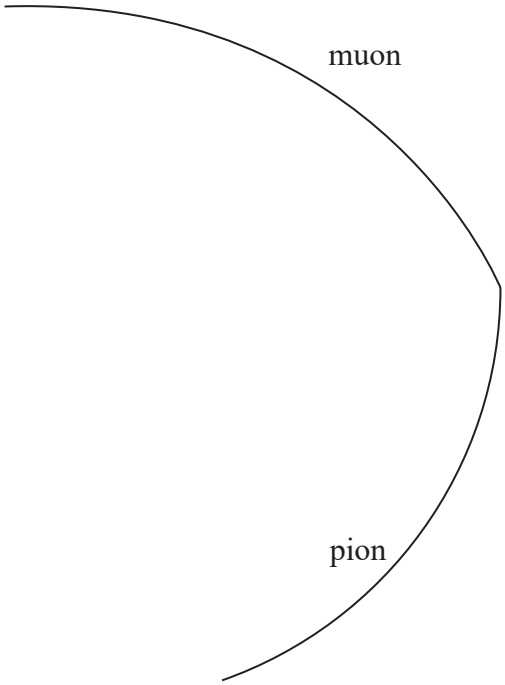
$Q = It$: $6.1\ A\ h = 6.1 \times 3600 = 21\,960\ C$, so $t = 21\,960\ C \div 550\ A = 40\ s$

40 s is more than 7 s, so the battery could maintain this current for 7 s.

(Total for Question 17 = 11 marks)

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18 A negatively charged pion decays into a muon and an antineutrino. The diagram shows tracks in a particle detector formed in such an event.



(a) Deduce whether the antineutrino is charged, giving two reasons for your decision.

(2)

The antineutrino is not charged: it does not leave a track in the detector.

Charge is conserved: before the decay the charge is −1 (pion), after it is −1 (muon) + 0, so the antineutrino has no charge.

(b) Write a particle equation to represent this decay.

(1)

$\pi^- \rightarrow \mu^- + \bar{\nu}_\mu$

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(c) According to the standard model, the pion and muon are classified within two different groups of particles.

State which group each particle belongs to and describe the two groups.

(4)

The muon is a lepton. Leptons are fundamental particles (not made of quarks) and do not feel the strong force.

The pion is a meson (a hadron). Mesons consist of a quark and an antiquark.

(d) The momentum of the pion just before it decays is 9.1×10^{-20} N s.

Determine the magnetic flux density of the magnetic field which acts in the detector and state its direction.

Scale of diagram 1 cm represents 10 cm

pion charge = -1.6×10^{-19} C

(4)

Radius of the pion track measured on the diagram = 5.5 cm, so actual r = 55 cm = 0.55 m

Momentum $p = BQr$, so $B = p/Qr$

$B = 9.1 \times 10^{-20}\ N\ s \div (1.6 \times 10^{-19}\ C \times 0.55\ m)$

$B = 1.0\ T$

Using Fleming's left-hand rule for the negative pion (force towards the centre of the curve):

Magnetic flux density = 1.0 T

Direction of magnetic field = out of the page

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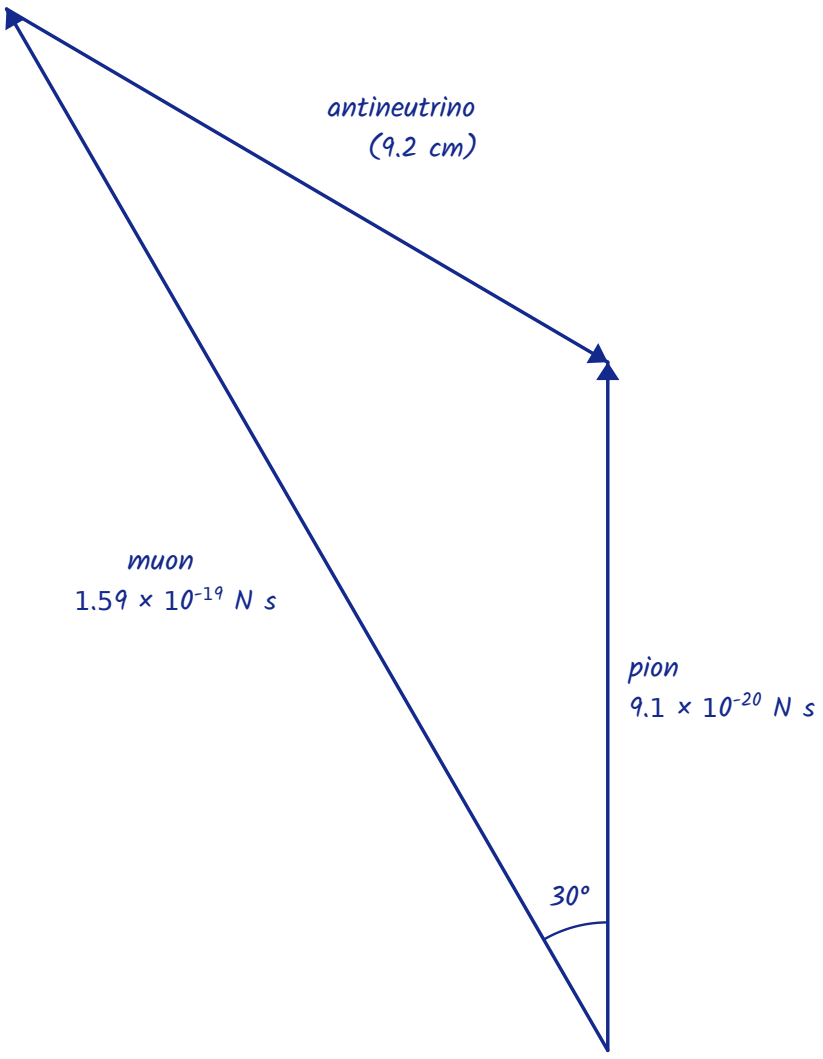
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(e) Use a vector diagram to determine the momentum of the antineutrino.

The initial momentum of the muon is 1.59×10^{-19} N s.

(5)

Scale: 1 cm represents 1.0×10^{-20} N s
momentum of pion = momentum of muon + momentum of antineutrino



Antineutrino vector measures 9.2 cm, so p = 9.2×10^{-20} N s

Momentum of antineutrino = *9.2×10^{-20} N s*

Direction of antineutrino = *150° to the muon (120° to the pion)*

(Total for Question 18 = 16 marks)

TOTAL FOR PAPER = 90 MARKS

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List of data, formulae and relationships

Acceleration of free fall	$g = 9.81 \text{ m s}^{-2}$	(close to Earth's surface)
Boltzmann constant	$k = 1.38 \times 10^{-23} \text{ J K}^{-1}$	
Coulomb law constant	$k = \frac{1}{4\pi\varepsilon_0} = 8.99 \times 10^{9} \text{ N m}^2 \text{ C}^{-2}$	
Electron charge	$e = -1.60 \times 10^{-19} \text{ C}$	
Electron mass	$m_e = 9.11 \times 10^{-31} \text{ kg}$	
Electronvolt	$1 \text{ eV} = 1.60 \times 10^{-19} \text{ J}$	
Gravitational constant	$G = 6.67 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2}$	
Gravitational field strength	$g = 9.81 \text{ N kg}^{-1}$	(close to Earth's surface)
Permittivity of free space	$\varepsilon_0 = 8.85 \times 10^{-12} \text{ F m}^{-1}$	
Planck constant	$h = 6.63 \times 10^{-34} \text{ J s}$	
Proton mass	$m_p = 1.67 \times 10^{-27} \text{ kg}$	
Speed of light in a vacuum	$c = 3.00 \times 10^{8} \text{ m s}^{-1}$	
Stefan-Boltzmann constant	$\sigma = 5.67 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$	
Unified atomic mass unit	$u = 1.66 \times 10^{-27} \text{ kg}$	

Mechanics

Kinematic equations of motion

$$s = \frac{(u + v)t}{2}$$

$$v = u + at$$

$$s = ut + \tfrac{1}{2}at^2$$

$$v^2 = u^2 + 2as$$

Forces

$$\Sigma F = ma$$

$$g = \frac{F}{m}$$

$$W = mg$$

moment of force $= Fx$

Momentum

$$p = mv$$

Work, energy and power

$$\Delta W = F\Delta s$$

$$E_k = \tfrac{1}{2}mv^2$$

$$\Delta E_{grav} = mg\Delta h$$

$$P = \frac{E}{t}$$

$$P = \frac{W}{t}$$

$$\text{efficiency} = \frac{\text{useful energy output}}{\text{total energy input}}$$

$$\text{efficiency} = \frac{\text{useful power output}}{\text{total power input}}$$

Electric circuits

Potential difference

$$V = \frac{W}{Q}$$

Resistance

$$R = \frac{V}{I}$$

Electrical power and energy

$$P = VI$$

$$P = I^2R$$

$$P = \frac{V^2}{R}$$

$$W = VIt$$

Resistivity

$$R = \frac{\rho l}{A}$$

Current

$$I = \frac{\Delta Q}{\Delta t}$$

$$I = nqvA$$

Materials

Density

$$\rho = \frac{m}{V}$$

Stokes' law

$$F = 6\pi\eta rv$$

Hooke's law

$$\Delta F = k\Delta x$$

Young modulus

$$\text{Stress } \sigma = \frac{F}{A}$$

$$\text{Strain } \varepsilon = \frac{\Delta x}{x}$$

$$E = \frac{\sigma}{\varepsilon}$$

Elastic strain energy

$$\Delta E_{\text{el}} = \tfrac{1}{2}F\Delta x$$

Waves and particle nature of light

Wave speed

$$v = f\lambda$$

Speed of a transverse wave on a string

$$v = \sqrt{\frac{T}{\mu}}$$

Intensity of radiation

$$I = \frac{P}{A}$$

Power of a lens

$$P = \frac{1}{f}$$

$$P = P_1 + P_2 + P_3 + \ldots$$

Thin lens equation

$$\frac{1}{u} + \frac{1}{v} = \frac{1}{f}$$

Magnification for a lens

$$m = \frac{\text{image height}}{\text{object height}} = \frac{v}{u}$$

Diffraction grating

$$n\lambda = d \sin\theta$$

Refractive index

$$n_1 \sin\theta_1 = n_2 \sin\theta_2$$

$$n = \frac{c}{v}$$

Critical angle

$$\sin C = \frac{1}{n}$$

Photon model

$$E = hf$$

Einstein's photoelectric equation

$$hf = \phi + \tfrac{1}{2}mv^2_{\text{max}}$$

de Broglie wavelength

$$\lambda = \frac{h}{p}$$

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Further mechanics

Impulse

$$F\Delta t = \Delta p$$

Kinetic energy of a non-relativistic particle

$$E_k = \frac{p^2}{2m}$$

Motion in a circle

$$v = \omega r$$

$$T = \frac{2\pi}{\omega}$$

$$F = ma = \frac{mv^2}{r}$$

$$a = \frac{v^2}{r}$$

$$a = r\omega^2$$

$$F = mr\omega^2$$

Fields

Coulomb's law

$$F = \frac{Q_1 Q_2}{4\pi\varepsilon_0 r^2}$$

Electric field strength

$$E = \frac{F}{Q}$$

$$E = \frac{Q}{4\pi\varepsilon_0 r^2}$$

$$E = \frac{V}{d}$$

Electric potential

$$V = \frac{Q}{4\pi\varepsilon_0 r}$$

Capacitance

$$C = \frac{Q}{V}$$

Energy stored in a capacitor

$$W = \tfrac{1}{2}QV$$

$$W = \tfrac{1}{2}CV^2$$

$$W = \tfrac{1}{2}\frac{Q^2}{C}$$

Capacitor discharge

$$Q = Q_0 e^{-t/RC}$$

$$I = I_0 e^{-t/RC}$$

$$V = V_0 e^{-t/RC}$$

$$\ln Q = \ln Q_0 - \frac{t}{RC}$$

$$\ln I = \ln I_0 - \frac{t}{RC}$$

$$\ln V = \ln V_0 - \frac{t}{RC}$$

In a magnetic field

$$F = BIl \sin\theta$$

$$F = Bqv \sin\theta$$

Faraday's and Lenz's laws

$$\mathscr{E} = \frac{-\mathrm{d}(N\phi)}{\mathrm{d}t}$$

Root-mean-square values

$$V_{rms} = \frac{V_0}{\sqrt{2}}$$

$$I_{rms} = \frac{I_0}{\sqrt{2}}$$

Nuclear and particle physics

In a magnetic field

$$r = \frac{p}{BQ}$$

Thermodynamics

Heating

$$\Delta E = mc\Delta\theta$$

$$\Delta E = L\Delta m$$

Molecular kinetic theory

$$\frac{1}{2}m\langle c^2\rangle = \frac{3}{2}kT$$

$$pV = \frac{1}{3}Nm\langle c^2\rangle$$

Ideal gas equation

$$pV = NkT$$

Stefan-Boltzmann law

$$L = \sigma AT^4$$

$$L = 4\pi r^2\sigma T^4$$

Wien's law

$$\lambda_{max}T = 2.898 \times 10^{-3}\ \text{m K}$$

Space

Intensity

$$I = \frac{L}{4\pi d^2}$$

Redshift of electromagnetic radiation

$$z = \frac{\Delta\lambda}{\lambda} \approx \frac{\Delta f}{f} \approx \frac{v}{c}$$

Cosmological expansion

$$v = H_0 d$$

Nuclear radiation

Mass-energy

$$\Delta E = c^2\Delta m$$

Radioactive decay

$$A = \lambda N$$

$$\frac{dN}{dt} = -\lambda N$$

$$\lambda = \frac{\ln 2}{t_{½}}$$

$$N = N_0\, e^{-\lambda t}$$

$$A = A_0\, e^{-\lambda t}$$

Gravitational fields

Gravitational force

$$F = \frac{Gm_1m_2}{r^2}$$

Gravitational field strength

$$g = \frac{Gm}{r^2}$$

Gravitational potential

$$V_{grav} = \frac{-Gm}{r}$$

Oscillations

Simple harmonic motion

$$F = -kx$$

$$a = -\omega^2 x$$

$$x = A\cos\omega t$$

$$v = -A\omega\sin\omega t$$

$$a = -A\omega^2\cos\omega t$$

$$T = \frac{1}{f} = \frac{2\pi}{\omega}$$

$$\omega = 2\pi f$$

Simple harmonic oscillator

$$T = 2\pi\sqrt{\frac{m}{k}}$$

$$T = 2\pi\sqrt{\frac{l}{g}}$$

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