Write your name here

Surname: StemUp Model Solution

Other names:

**Pearson Edexcel Level 3 GCE**

Centre Number

Candidate Number

# Physics

## Advanced
## Paper 2: Advanced Physics II

Wednesday 21 June 2017 – Morning
**Time: 1 hour 45 minutes**

Paper Reference
**9PH0/02**

**You do not need any other materials.**

Total Marks

### Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Answer the questions in the spaces provided
  – *there may be more space than you need.*

### Information

- The total mark for this paper is 90.
- The marks for **each** question are shown in brackets
  – *use this as a guide as to how much time to spend on each question.*
- You may use a scientific calculator.
- In questions marked with an **asterisk** (*), marks will be awarded for your ability to structure your answer logically showing how the points that you make are related or follow on from each other where appropriate.

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- You are advised to show your working in calculations including units where appropriate.

*Turn over* ▶

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**Answer ALL questions.**

**All multiple choice questions must be answered with a cross ☒ in the box for the correct answer from A to D. If you change your mind about an answer, put a line through the box ☒ and then mark your new answer with a cross ☒.**

**1** Which of the following wave properties is **not** exhibited by sound waves?

☒ **A** diffraction

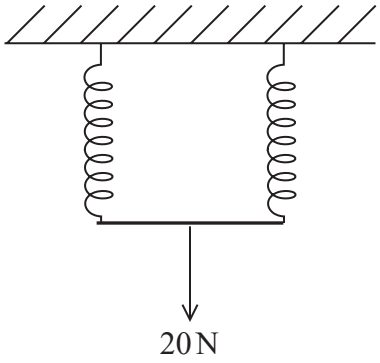
☒ **B** interference

☒ **C** polarisation

☒ **D** refraction

**(Total for Question 1 = 1 mark)**

**2** Two identical springs are arranged side by side as shown.




When a force of 20 N is applied, an extension of 8 cm is obtained.

A force of 5 N is applied to one of the springs on its own.

Which of the following is the extension obtained?

☒ **A** 2 cm

☒ **B** 4 cm

☒ **C** 8 cm

☒ **D** 16 cm

**(Total for Question 2 = 1 mark)**

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**3** A playground swing completes 24 oscillations in 1 minute.

Which of the following is the frequency of the oscillations?

☒ **A** 0.042 Hz

☒ **B** 0.40 Hz

☒ **C** 2.5 Hz

☒ **D** 24 Hz

**(Total for Question 3 = 1 mark)**

**4** Which of the following is **not** a similarity between gravitational fields and electric fields?

☒ **A** For a point charge or point mass, the field follows the inverse square law.

☒ **B** For a point charge or point mass, the field is radial.

☒ **C** Both fields act at a distance.

☒ **D** Both fields act on all particles.

**(Total for Question 4 = 1 mark)**

**5** A data book contains the following information for ethanol.

latent heat of fusion = 109 kJ kg$^{-1}$

latent heat of vaporisation = 838 kJ kg$^{-1}$

545 J is transferred from a sample of ethanol when it condenses.

Which of the following shows how to calculate the mass of ethanol that condenses?

☒ **A** 545 ÷ 109 000

☒ **B** 545 ÷ 838 000

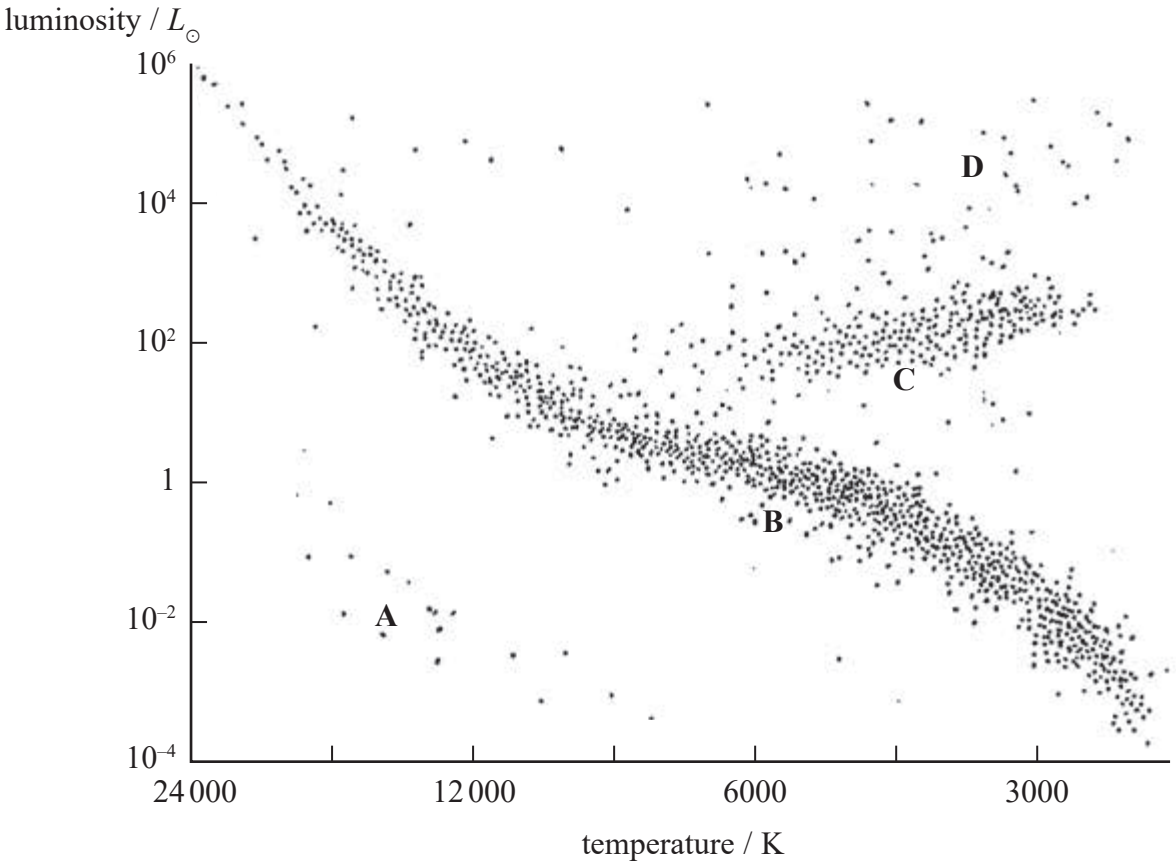
☒ **C** 109 000 ÷ 545

☒ **D** 838 000 ÷ 545

**(Total for Question 5 = 1 mark)**

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**6** Four regions **A**, **B**, **C** and **D** are labelled on the Hertzsprung-Russell diagram.




Which region includes the position of the Sun?

- ☒ **A**
- ☒ **B**
- ☒ **C**
- ☒ **D**

**(Total for Question 6 = 1 mark)**

**7** A black body radiator of temperature $T$ and surface area $A$ has a luminosity $L$.

Which of the following is the luminosity of a black body radiator with surface area $A/2$ and temperature $2T$?

- ☒ **A** $\frac{L}{2}$
- ☒ **B** $L$
- ☒ **C** $4L$
- ☒ **D** $8L$

**(Total for Question 7 = 1 mark)**

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**8** A line in the hydrogen spectrum of a star in the Milky Way galaxy is observed to have a wavelength of 656.3 nm. In a laboratory on Earth this line has a wavelength of 654.9 nm.

Which of the following expressions gives the magnitude of the velocity of the star relative to Earth?

☒ **A** $\frac{656.3}{654.9} \times 3 \times 10^8 \text{ m s}^{-1}$

☒ **B** $\frac{654.9}{(656.3 - 654.9)} \times 3 \times 10^8 \text{ m s}^{-1}$

☒ **C** $\frac{654.9}{656.3} \times 3 \times 10^8 \text{ m s}^{-1}$

☒ **D** $\frac{(656.3 - 654.9)}{654.9} \times 3 \times 10^8 \text{ m s}^{-1}$

**(Total for Question 8 = 1 mark)**

**9** An object is placed 6.5 cm away from a lens of focal length 3.9 cm. An image is formed 9.8 cm from the lens.

Which of the following is the magnification?

☒ **A** 0.60

☒ **B** 0.66

☒ **C** 1.5

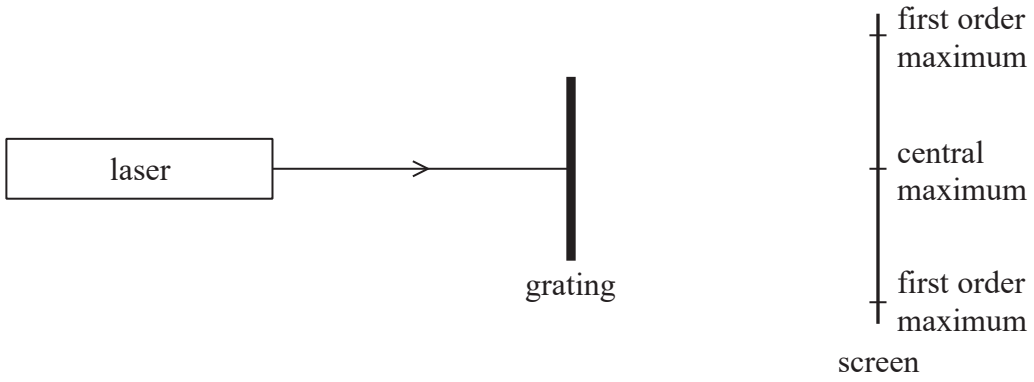
☒ **D** 1.7

**(Total for Question 9 = 1 mark)**

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**10** A beam of light from a laser is directed at a diffraction grating.

The diagram shows the positions of the central maximum and the first order maxima on a screen.




Which of the following would cause the first order maxima to be closer to the central maximum on the screen?

☒ **A** moving the laser closer to the grating

☒ **B** moving the screen further from the grating

☒ **C** using a grating with more lines per metre

☒ **D** using laser light with a higher frequency

**(Total for Question 10 = 1 mark)**

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**11** An electric iron rated at 2600 W contains a steel plate which is heated to a working temperature of 215 °C. Room temperature is 18 °C.

Deduce whether the plate could reach its working temperature in less than 1 minute.

mass of steel plate = 890 g

specific heat capacity of steel = 450 J $kg^{-1}$ $K^{-1}$

**(3)**

*Energy needed: $\Delta E = mc\Delta\theta$ = 0.890 kg × 450 J $kg^{-1}$ $K^{-1}$ × (215 − 18) K*

*$\Delta E$ = 78 900 J*

*Time needed: P = E/t so t = E/P = 78 900 J ÷ 2600 W = 30 s*

*30 s is less than 1 minute, so yes, the plate could reach its working temperature in less than 1 minute.*

**(Total for Question 11 = 3 marks)**

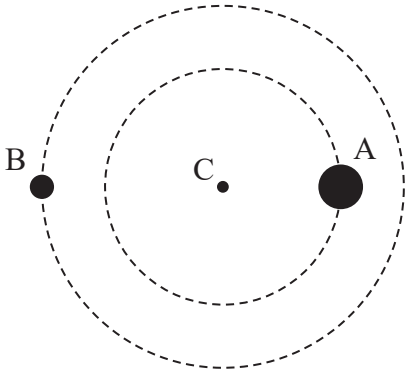
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**12** The diagram shows two black holes, A and B, orbiting each other.

Assume that the centre of mass C of the system is the centre of a circular orbit for each black hole as shown in the diagram.




Black hole A is in an orbit of radius $2.9 \times 10^{10}$ m and black hole B is in an orbit of radius $3.6 \times 10^{10}$ m. Both orbit with the same period, so the total distance between them is $6.5 \times 10^{10}$ m.

(a) Calculate the force between the black holes.

mass of Sun, $M_\odot = 1.99 \times 10^{30}$ kg
mass of black hole A = $36M_\odot$
mass of black hole B = $29M_\odot$

**(2)**

$F = Gm_1m_2/r^2 = 6.67 \times 10^{-11} \times (36 \times 1.99 \times 10^{30}) \times (29 \times 1.99 \times 10^{30})$ $\div (6.5 \times 10^{10})^2$ so $F = 6.5 \times 10^{31}$ N

Force = $6.5 \times 10^{31}$ N

(b) By considering the orbit of one black hole about C, determine the period of the orbit.

**(3)**

For B: $F = mv^2/r$ with $v = 2\pi r/T$, so $F = 4\pi^2 mr/T^2$

$T^2 = 4\pi^2 mr/F = 4\pi^2 \times (29 \times 1.99 \times 10^{30}\ kg) \times 3.6 \times 10^{10}\ m \div 6.5 \times 10^{31}$ N

$T^2 = 1.26 \times 10^{12}\ s^2$, so $T = 1.1 \times 10^6$ s

Period = $1.1 \times 10^6$ s

**(Total for Question 12 = 5 marks)**

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**13** The distance to astronomical objects relatively close to the Sun is determined using trigonometric parallax. For objects beyond a certain distance standard candles are used.

(a) State what is meant by a standard candle.

**(1)**

An object (astronomical source) of known luminosity.

(b) Explain why trigonometric parallax is not used beyond a certain distance.

**(2)**

Beyond a certain distance the parallax angle becomes very small (the diameter of the Earth's orbit is very small compared with the distance).

So the angle cannot be measured precisely, giving a very large percentage uncertainty in the distance.

(c) Describe how distances too large for the use of standard candles can be determined.

**(3)**

Measure the change in wavelength (or frequency) of a known spectral line in light from the distant galaxy compared with the laboratory value.

Calculate the redshift $z = \Delta\lambda/\lambda$ and use $z = v/c$ to determine the velocity of the galaxy relative to Earth.

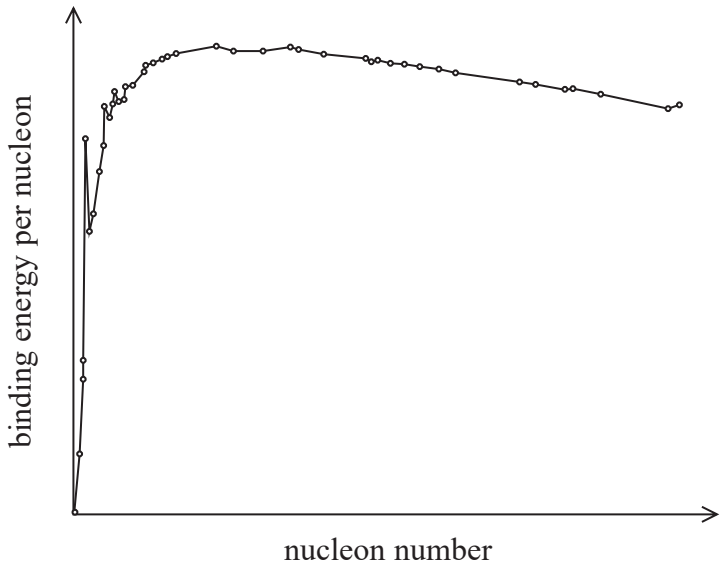
Then apply Hubble's law $v = H_0 d$ to calculate the distance, $d = v/H_0$.

**(Total for Question 13 = 6 marks)**

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**14** Nuclear fusion involves small nuclei joining to make larger nuclei. Nuclear fission involves large nuclei splitting to become smaller nuclei. Both of these processes release energy.

(a) The graph shows how the binding energy per nucleon varies with nucleon number for a range of isotopes.




Use the binding energy per nucleon curve to explain how fusion and fission both release energy.

**(3)**

*Fusion: small nuclei join to make a larger nucleus, so the binding energy per nucleon increases as the number of nucleons increases.*

*Fission: a large nucleus splits into smaller nuclei, so the binding energy per nucleon increases as the number of nucleons decreases.*

*In both processes the binding energy per nucleon increases, and whenever this happens energy is released.*

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(b) Explain the conditions required to bring about and maintain nuclear fusion.

**(3)**

A very high temperature and a very high density (pressure) are needed.

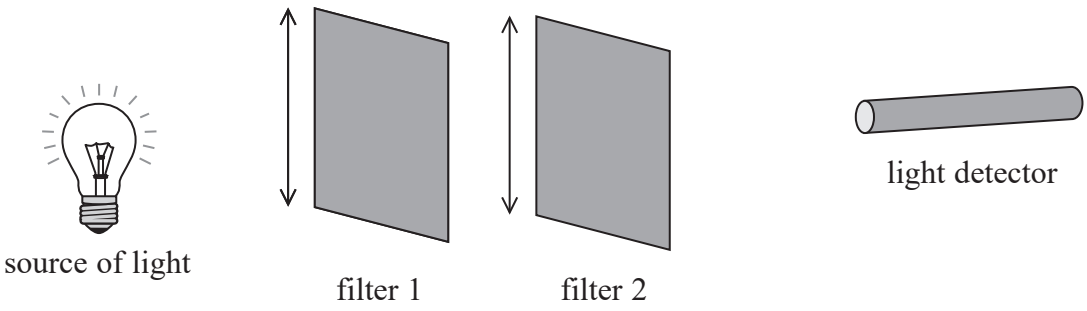
The very high temperature gives the nuclei enough kinetic energy to overcome the electrostatic repulsion between the positive nuclei, so they get close enough for the strong force to act and they fuse.

The very high density gives a high enough collision rate between nuclei to maintain the reaction.

**(Total for Question 14 = 6 marks)**

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***15** The diagram shows apparatus used to investigate polarising filters.



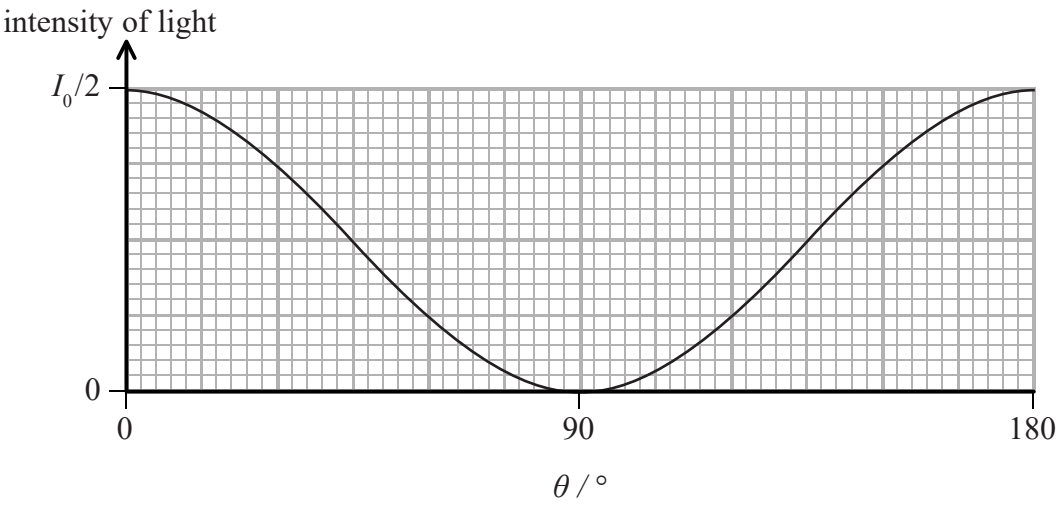

The arrows show the orientation of the plane of polarisation of the filters.

Light is incident on filter 1 and the intensity of the light is measured, using the light detector, when the filters are in the positions shown.

Filter 2 is then rotated and the intensity of light is measured for different angles of rotation $\theta$.

The intensity of light measured with no filters present is $I_0$.

The results are shown on the graph.




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Explain the effect of the filters on the intensity of light and why the intensity varies as shown.

**(6)**

Light from the source is unpolarised: it has oscillations (of the electric field) in all planes perpendicular to the direction of travel.

Filter 1 only transmits the component of the oscillations parallel to its plane of polarisation and absorbs the perpendicular components. So the light leaving filter 1 is plane polarised and its intensity is reduced to $I_0/2$.

At $\theta = 0°$ (and 180°) filter 2 is aligned with filter 1, so all the light that passes through filter 1 also passes through filter 2. The intensity stays at $I_0/2$, the maximum on the graph.

As filter 2 is rotated, only the component of the polarised light from filter 1 in the plane of filter 2 is allowed through, so the intensity gradually reduces.

At 90° the planes of polarisation of the two filters are at right angles, so all the light from filter 1 is absorbed by filter 2 and the intensity is zero.

Beyond 90° the component in the plane of filter 2 increases again, so the intensity rises back to $I_0/2$ at 180°.

**(Total for Question 15 = 6 marks)**

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**16** A student is investigating a 'Cartesian diver'.

The diver is made from a plastic pipette. When placed in a plastic bottle full of water the diver rises to the top and touches the lid.



(a) Show that the downward force of the lid on the diver is about 0.02 N.

volume of diver = $8.0 \times 10^{-6}\,m^3$

mass of diver = 0.0059 kg

density of water = $1.0 \times 10^{3}\,kg\,m^{-3}$

**(3)**

*Mass of water displaced = $\rho V = 1.0 \times 10^{3} \times 8.0 \times 10^{-6} = 8.0 \times 10^{-3}$ kg*

*Upthrust = $mg = 8.0 \times 10^{-3} \times 9.81 = 0.0785$ N*

*Weight of diver = $0.0059 \times 9.81 = 0.0579$ N*

*Force of lid = upthrust − weight = $0.0785 - 0.0579 = 0.0206$ N $\approx 0.02$ N*

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(b) When the pressure is increased by squeezing the bottle, water is forced into the diver increasing its weight. The diver sinks, then remains at rest in the position shown.



The volume of air in the empty pipette in part (a) was $8.0 \times 10^{-6}\,m^3$.

Show that the volume now occupied by the air is about $6 \times 10^{-6}\,m^3$.

**(3)**

Diver at rest, so the weight of water that entered = the force of the lid (0.0206 N)

Volume of water = $F/(\rho g) = 0.0206 \div (9.81 \times 1.0 \times 10^3) = 2.1 \times 10^{-6}\ m^3$

Volume of air = $8.0 \times 10^{-6} - 2.1 \times 10^{-6} = 5.9 \times 10^{-6}\ m^3 \approx 6 \times 10^{-6}\ m^3$

(c) The pressure of the air in the empty pipette in part (a) was $1.01 \times 10^5\,Pa$.

Calculate the pressure of the air in part (b).

**(2)**

$pV$ = constant (same mass of air, constant temperature): $p_1V_1 = p_2V_2$

$p_2 = 1.01 \times 10^5\ Pa \times 8.0 \times 10^{-6}\ m^3 \div 5.9 \times 10^{-6}\ m^3 = 1.37 \times 10^5\ Pa$

Pressure = $1.4 \times 10^5\ Pa$

**(Total for Question 16 = 8 marks)**

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**17** A coulombmeter is used to measure charge.




In a laboratory demonstration of the photoelectric effect, a sheet of zinc was placed on top of a coulombmeter and the zinc was given a negative charge.

*(a) The following observations were made:

- under normal lighting conditions the charge remained constant
- when the zinc was illuminated with ultraviolet light, the magnitude of the charge on the zinc decreased as time passed
- when a larger sheet of zinc was used the charge on the zinc decreased more rapidly.

In each case the initial charge on the zinc was the same.

Explain these observations.

**(6)**

Light consists of photons, each with energy E = hf. One photon interacts with one electron in the zinc.

An electron is only emitted (photoemission) if the photon energy is greater than the work function of zinc, i.e. the frequency is above the threshold frequency.

Photons of normal laboratory light have too low a frequency, so their energy is less than the work function. No electrons are emitted however intense the light, so the charge remains constant.

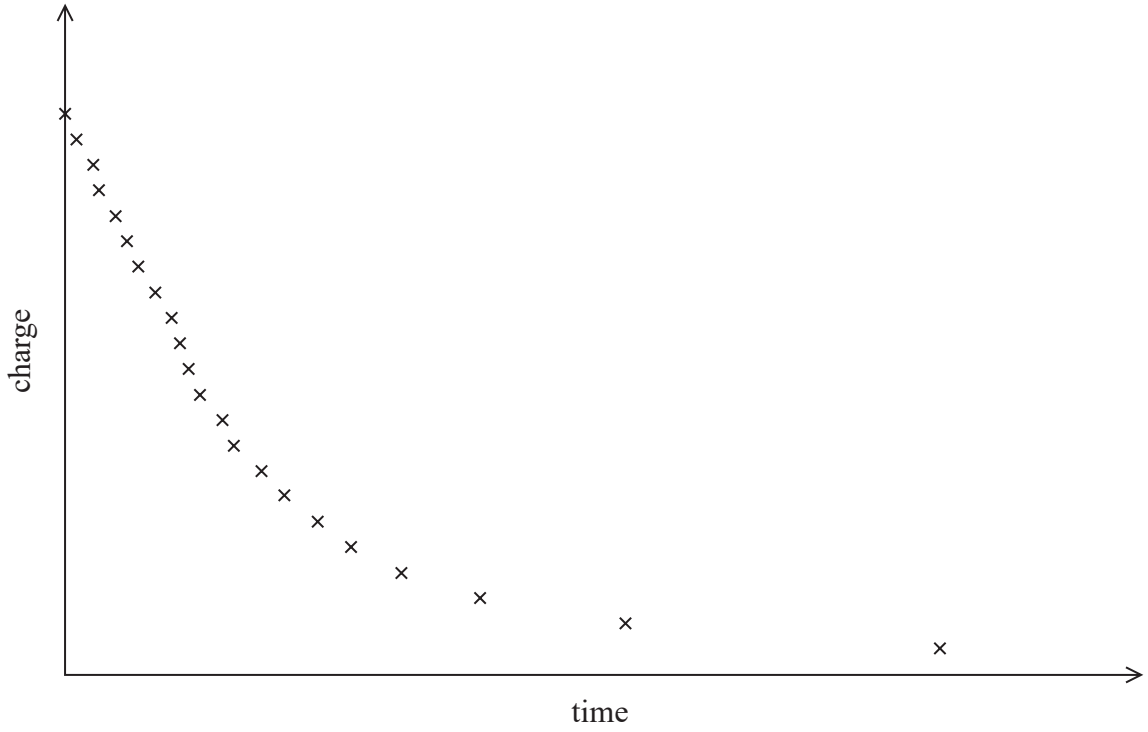
UV photons have a high enough frequency, so their energy is greater than the work function and electrons are emitted. The zinc loses electrons, so the magnitude of the negative charge decreases.

With a larger sheet more photons are incident on (absorbed by) the zinc in a given time, so more electrons are emitted in a given time and the charge is lost more quickly.

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(b) For one sheet of zinc, the charge at different times was measured.

The following graph was obtained.




A student suggests that this is an exponential decay curve.
Explain how this suggestion could be tested.

**(3)**

If it is exponential decay the charge would be of the form $Q = Q_0e^{-kt}$,

so $\ln Q = \ln Q_0 - kt$.

Read pairs of values of charge and time from the graph and plot a graph of ln (charge) against time.

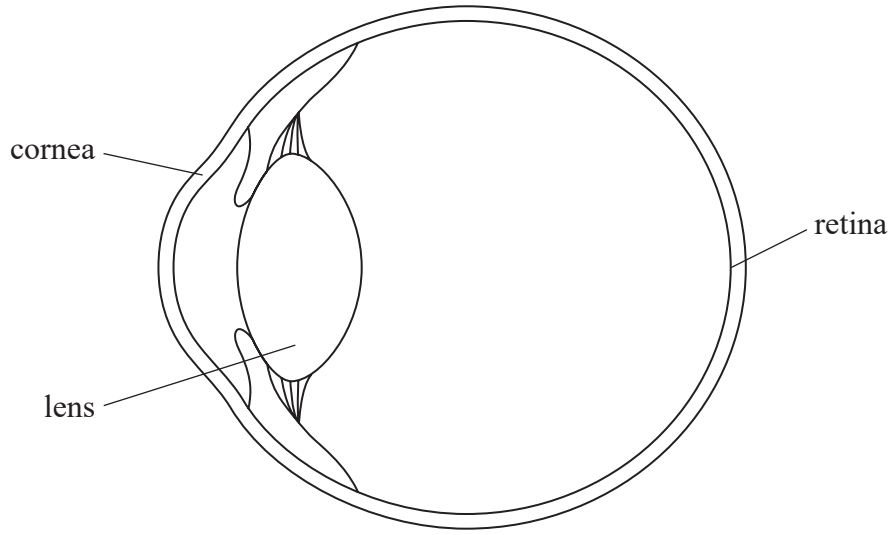
If this gives a straight line with a negative gradient, the decay is exponential.

(Alternatively: check that $Q/Q_0$ is the same for equal time intervals, or that the time to halve is constant.)

**(Total for Question 17 = 9 marks)**

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**18** Light entering a normal eye is refracted by both the cornea and the lens before a focused image is formed on the retina.




(a) It is suggested that the cornea provides 80% of the focusing power of the eye.

Determine whether this is correct.

focal length of cornea = 2.23 cm

focal length of lens for near object = 5.27 cm

**(4)**

Power = 1/f: $P_{cornea}$ = 1 ÷ 0.0223 m = 44.8 D

$P_{lens}$ = 1 ÷ 0.0527 m = 19.0 D

Total power P = $P_1$ + $P_2$ = 44.8 + 19.0 = 63.8 D

Percentage from cornea = 44.8 ÷ 63.8 × 100 = 70%

70% is less than 80%, so the suggestion is not correct.

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(b) Light from a point object forms a focused image on the retina.

The cornea and lens may be treated as a single lens of focal length 1.6 cm that is 2.4 cm from the retina.

(i) Calculate the distance from the point object to this single lens when a focused image is formed on the retina.

**(2)**

$1/f = 1/u + 1/v$ so $1/1.6 = 1/u + 1/2.4$

$1/u = 0.625 - 0.417 = 0.208\ cm^{-1}$, so $u = 4.8$ cm

Distance = 4.8 cm

(ii) A ray of light strikes the front of the cornea at an angle to the normal in air of 15°.

Calculate the angle of the ray to the normal in the cornea.

speed of light in air = $3.00 \times 10^8\ m\,s^{-1}$

speed of light in cornea = $2.18 \times 10^8\ m\,s^{-1}$

**(3)**

$n = c/v = 3.00 \times 10^8 \div 2.18 \times 10^8 = 1.38$

$n_1 \sin\theta_1 = n_2 \sin\theta_2$: $1 \times \sin 15° = 1.38 \times \sin\theta$

$\sin\theta = 0.188$, so $\theta = 10.8°$

Angle to normal in cornea = 11° (10.8°)

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(c) People swimming under water often wear goggles. The goggles enable them to see objects under water clearly whereas without goggles objects appear blurred.

Explain why wearing goggles has this effect.

speed of light in water = $2.25 \times 10^8\ m\,s^{-1}$

**(3)**

*Refractive index from air to cornea = 3.00/2.18 = 1.38, but from water to cornea = 2.25/2.18 = 1.03. The difference in speed of light from water to cornea is much smaller than from air to cornea.*

*So under water there is much less refraction at the cornea: the power of the cornea (eye) is reduced and its focal length increased, so the image forms behind the retina and objects look blurred.*

*If goggles are worn there is a layer of air in front of the eye, so the interface is air to cornea and refraction is as normal, so the image is focused on the retina.*

**(Total for Question 18 = 12 marks)**

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**19** A school science department keeps a sample of potassium chloride to use as a test source for Geiger-Müller tubes.




Potassium contains 0.012% of the unstable isotope potassium-40.

(a) Potassium-40 undergoes $\beta^-$ decay, producing a stable isotope of calcium.

Complete the nuclear equation for this decay.

**(2)**

$$^{40}_{19}\mathrm{K} \rightarrow {}^{40}_{20}\mathrm{Ca} + {}^{0}_{-1}\beta + \bar{\nu}_e$$

(b) A teacher makes some measurements using the potassium chloride test source to determine whether a Geiger-Müller tube is sufficiently efficient at detecting β radiation.

(i) The potassium chloride sample has a mass of 300 mg.
Show that the number of nuclei of potassium-40 in the sample is about $3 \times 10^{17}$.

number of potassium nuclei in 1 g of potassium chloride = $8.1 \times 10^{21}$

**(2)**

$N = 0.300\ g \times 8.1 \times 10^{21}\ g^{-1} \times 0.012/100$

$N = 2.9 \times 10^{17}$ nuclei ($\approx 3 \times 10^{17}$)

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(ii) Show that the activity of this sample is about 5 Bq.

half-life of potassium-40 = $1.25 \times 10^9$ years

**(3)**

$t_{½} = 1.25 \times 10^9 \times 365 \times 24 \times 3600\ s = 3.94 \times 10^{16}\ s$

$\lambda = \ln 2 / t_{½} = 0.693 \div 3.94 \times 10^{16}\ s = 1.76 \times 10^{-17}\ s^{-1}$

$A = \lambda N = 1.76 \times 10^{-17}\ s^{-1} \times 2.9 \times 10^{17} = 5.1\ Bq \approx 5\ Bq$

(iii) With no sample in front of the Geiger-Müller tube, a count rate of 15 counts per minute is recorded. When the potassium chloride test sample is placed next to the Geiger-Müller tube 176 counts are recorded in a period of 10 minutes.

A detector is considered efficient if it detects at least 7.5% of beta emissions from the source.

Determine whether this Geiger-Müller tube can be considered efficient.

**(3)**

Background in 10 min = 15 × 10 = 150 counts

Counts from source = 176 − 150 = 26

Count rate = 26 ÷ 600 s = 0.043 Bq

Percentage detected = 0.043 ÷ 5.1 × 100 = 0.85%

0.85% is much less than 7.5% (7.5% of 5.1 Bq = 0.38 Bq), so the tube cannot be considered efficient.

(iv) Explain a possible reason why only a low proportion of the decays are detected.

**(2)**

The β particles are emitted in all directions, so only a small fraction travel towards the window of the tube.

Also some β particles are absorbed by the sample material itself or by the window of the tube before they can be detected.

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(c) The science department also has a sample of strontium-90. This undergoes beta decay with a half-life of 29 years.

State why the half-life of potassium-40 makes the potassium chloride a more suitable material than strontium-90 for the test.

**(1)**

*The half-life of potassium-40 is so long that the proportion of unstable nuclei, and so the activity, does not change significantly over time (Sr-90's activity would fall noticeably over the years).*

**(Total for Question 19 = 13 marks)**

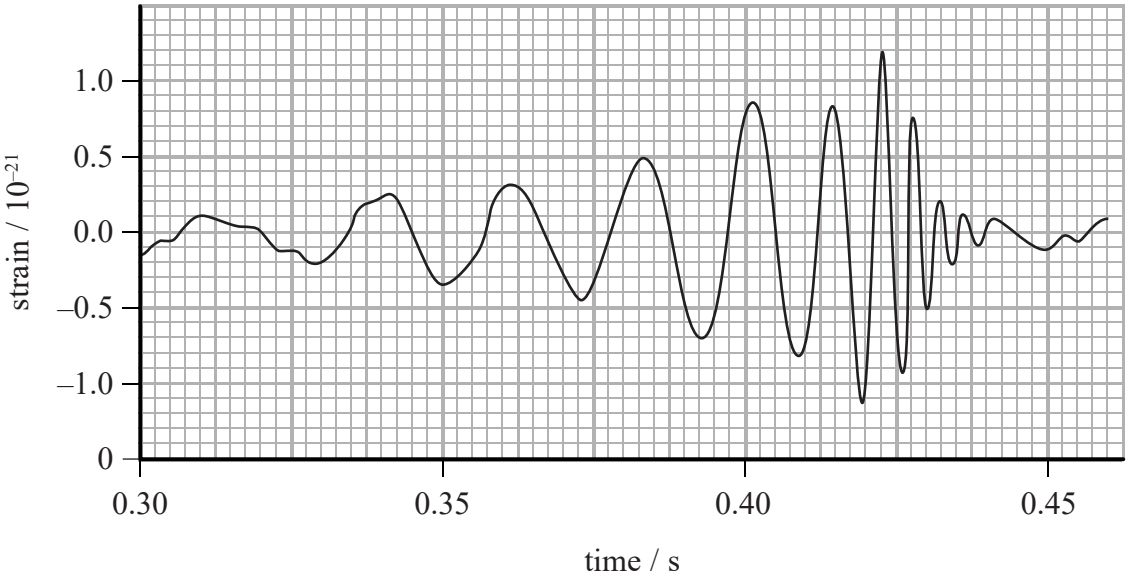
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**20** In 2016 scientists at the Laser Interferometer Gravitational-Wave Observatory (LIGO) announced that gravitational waves had been detected.

The signal they detected is shown on the graph.




(a) Gravitational waves travel at the speed of light.

Determine the mean wavelength of the waves detected between 0.30 s and 0.35 s on the graph.

**(3)**

*From the graph there are 2 complete waves between 0.30 s and 0.35 s*

*So 2T = 0.05 s, T = 0.025 s*

*f = 1/T = 1 ÷ 0.025 s = 40 Hz*

*v = fλ: λ = 3.00 × $10^{8}$ m $s^{-1}$ ÷ 40 Hz = 7.5 × $10^{6}$ m*

Mean wavelength = *7.5 × $10^{6}$ m*

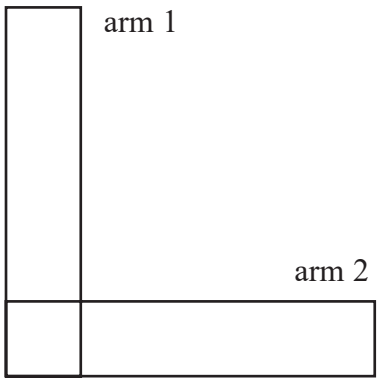
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(b) Gravitational waves alternately compress and stretch matter by very small amounts as they pass through.

The LIGO detector has two arms, at 90° to each other, each 4 km long. As a gravitational wave passes the detector, the arms change length. The detector continuously compares the lengths of the two arms.




(i) An article states that 'the maximum change in the 4 km length of the arm is about 0.001 times the diameter of a proton'.

Determine whether this statement applies to the gravitational wave shown in the graph.

diameter of proton = $8.8 \times 10^{-16}$ m

**(3)**

Maximum strain from the graph = $1.2 \times 10^{-21}$

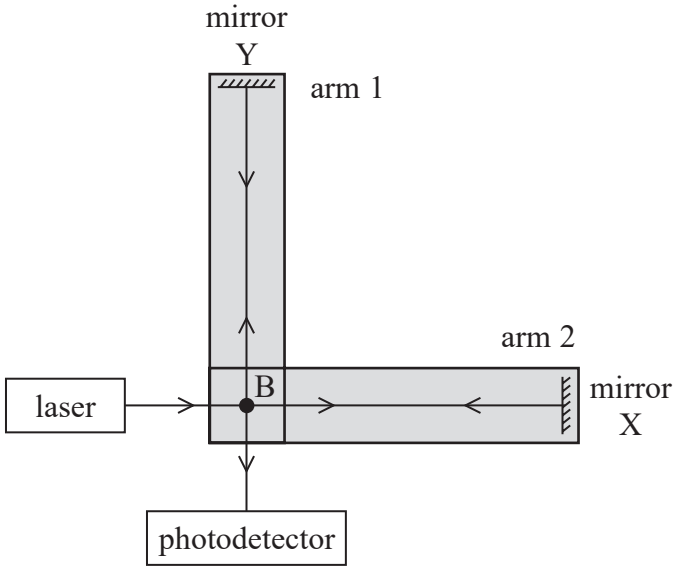
Strain = $\Delta L/L$, so $\Delta L = 1.2 \times 10^{-21} \times 4000$ m = $4.8 \times 10^{-18}$ m

0.001 × proton diameter = $0.001 \times 8.8 \times 10^{-16}$ m = $8.8 \times 10^{-19}$ m

$4.8 \times 10^{-18}$ m is about 5.5 times bigger (0.0055 proton diameters), so the statement does not apply to this wave.

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(ii) In the LIGO detector, any change in the lengths of the arms is detected using a laser beam and photodetector.




The laser beam is split into two at B, one beam travelling to one mirror and the other beam travelling to the other mirror. After reflection at the mirrors, the beams are recombined at B and reach the photodetector. The photodetector measures the intensity of the incident light.

The system is arranged so that when no gravitational waves are present, the beams have a path difference of half a wavelength at the photodetector.

Explain how the photodetector detects very small changes in the length of one arm, when the other arm stays the same length.

**(4)**

With a path difference of half a wavelength the two beams arrive at the photodetector in antiphase.

So destructive interference takes place and the resultant amplitude is zero, so no light (no signal) is detected.

If one arm changes length the path difference changes, so the phase difference between the beams changes and they are no longer in antiphase.

The interference is no longer completely destructive, so light reaches the photodetector and a signal is detected.

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(iii) The system could be arranged so that when no gravitational waves are present, the beams have zero path difference at the photodetector.

Explain whether using an initial path difference of half a wavelength is a more sensitive way of detecting changes in length than having an initial path difference of zero.

**(2)**

*With zero path difference there is constructive interference, so there is a maximum signal at the photodetector.*

*A small change in length gives a change from maximum amplitude that is a very small percentage, so it is hard to detect. A change from zero (no light to some light) is easy to detect, so half a wavelength is more sensitive.*

**(Total for Question 20 = 12 marks)**

**TOTAL FOR PAPER = 90 MARKS**

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## List of data, formulae and relationships

| | | |
|---|---|---|
| Acceleration of free fall | $g = 9.81 \text{ m s}^{-2}$ | (close to Earth's surface) |
| Boltzmann constant | $k = 1.38 \times 10^{-23} \text{ J K}^{-1}$ | |
| Coulomb law constant | $k = \frac{1}{4\pi\varepsilon_0} = 8.99 \times 10^{9} \text{ N m}^2 \text{ C}^{-2}$ | |
| Electron charge | $e = -1.60 \times 10^{-19} \text{ C}$ | |
| Electron mass | $m_e = 9.11 \times 10^{-31} \text{ kg}$ | |
| Electronvolt | $1 \text{ eV} = 1.60 \times 10^{-19} \text{ J}$ | |
| Gravitational constant | $G = 6.67 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2}$ | |
| Gravitational field strength | $g = 9.81 \text{ N kg}^{-1}$ | (close to Earth's surface) |
| Permittivity of free space | $\varepsilon_0 = 8.85 \times 10^{-12} \text{ F m}^{-1}$ | |
| Planck constant | $h = 6.63 \times 10^{-34} \text{ J s}$ | |
| Proton mass | $m_p = 1.67 \times 10^{-27} \text{ kg}$ | |
| Speed of light in a vacuum | $c = 3.00 \times 10^{8} \text{ m s}^{-1}$ | |
| Stefan-Boltzmann constant | $\sigma = 5.67 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$ | |
| Unified atomic mass unit | $u = 1.66 \times 10^{-27} \text{ kg}$ | |

### Mechanics

Kinematic equations of motion

$$s = \frac{(u + v)t}{2}$$

$$v = u + at$$

$$s = ut + \frac{1}{2}at^2$$

$$v^2 = u^2 + 2as$$

Forces

$$\Sigma F = ma$$

$$g = \frac{F}{m}$$

$$W = mg$$

moment of force $= Fx$

Momentum

$$p = mv$$

Work, energy and power

$$\Delta W = F\Delta s$$

$$E_k = \frac{1}{2}mv^2$$

$$\Delta E_{grav} = mg\Delta h$$

$$P = \frac{E}{t}$$

$$P = \frac{W}{t}$$

$$\text{efficiency} = \frac{\text{useful energy output}}{\text{total energy input}}$$

$$\text{efficiency} = \frac{\text{useful power output}}{\text{total power input}}$$

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## Electric circuits

Potential difference

$$V = \frac{W}{Q}$$

Resistance

$$R = \frac{V}{I}$$

Electrical power and energy

$$P = VI$$

$$P = I^2R$$

$$P = \frac{V^2}{R}$$

$$W = VIt$$

Resistivity

$$R = \frac{\rho l}{A}$$

Current

$$I = \frac{\Delta Q}{\Delta t}$$

$$I = nqvA$$

## Materials

Density

$$\rho = \frac{m}{V}$$

Stokes' law

$$F = 6\pi\eta rv$$

Hooke's law

$$\Delta F = k\Delta x$$

Young modulus

$$\text{Stress } \sigma = \frac{F}{A}$$

$$\text{Strain } \varepsilon = \frac{\Delta x}{x}$$

$$E = \frac{\sigma}{\varepsilon}$$

Elastic strain energy

$$\Delta E_{\text{el}} = \frac{1}{2}F\Delta x$$

## Waves and Particle Nature of Light

Wave speed

$$v = f\lambda$$

Speed of a transverse wave on a string

$$v = \sqrt{\frac{T}{\mu}}$$

Intensity of radiation

$$I = \frac{P}{A}$$

Power of a lens

$$P = \frac{1}{f}$$

$$P = P_1 + P_2 + P_3 + \ldots$$

Thin lens equation

$$\frac{1}{u} + \frac{1}{v} = \frac{1}{f}$$

Magnification for a lens

$$m = \frac{\text{image height}}{\text{object height}} = \frac{v}{u}$$

Diffraction grating

$$n\lambda = d \sin\theta$$

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Refractive index

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$n = \frac{c}{v}$$

Critical angle

$$\sin C = \frac{1}{n}$$

Photon model

$$E = hf$$

Einstein's photoelectric equation

$$hf = \phi + \frac{1}{2}mv^2_{\max}$$

de Broglie wavelength

$$\lambda = \frac{h}{p}$$

**Further mechanics**

Impulse

$$F\Delta t = \Delta p$$

Kinetic energy of a non-relativistic particle

$$E_k = \frac{p^2}{2m}$$

Motion in a circle

$$v = \omega r$$

$$T = \frac{2\pi}{\omega}$$

$$F = ma = \frac{mv^2}{r}$$

$$a = \frac{v^2}{r}$$

$$a = r\omega^2$$

Centripetal force

$$F = \frac{mv^2}{r}$$

$$F = mr\omega^2$$

**Fields**

Coulomb's law

$$F = k\frac{Q_1Q_2}{r^2}$$

$$\text{where } k = \frac{1}{4\pi\varepsilon_0}$$

Electric field strength

$$E = \frac{F}{Q}$$

$$E = k\frac{Q}{r^2}$$

$$E = \frac{V}{d}$$

Electric potential

$$V = k\frac{Q}{r}$$

Capacitance

$$C = \frac{Q}{V}$$

Energy stored in a capacitor

$$W = \frac{1}{2}QV$$

Capacitor discharge

$$Q = Q_0 e^{-t/RC}$$

Resistor – capacitor discharge

$$I = I_0 e^{-t/RC}$$

$$V = V_0 e^{-t/RC}$$

In a magnetic field

$$F = BIl \sin \theta$$

$$F = Bqv \sin \theta$$

Faraday's and Lenz's laws

$$\varepsilon = \frac{-\mathrm{d}(N\phi)}{\mathrm{d}t}$$

Root-mean-square values

$$V_{\text{rms}} = \frac{V_0}{\sqrt{2}}$$

$$I_{\text{rms}} = \frac{I_0}{\sqrt{2}}$$

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## Nuclear and particle physics

In a magnetic field

$$r = \frac{p}{BQ}$$

## Thermodynamics

Heating

$$\Delta E = mc\Delta\theta$$

$$\Delta E = L\Delta m$$

Molecular kinetic theory

$$\frac{1}{2}m\langle c^2\rangle = \frac{3}{2}kT$$

$$pV = \frac{1}{3}Nm\langle c^2\rangle$$

Ideal gas equation

$$pV = NkT$$

Stefan-Boltzmann law

$$L = \sigma AT^4$$

$$L = \sigma 4\pi r^2 T^4$$

Wien's law

$$\lambda_{max} T = 2.898 \times 10^{-3} \text{ m K}$$

## Space

Intensity

$$I = \frac{L}{4\pi d^2}$$

Redshift of electromagnetic radiation

$$z = \frac{\Delta\lambda}{\lambda} \approx \frac{\Delta f}{f} \approx \frac{v}{c}$$

Cosmological expansion

$$v = H_0 d$$

## Nuclear radiation

Mass-energy

$$\Delta E = c^2\Delta m$$

Radioactive decay

$$A = \lambda N$$

$$\frac{dN}{dt} = -\lambda N$$

$$\lambda = \frac{\ln 2}{t_{½}}$$

$$N = N_0 e^{-\lambda t}$$

$$A = A_0 e^{-\lambda t}$$

## Gravitational fields

Gravitational force

$$F = \frac{Gm_1 m_2}{r^2}$$

Gravitational field strength

$$g = \frac{Gm}{r^2}$$

Gravitational potential

$$V_{grav} = \frac{-Gm}{r}$$

## Oscillations

Simple harmonic motion

$$F = -kx$$

$$a = -\omega^2 x$$

$$x = A \cos \omega t$$

$$v = -A\omega \sin \omega t$$

$$a = -A\omega^2 \cos \omega t$$

$$T = \frac{1}{f} = \frac{2\pi}{\omega}$$

$$\omega = 2\pi f$$

Simple harmonic oscillator

$$T = 2\pi\sqrt{\frac{m}{k}}$$

$$T = 2\pi\sqrt{\frac{l}{g}}$$

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