Write your name here

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Pearson Edexcel Level 3 GCE

Centre Number | Candidate Number

Physics

Advanced
Paper 1: Advanced Physics I

Monday 4 June 2018 – Afternoon
Time: 1 hour 45 minutes

Paper Reference
9PH0/01

You must have:
Ruler

Total Marks

Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Answer the questions in the spaces provided
  – *there may be more space than you need.*

Information

- The total mark for this paper is 90.
- The marks for **each** question are shown in brackets
  – *use this as a guide as to how much time to spend on each question.*
- You may use a scientific calculator.
- In questions marked with an **asterisk** (*), marks will be awarded for your ability to structure your answer logically showing how the points that you make are related or follow on from each other where appropriate.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- You are advised to show your working in calculations including units where appropriate.

Turn over ▶

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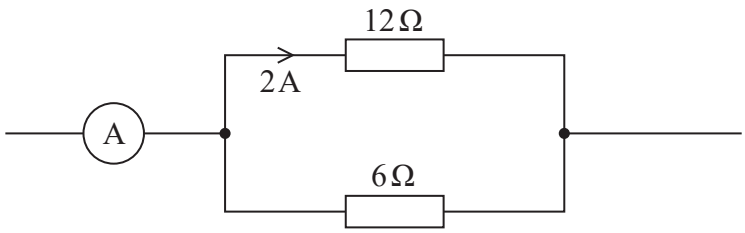
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Answer ALL questions.

All multiple choice questions must be answered with a cross ☒ in the box for the correct answer from A to D. If you change your mind about an answer, put a line through the box ☒ and then mark your new answer with a cross ☒.

1 Part of an electric circuit is shown.



What is the current shown by the ammeter?

☒ **A** 3 A

☒ **B** 4 A

☒ **C** 5 A

☒ **D** 6 A

(Total for Question 1 = 1 mark)

2 A cell is connected across a resistor. After a while the internal resistance of the cell increases.

Which row of the table correctly shows the change in the current in the circuit and the change in the terminal potential difference across the cell?

	Current	Terminal potential difference
☒ **A**	decreases	decreases
☒ **B**	decreases	increases
☒ **C**	increases	decreases
☒ **D**	increases	increases

(Total for Question 2 = 1 mark)

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3 An object is falling at terminal velocity.

Which of the following is **not** a valid conclusion from this statement?

☒ **A** The acceleration of the object is zero.

☒ **B** There is a resistive force acting on the object.

☒ **C** There is a resultant force acting on the object.

☒ **D** The object has weight.

(Total for Question 3 = 1 mark)

4 A light dependent resistor is connected across a cell of negligible internal resistance. The light intensity is increased.

Which of the following statements about the current is correct?

☒ **A** It decreases because there is an increase in the number of conduction electrons.

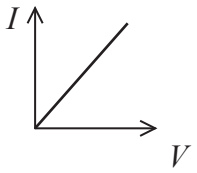
☒ **B** It increases because there is an increase in the number of conduction electrons.

☒ **C** It decreases because the amplitude of lattice vibrations decreases.

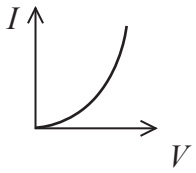
☒ **D** It increases because the amplitude of lattice vibrations increases.

(Total for Question 4 = 1 mark)

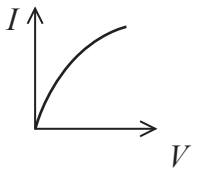
5 Which of the following graphs shows how the current varies with potential difference for a filament lamp?



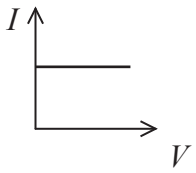
A



B



C



D

☒ **A**

☒ **B**

☒ **C**

☒ **D**

(Total for Question 5 = 1 mark)

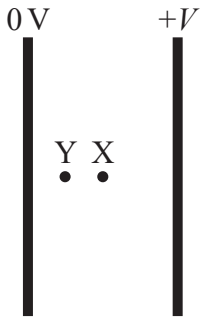
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6 Which of the following are the base units for impulse?

- ☒ **A** $kg\,m\,s^{-1}$
- ☐ **B** $kg\,m\,s^{-2}$
- ☐ **C** $N\,m$
- ☐ **D** $N\,s$

(Total for Question 6 = 1 mark)

7 A potential difference V is applied across two parallel plates. An electron midway between the two plates at point X experiences an electric force F.



The electron moves to point Y which is halfway between point X and the left-hand plate.

Which of the following is the electric force experienced by the electron at Y?

- ☐ **A** $2F$
- ☒ **B** F
- ☐ **C** $\frac{F}{2}$
- ☐ **D** $\frac{F}{4}$

(Total for Question 7 = 1 mark)

8 A wire carries an alternating current of peak value 3 A.

Which of the following is the root-mean-square value of this current?

- ☐ **A** 1.5 A
- ☒ **B** 2.1 A
- ☐ **C** 4.2 A
- ☐ **D** 9.0 A

(Total for Question 8 = 1 mark)

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9 Electric and magnetic fields can be used in particle accelerators.

Which row in the table correctly describes the use of electric and magnetic fields in the particle accelerator indicated?

	Particle accelerator	Magnetic field	Electric field
☐ **A**	cyclotron	not used	used to accelerate particles
☒ **B**	cyclotron	used to accelerate particles	used to accelerate particles
☐ **C**	linac	used to accelerate particles	not used
☐ **D**	linac	used to accelerate particles	used to accelerate particles

(Total for Question 9 = 1 mark)

10 Which of the following particle equations is correct for the decay of a proton within a nucleus?

☐ **A** $p \rightarrow n + \beta^+$

☐ **B** $p \rightarrow p + \beta^+$

☒ **C** $p \rightarrow n + \beta^+ + \nu$

☐ **D** $p \rightarrow p + \beta^+ + \nu$

(Total for Question 10 = 1 mark)

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11 A "metre bridge" is a circuit which can be used to measure an unknown resistance accurately. The metre bridge includes a metre length of nichrome wire.

(a) Calculate the resistance of a 1.00 m length of the nichrome wire.

(3)

resistivity of nichrome = 1.12×10^{-6} Ωm
diameter of wire = 4.00×10^{-4} m

$R = \rho l/A$, with $A = \pi r^2$ and $r = 4.00 \times 10^{-4}\ m \div 2 = 2.00 \times 10^{-4}\ m$

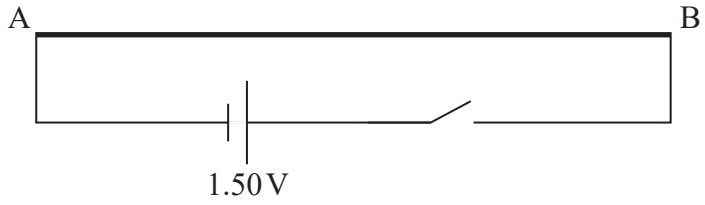
$A = \pi \times (2.00 \times 10^{-4}\ m)^2 = 1.26 \times 10^{-7}\ m^2$

$R = (1.12 \times 10^{-6}\ \Omega\ m \times 1.00\ m) \div 1.26 \times 10^{-7}\ m^2$

$R = 8.9\ \Omega$

Resistance = 8.9 Ω

(b) This metre length of wire, labelled AB, is connected to a 1.50 V cell of negligible internal resistance and a switch as shown.



(i) Explain how the potential along this wire varies with distance from A when the switch is closed.

(2)

The current is the same through the whole length of wire and the resistance increases with length ($R = \rho l/A$), so by $V = IR$ the potential (difference from A) is proportional to the length of wire: it increases uniformly from 0 V at A to 1.50 V at B.

(ii) Show that the potential difference between A and a point 75.0 cm along the wire from A is about 1.1 V.

(2)

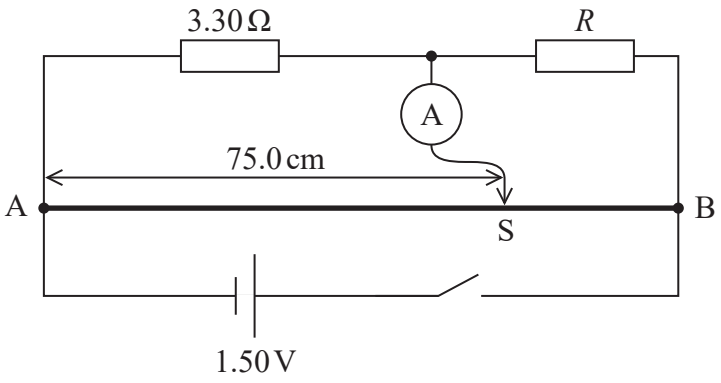
p.d. is proportional to length, so the ratio of lengths = ratio of potentials:

$V = (75.0\ cm \div 100\ cm) \times 1.50\ V = 1.125\ V = 1.13\ V$, which is about 1.1 V

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(c) The metre bridge circuit is shown. The circuit includes a resistor of resistance 3.30 Ω, a very sensitive ammeter and a resistor of unknown resistance *R*.



A metal slider S can be moved along the nichrome wire and pressed firmly against it to make an electrical connection.

When the switch is closed and S is 75.0 cm along the nichrome wire, the ammeter reads 0 A because the potential difference across the ammeter is zero.

Calculate *R*.

(2)

Ammeter reads 0, so the p.d. across 3.30 Ω = p.d. across 75.0 cm of wire = 1.125 V

I = V/R = 1.125 V ÷ 3.30 Ω = 0.341 A (same current through R)

p.d. across R = 1.50 V − 1.125 V = 0.375 V

R = 0.375 V ÷ 0.341 A = 1.10 Ω

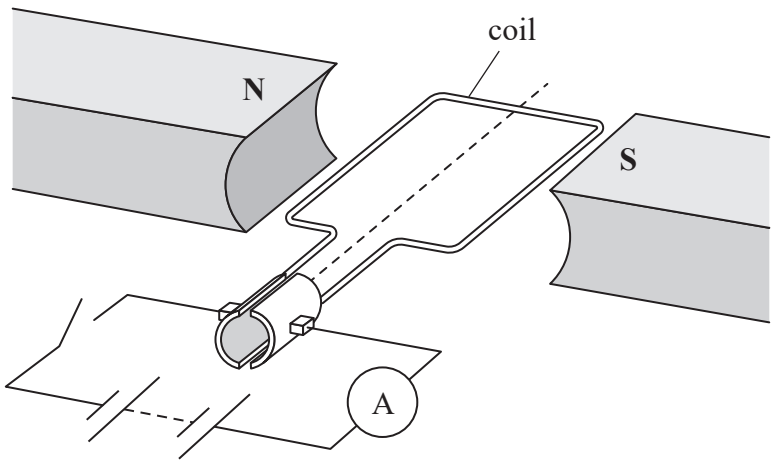
R = 1.10 Ω

(Total for Question 11 = 9 marks)

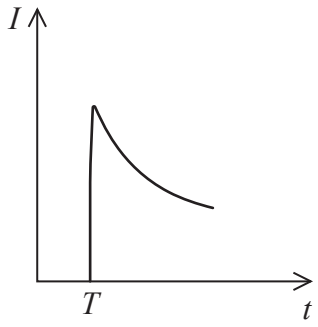
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***12** A simple electric motor consists of a coil that is free to rotate in a magnetic field.

A student connects the motor to an ammeter and a battery.



The graph shows how the current I in the coil varies with time t. The switch is closed at time T.



Explain why the current rises to a maximum then decreases.
Your answer should include a reference to Faraday and Lenz's laws.

(6)

When the switch is closed at T a current flows due to the battery. The coil is not yet moving, so the initial (maximum) current = battery emf ÷ resistance ($I = \varepsilon/R$).

The current-carrying coil is in a magnetic field, so there is a force on the sides of the coil ($F = BIl$) and the coil rotates.

As the coil rotates it cuts the magnetic field lines, so the magnetic flux linkage of the coil changes.

By Faraday's law an emf is induced in the coil, equal to the rate of change of flux linkage.

By Lenz's law the induced emf opposes the change producing it, so it opposes the

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battery emf (a back emf) and the original current.

The resultant emf is reduced, so the current decreases. The faster the coil rotates, the greater the rate of change of flux linkage, the larger the back emf and the smaller the current.

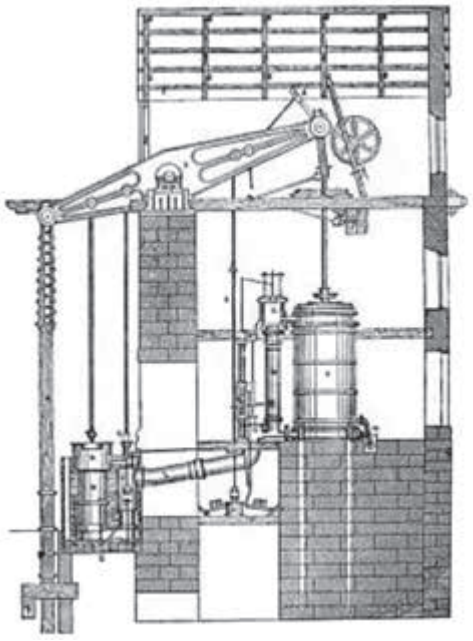
(Total for Question 12 = 6 marks)

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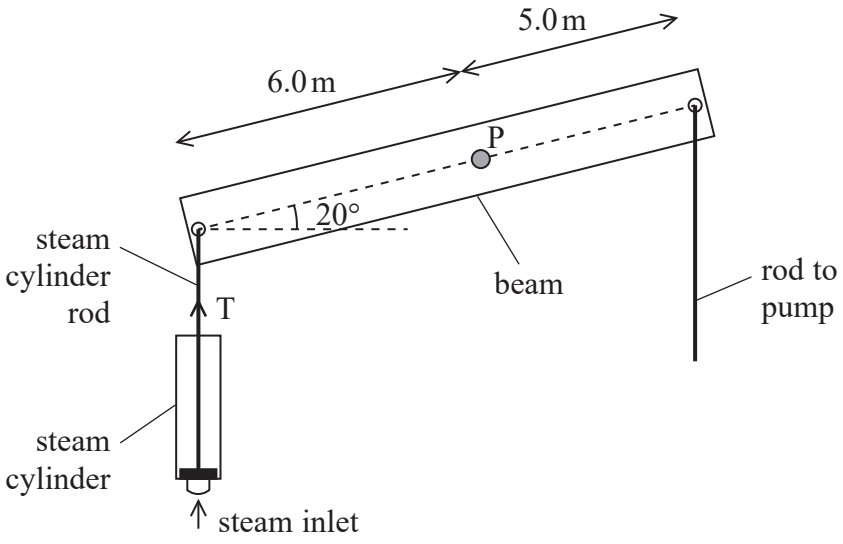
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13 Beam engines contributed to powering the Industrial Revolution in Britain in the 18th century. A beam engine consisted of a beam which could rock to and fro around a well-oiled pivot. Attached to the beam there are two rods, one connected to a piston in a steam cylinder and the other connected to a pump.



The diagram below shows a simplified arrangement of a beam engine.



(a) The beam has a constant thickness and a mass of 3.05×10^4 kg. The length of the beam is 11.0 m. The pivot P is positioned 6.0 m from the steam cylinder end of the beam.

In its resting position the steam cylinder rod is supported by the base of the steam cylinder with the beam at an angle of 20° to the horizontal.

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The steam cylinder rod exerts a force T on the beam. The force exerted on the beam by the pump rod can be neglected.

Calculate the force T.

(4)

Weight of beam acts at its centre of mass, 5.5 m from the end, i.e. 0.5 m from P.

$W = mg = 3.05 \times 10^4$ kg $\times$ 9.81 N kg^{-1} $= 2.99 \times 10^5$ N

Moments about P: clockwise moment = anticlockwise moment

$T \times 6.0$ m $\times \cos 20° = 2.99 \times 10^5$ N $\times$ 0.5 m $\times \cos 20°$

$T = (2.99 \times 10^5$ N $\times$ 0.5 m$) \div 6.0$ m $= 2.49 \times 10^4$ N

$T =$ 2.5×10^4 N (25 kN)

(b) The engine, which ran continuously, could lift a mass of 2500 kg of water through 12 m each minute.
The engine used 1250 kg of coal a day. 1 kg of coal can release 22.3 MJ of energy.
The beam engine was said to have an efficiency of 10%.

Deduce whether this claim for efficiency was correct.

(5)

Energy gained by the water each minute: $\Delta E_{grav} = mg\Delta h = 2500$ kg $\times$ 9.81 N kg^{-1} $\times$ 12 m $= 2.94 \times 10^5$ J (294 kJ per minute)

Energy output per day = 294 kJ $\times$ 60 $\times$ 24 $= 4.24 \times 10^8$ J = 424 MJ

Energy input from the coal per day = 1250 kg $\times$ 22.3 MJ kg^{-1} = 27 900 MJ

efficiency = useful energy output $\div$ total energy input = 424 MJ $\div$ 27 900 MJ = 0.015 = 1.5%

1.5% is much less than 10%, so the claim of 10% efficiency was not correct.

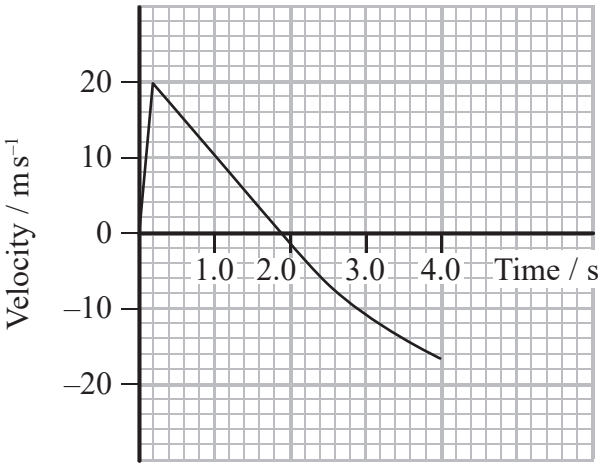
(Total for Question 13 = 9 marks)

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14 A physics class made a toy rocket. A drinks bottle was partially filled with water and inverted over a valve. An air pump delivered air to the bottle until the pressure forced the bottle from the valve and the water was ejected from the bottle at high speed.



A velocity-time graph for the bottle for the first 4 s after take-off is shown.



(a) Determine the height to which the rocket travelled.

(2)

Maximum height is reached when v = 0, at t = 2.0 s. Height = area under the velocity-time graph up to 2.0 s.

Area of triangle = ½ × base × height = ½ × 1.9 s × 20 m s^{-1}

Height = 19 m

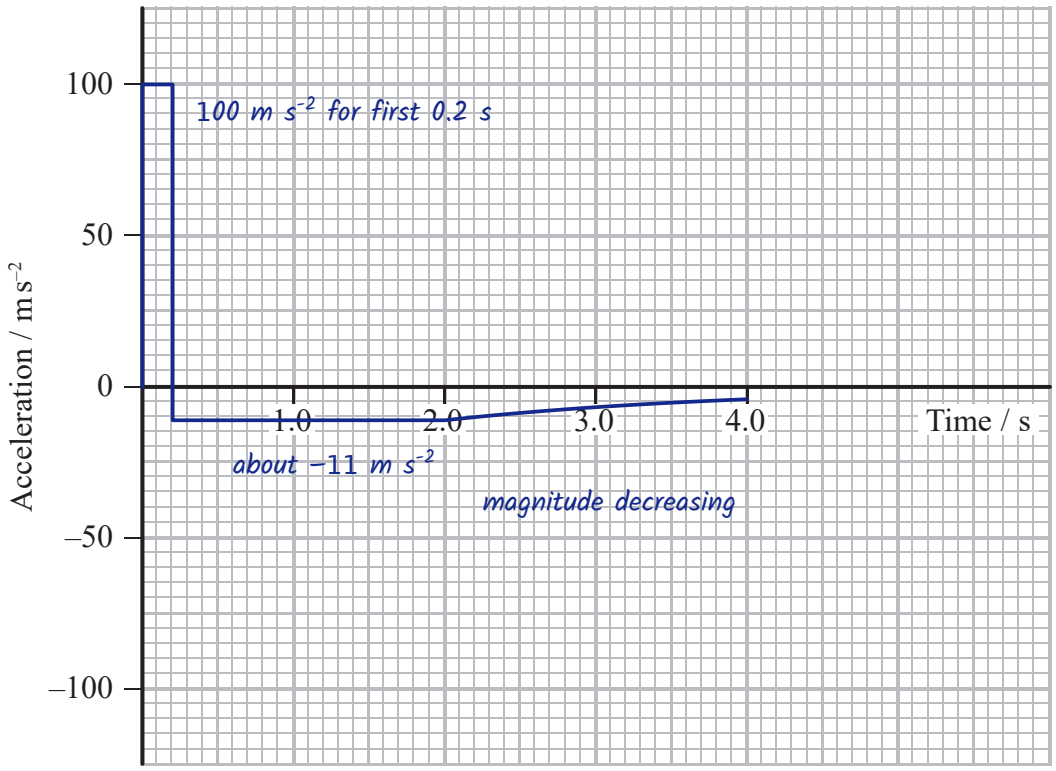
Height = 19 m

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(b) Sketch the corresponding acceleration-time graph on the axes below.

(5)



(Total for Question 14 = 7 marks)

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15 The discovery of the Higgs particle was an important contribution to our understanding of particle physics.

(a) Describe the standard model for subatomic particles. You should identify the fundamental particles and the composition of the particles we can observe.

(5)

In the standard model all matter is made from fundamental particles, quarks and leptons, which are not made of anything smaller.

There are 6 quarks (up, down, strange, charm, top, bottom) and 6 leptons (electron, muon, tau and their three neutrinos).

Each particle has an antiparticle with the same mass but opposite charge.

The particles we observe made from quarks are hadrons. Baryons are made of 3 quarks, e.g. proton = uud, neutron = udd.

Mesons are made of a quark and an antiquark, e.g. π^+ = an up quark and an anti-down quark.

Forces are carried by exchange (gauge) bosons, and the Higgs boson gives particles their mass.

(b) The mass of the Higgs particle is 2.2×10^{-25} kg.

Calculate this mass in GeV/c^2.

(3)

$\Delta E = \Delta mc^2 = 2.2 \times 10^{-25}\ kg \times (3.0 \times 10^8\ m\ s^{-1})^2 = 1.98 \times 10^{-8}\ J$

$E = 1.98 \times 10^{-8}\ J \div 1.6 \times 10^{-19}\ J\ eV^{-1} = 1.24 \times 10^{11}\ eV$

= 124 GeV, so mass = 124 GeV/c^2 (about 120 GeV/c^2)

Mass = 124 GeV/c^2

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(c) The Higgs particle was discovered using the Large Hadron Collider (LHC) in 2012. Two beams of very high energy protons, moving in opposite directions, were made to collide.

(i) Explain the need for such high energy collisions.

(3)

In the collision the (kinetic) energy of the protons is converted into mass (of the Higgs particle), according to $E = mc^2$.

The Higgs particle is very massive (about 120 GeV/c^2) and c^2 is very large, so a lot of energy is needed to create it: at least 120 GeV in total, so at least 60 GeV for each beam.

High energy is also needed to overcome the electrostatic repulsion between the protons.

(ii) The beams of protons are contained within a ring of superconducting magnets.

Calculate the momentum of a proton in a beam.

(3)

magnetic field strength = 8.3 T
circumference of the ring = 27 km

circumference = $2\pi r$, so $r = 27\,000\ m \div 2\pi = 4300\ m$

Magnetic force provides the centripetal force: $Bqv = mv^2/r$, so $p = mv = Bqr$

$p = 8.3\ T \times 1.6 \times 10^{-19}\ C \times 4300\ m = 5.7 \times 10^{-15}\ N\ s$

Momentum = $5.7 \times 10^{-15}\ N\ s$

(iii) State the total momentum of the products of the collision between the two beams of protons.

(1)

Total momentum = 0 (zero)

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(d) The LHC accelerates protons until they gain energies of about 7 TeV.

A student used the equation $E_k = \frac{p^2}{2m}$ to predict the energy of a proton in the beam, using the momentum calculated in (c)(ii), but found the energy was far higher than 7 TeV.

Explain why.

(2)

The protons are moving at very high speeds, close to the speed of light (relativistic speeds).

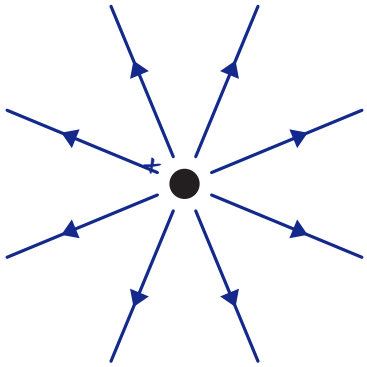
At these speeds the mass of the proton increases, and $E_k = p^2/2m$ is only valid at non-relativistic speeds, so it gives a value far too high.

(Total for Question 15 = 17 marks)

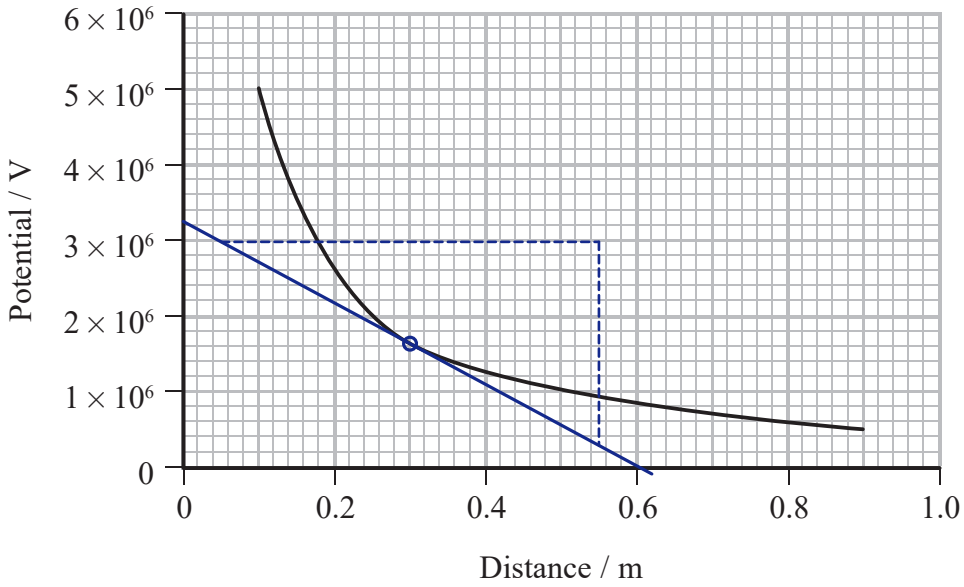
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16 (a) Sketch the electric field around a positive point charge.

(3)



(b) The graph shows how potential varies with distance from the centre of a charged sphere.



Air molecules will be ionised if the electric field strength exceeds $3 \times 10^6\,\text{V m}^{-1}$.

Deduce whether air molecules will be ionised at a distance of 30 cm from the centre of this sphere.

(4)

Tangent drawn at 0.30 m (see graph). E = −gradient of the V against r graph (E = −ΔV/Δr).

gradient = (2.97 − 0.28) × 10^6 V ÷ (0.55 − 0.05) m = −5.4 × 10^6 V m^{-1}

E = 5.4 × 10^6 V m^{-1}, which is greater than 3 × 10^6 V m^{-1}, so air molecules would be ionised at 30 cm.

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(c) A magician did a trick which he claimed was the most dangerous ever. He positioned himself midway between two charged spheres which were separated by a distance of about two metres. Each sphere was charged to a potential that would cause ionisation at a distance of one metre. He wore a protective suit of chain mail and a helmet consisting of a metal cage. The protective suit and helmet were earthed to a potential of 0 V.



A scientist said "there is no danger in this and I would happily do it tomorrow".

Explain whether this statement is justified.

(3)

The metal suit and helmet act as a Faraday cage: they are conducting and are all at the same potential (0 V).

There is no potential gradient inside, so the electric field strength inside the cage is zero and there cannot be a p.d. across his body.

If a spark strikes him, the charge (current) is conducted through the suit to earth, not through his body. So the statement is justified.

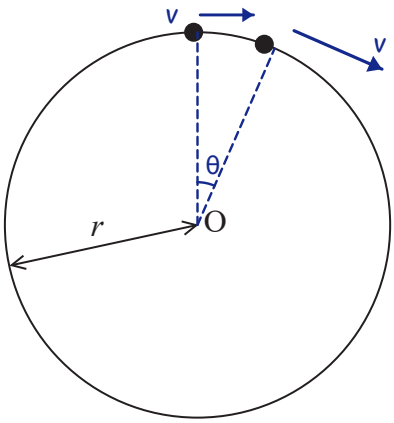
(Total for Question 16 = 10 marks)

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17 A centrifuge is a machine which rotates.

(a) A particle in a centrifuge moves in a circle of radius r, centre O, with a constant speed v.

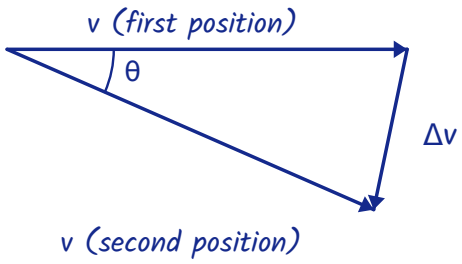
The diagram represents two positions of the particle.



Derive the equation for centripetal acceleration $a = \frac{v^2}{r}$ by considering the velocity at these two positions.

Your answer should include a vector diagram.

(5)



Vector diagram: the velocities v at the two positions drawn tail to tail; the third side of the triangle is the change in velocity Δv (directed towards O).

The velocity turns through the same angle θ as the radius, in time t. Acceleration a = Δv/t

For small angles Δv/v ≈ sin θ ≈ θ (θ in radians), so Δv = vθ and a = vθ/t

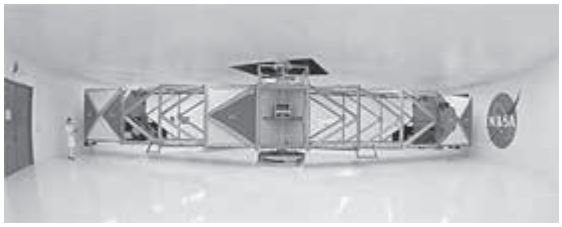
The arc length travelled is vt = rθ, so θ = vt/r

a = (v/t) × (vt/r): the t's cancel, giving $a = v^2/r$

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(b) The United States' space agency, NASA, uses a centrifuge to test whether equipment will operate when experiencing large forces. The equipment to be tested is attached to the end of the frame of the centrifuge, which rotates around a vertical axis at its centre.



The centrifuge rotates at 50 revolutions per minute with a radius of 8.8 m.

(i) Show that the angular velocity of the centrifuge is about 5 rad s^{-1}.

(2)

ω = angle turned ÷ time = (50 × 2π rad) ÷ 60 s

ω = 5.24 rad s^{-1}, which is about 5 rad s^{-1}

(ii) Explain how the centrifuge applies large forces to the equipment under test.

(2)

A resultant (centripetal) force is needed to keep the equipment moving in a circle: $F = mr\omega^2$

The radius r is large (8.8 m), so the equipment has a high linear velocity and the force on it is large (also large if its mass is large).

(iii) The NASA website says the centrifuge can be used to test whether the equipment can withstand accelerations of up to about 25g.

Deduce whether this claim is correct.

(2)

$a = r\omega^2 = 8.8\ m \times (5.24\ rad\ s^{-1})^2 = 242\ m\ s^{-2}$

$242\ m\ s^{-2} \div 9.81\ m\ s^{-2} = 24.6g$, which is about 25g, so the claim is correct.

(Total for Question 17 = 11 marks)

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18 A 'Gauss gun' can be made from five ball bearings of equal mass and two magnets, as shown.



Pairs of ball bearings are placed to the right of two strong magnets. A single ball bearing is released from the left, as shown. The ball bearing is attracted to, and collides with, the first magnet. This and all subsequent collisions can be assumed to be elastic.

(a) Explain what happens to make the last ball bearing on the right subsequently move off with a large velocity.

(3)

The magnet attracts the single ball and accelerates it, so its kinetic energy increases and it hits the magnet at high velocity.

Momentum is conserved in the collisions, so momentum is passed through the magnet to the pair of balls.

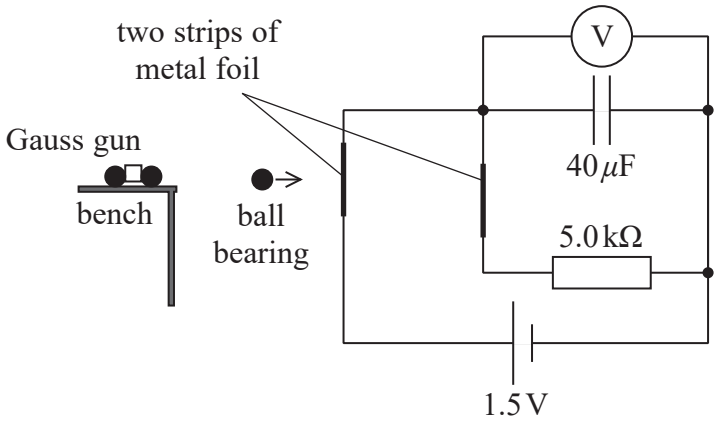
The collisions are elastic, so KE is conserved: the last ball of the pair (equal mass) moves off with the same velocity (KE) as the ball that hit the magnet.

This ball is accelerated by the second magnet and the process repeats, so the last ball leaves even faster.

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(b) A student set up the apparatus shown to measure the speed of the last ball bearing. The 'Gauss gun' was placed at the end of a bench, so that the ball bearing left the gun and broke two strips of metal foil which formed part of an electric circuit.



As the ball bearing left the gun, it broke the first foil strip at its centre so that the capacitor started to discharge. When the ball bearing broke the second foil strip the capacitor discharge stopped.

(i) Calculate the energy stored in the capacitor when it was fully charged.

(2)

$W = \frac{1}{2}CV^2 = \frac{1}{2} \times 40 \times 10^{-6}\ F \times (1.5\ V)^2$

$W = 4.5 \times 10^{-5}\ J$

Energy stored = 45 μJ

(ii) The voltmeter reading halved in the time taken for the ball bearing to travel between the two foil strips.

Show that the time taken for the ball bearing to travel between the two foil strips was about 0.1 s.

(2)

$V = V_0 e^{-t/RC}$ with $V = 0.5V_0$; $RC = 5000\ \Omega \times 40 \times 10^{-6}\ F = 0.20\ s$

$0.5 = e^{-t/0.20s}$, so $\ln 0.5 = -t/0.20\ s$

$t = 0.20\ s \times 0.693 = 0.139\ s \approx 0.14\ s$, which is about 0.1 s

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(iii) The two foil strips were 0.50 m apart.

Calculate the horizontal velocity of the ball bearing.

(2)

v = distance ÷ time = 0.50 m ÷ 0.139 s

$v = 3.6\ m\ s^{-1}$

Horizontal velocity = $3.6\ m\ s^{-1}$

(iv) The student positioned the second foil strip with its centre 8.0 cm lower than the centre of the first foil strip.

Deduce whether the ball bearing broke the second foil strip at its centre.

Assume the ball bearing was travelling horizontally as it broke the first foil strip.

(2)

Vertically: $u = 0$, $a = g = 9.81\ m\ s^{-2}$, $t = 0.139\ s$

$s = \frac{1}{2}at^2 = \frac{1}{2} \times 9.81\ m\ s^{-2} \times (0.139\ s)^2 = 0.094\ m = 9.4\ cm$

The ball falls about 9 cm, more than 8.0 cm, between the strips, so it did not break the second foil strip at its centre (it hit about 1 cm lower).

(Total for Question 18 = 11 marks)

TOTAL FOR PAPER = 90 MARKS

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List of data, formulae and relationships

Acceleration of free fall	$g = 9.81\ \text{m s}^{-2}$	(close to Earth's surface)
Boltzmann constant	$k = 1.38 \times 10^{-23}\ \text{J K}^{-1}$	
Coulomb law constant	$k = \frac{1}{4\pi\varepsilon_0} = 8.99 \times 10^{9}\ \text{N m}^2\ \text{C}^{-2}$	
Electron charge	$e = -1.60 \times 10^{-19}\ \text{C}$	
Electron mass	$m_e = 9.11 \times 10^{-31}\ \text{kg}$	
Electronvolt	$1\ \text{eV} = 1.60 \times 10^{-19}\ \text{J}$	
Gravitational constant	$G = 6.67 \times 10^{-11}\ \text{N m}^2\ \text{kg}^{-2}$	
Gravitational field strength	$g = 9.81\ \text{N kg}^{-1}$	(close to Earth's surface)
Permittivity of free space	$\varepsilon_0 = 8.85 \times 10^{-12}\ \text{F m}^{-1}$	
Planck constant	$h = 6.63 \times 10^{-34}\ \text{J s}$	
Proton mass	$m_p = 1.67 \times 10^{-27}\ \text{kg}$	
Speed of light in a vacuum	$c = 3.00 \times 10^{8}\ \text{m s}^{-1}$	
Stefan-Boltzmann constant	$\sigma = 5.67 \times 10^{-8}\ \text{W m}^{-2}\ \text{K}^{-4}$	
Unified atomic mass unit	$u = 1.66 \times 10^{-27}\ \text{kg}$	

Mechanics

Kinematic equations of motion

$$s = \frac{(u + v)t}{2}$$

$$v = u + at$$

$$s = ut + \frac{1}{2}at^2$$

$$v^2 = u^2 + 2as$$

Forces

$$\Sigma F = ma$$

$$g = \frac{F}{m}$$

$$W = mg$$

moment of force $= Fx$

Momentum

$$p = mv$$

Work, energy and power

$$\Delta W = F\Delta s$$

$$E_k = \frac{1}{2}mv^2$$

$$\Delta E_{grav} = mg\Delta h$$

$$P = \frac{E}{t}$$

$$P = \frac{W}{t}$$

$$\text{efficiency} = \frac{\text{useful energy output}}{\text{total energy input}}$$

$$\text{efficiency} = \frac{\text{useful power output}}{\text{total power input}}$$

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Electric circuits

Potential difference

$$V = \frac{W}{Q}$$

Resistance

$$R = \frac{V}{I}$$

Electrical power and energy

$$P = VI$$

$$P = I^2R$$

$$P = \frac{V^2}{R}$$

$$W = VIt$$

Resistivity

$$R = \frac{\rho l}{A}$$

Current

$$I = \frac{\Delta Q}{\Delta t}$$

$$I = nqvA$$

Materials

Density

$$\rho = \frac{m}{V}$$

Stokes' law

$$F = 6\pi\eta rv$$

Hooke's law

$$\Delta F = k\Delta x$$

Young modulus

$$\text{Stress } \sigma = \frac{F}{A}$$

$$\text{Strain } \varepsilon = \frac{\Delta x}{x}$$

$$E = \frac{\sigma}{\varepsilon}$$

Elastic strain energy

$$\Delta E_{\text{el}} = \frac{1}{2}F\Delta x$$

Waves and Particle Nature of Light

Wave speed

$$v = f\lambda$$

Speed of a transverse wave on a string

$$v = \sqrt{\frac{T}{\mu}}$$

Intensity of radiation

$$I = \frac{P}{A}$$

Power of a lens

$$P = \frac{1}{f}$$

$$P = P_1 + P_2 + P_3 + \ldots$$

Thin lens equation

$$\frac{1}{u} + \frac{1}{v} = \frac{1}{f}$$

Magnification for a lens

$$m = \frac{\text{image height}}{\text{object height}} = \frac{v}{u}$$

Diffraction grating

$$n\lambda = d \sin\theta$$

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Refractive index

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$n = \frac{c}{v}$$

Critical angle

$$\sin C = \frac{1}{n}$$

Photon model

$$E = hf$$

Einstein's photoelectric equation

$$hf = \phi + \frac{1}{2}mv^2_{\max}$$

de Broglie wavelength

$$\lambda = \frac{h}{p}$$

Further mechanics

Impulse

$$F\Delta t = \Delta p$$

Kinetic energy of a non-relativistic particle

$$E_k = \frac{p^2}{2m}$$

Motion in a circle

$$v = \omega r$$

$$T = \frac{2\pi}{\omega}$$

$$F = ma = \frac{mv^2}{r}$$

$$a = \frac{v^2}{r}$$

$$a = r\omega^2$$

Centripetal force

$$F = \frac{mv^2}{r}$$

$$F = mr\omega^2$$

Fields

Coulomb's law

$$F = k\frac{Q_1Q_2}{r^2}$$

$$\text{where } k = \frac{1}{4\pi\varepsilon_0}$$

Electric field strength

$$E = \frac{F}{Q}$$

$$E = k\frac{Q}{r^2}$$

$$E = \frac{V}{d}$$

Electric potential

$$V = k\frac{Q}{r}$$

Capacitance

$$C = \frac{Q}{V}$$

Energy stored in a capacitor

$$W = \frac{1}{2}QV$$

Capacitor discharge

$$Q = Q_0e^{-t/RC}$$

Resistor – capacitor discharge

$$I = I_0e^{-t/RC}$$

$$V = V_0e^{-t/RC}$$

In a magnetic field

$$F = BIl \sin \theta$$

$$F = Bqv \sin \theta$$

Faraday's and Lenz's laws

$$\varepsilon = \frac{-\mathrm{d}(N\phi)}{\mathrm{d}t}$$

Root-mean-square values

$$V_{\text{rms}} = \frac{V_0}{\sqrt{2}}$$

$$I_{\text{rms}} = \frac{I_0}{\sqrt{2}}$$

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Nuclear and particle physics

In a magnetic field

$$r = \frac{p}{BQ}$$

Thermodynamics

Heating

$$\Delta E = mc\Delta\theta$$

$$\Delta E = L\Delta m$$

Molecular kinetic theory

$$\frac{1}{2}m\langle c^2\rangle = \frac{3}{2}kT$$

$$pV = \frac{1}{3}Nm\langle c^2\rangle$$

Ideal gas equation

$$pV = NkT$$

Stefan-Boltzmann law

$$L = \sigma AT^4$$

$$L = \sigma 4\pi r^2 T^4$$

Wien's law

$$\lambda_{max} T = 2.898 \times 10^{-3} \text{ m K}$$

Space

Intensity

$$I = \frac{L}{4\pi d^2}$$

Redshift of electromagnetic radiation

$$z = \frac{\Delta\lambda}{\lambda} \approx \frac{\Delta f}{f} \approx \frac{v}{c}$$

Cosmological expansion

$$v = H_0 d$$

Nuclear radiation

Mass-energy

$$\Delta E = c^2\Delta m$$

Radioactive decay

$$A = \lambda N$$

$$\frac{dN}{dt} = -\lambda N$$

$$\lambda = \frac{\ln 2}{t_{½}}$$

$$N = N_0 e^{-\lambda t}$$

$$A = A_0 e^{-\lambda t}$$

Gravitational fields

Gravitational force

$$F = \frac{Gm_1m_2}{r^2}$$

Gravitational field strength

$$g = \frac{Gm}{r^2}$$

Gravitational potential

$$V_{grav} = \frac{-Gm}{r}$$

Oscillations

Simple harmonic motion

$$F = -kx$$

$$a = -\omega^2 x$$

$$x = A\cos\omega t$$

$$v = -A\omega\sin\omega t$$

$$a = -A\omega^2\cos\omega t$$

$$T = \frac{1}{f} = \frac{2\pi}{\omega}$$

$$\omega = 2\pi f$$

Simple harmonic oscillator

$$T = 2\pi\sqrt{\frac{m}{k}}$$

$$T = 2\pi\sqrt{\frac{l}{g}}$$

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