

MARK SCHEME for the October/November 2015 series

9709 MATHEMATICS

9709/71

Paper 7, maximum raw mark 50

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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Cambridge is publishing the mark schemes for the October/November 2015 series for most Cambridge IGCSE[®], Cambridge International A and AS Level components and some Cambridge O Level components.

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	Cambridge International A Level – October/November 2015	9709	71

Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
 - A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
 - B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more “method” steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
 - The symbol ∇ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously “correct” answers or results obtained from incorrect working.

Note: B2 or A2 means that the candidate can earn 2 or 0.

B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
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The following abbreviations may be used in a mark scheme or used on the scripts:

AEF	Any Equivalent Form (of answer is equally acceptable)
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
BOD	Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
CAO	Correct Answer Only (emphasising that no “follow through” from a previous error is allowed)
CWO	Correct Working Only – often written by a ‘fortuitous’ answer
ISW	Ignore Subsequent Working
MR	Misread
PA	Premature Approximation (resulting in basically correct work that is insufficiently accurate)
SOS	See Other Solution (the candidate makes a better attempt at the same question)
SR	Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

MR –1	A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become “follow through ✓” marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy. An MR –2 penalty may be applied in particular cases if agreed at the coordination meeting.
PA –1	This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

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1	$\lambda = (1.2 + 2.3) \div 2$ $= 1.75$ $e^{-1.75} \left(\frac{1.75^2}{2} + \frac{1.75^3}{3!} \right)$ $= 0.421$ (3 sf)	M1 A1 M1 A1 [4]	Attempt combined mean, allow 1.2 + 2.3 Correct mean Allow incorrect mean. Allow end errors (1 and/or 4)
		Total: 4	
2 (i)	$\frac{6}{\sqrt{120}}$ oe seen $\frac{30-29}{\left(\frac{6}{\sqrt{120}}\right)}$ (= 1.826) $P(z > '1.826') = 1 - \Phi('1.826')$ $= 0.034$ (2 sf)	B1 M1 M1 A1 [4]	Or 6 ² /120 oe seen ± Allow without $\sqrt{120}$. No sd/var mix Correct tail consistent with their working 0.0339
(ii)	No n is large (≥ 30) Sample mean is (appr) normally distrib or The CLT applies oe	B1 B1 [2]	1 st B1 for either comment 2 nd B1 for 'No' with 2 nd comment (No mark for 'No' alone)
		Total: 6	
3 (i)	$\frac{3420}{60} (= 57)$ $\frac{60}{59} \left(\frac{195200}{60} - 57^2 \right)$ (= 4.40678) $= 4.41$ (3 sf)	B1 M1 A1 [3]	 Oe As final answer
(ii)	$'57' \pm z \sqrt{\frac{4.40678}{60}}$ $z = 2.326$ [56.4 to 57.6] (3 sf)	M1 B1 A1 [3]	 2.326 – 2.329 (accept 2.33 if no better seen) NB: use of biased variance in (ii) can score in full
		Total: 6	

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4 (i)	$k \int_1^2 (3-x) dx = 1$ $k \left[3x - \frac{x^2}{2} \right]_1^2 = 1$ $(k(6 - 2 - (3 - 0.5)) = 1)$ $k \times 1.5 = 1 \text{ or } k \times \frac{3}{2} = 1 \text{ or } k = \frac{1}{1.5} \text{ oe}$ $k = \frac{2}{3} \text{ AG}$	M1 A1 A1 [3]	Attempt $\int f(x) = 1$, ignore limits or $\frac{k}{2}(h_1 + h_2) = 1$ Correct integration & limits or $\frac{k}{2}(2 + 1) = 1$ No errors seen
(ii)	$\frac{2}{3} \int_1^m (3-x) dx = 0.5 \text{ oe } \int \text{from } m \text{ to } 2$ $\left(\frac{2}{3} \left[3x - \frac{x^2}{2} \right]_1^m = 0.5 \right)$ $\frac{2}{3} \left[3m - \frac{m^2}{2} - 2.5 \right] = 0.5$ $m^2 - 6m + 6.5 = 0 \text{ oe}$ $\left(m = \frac{6 \pm \sqrt{36 - 4 \times 6.5}}{2} = 1.42 \text{ or } 4.58 \right)$ $m = 1.42 \text{ (3 sf)}$	M1* dep M1* A1 A1 [4]	Attempt $\text{Int } f(x) = 0.5$, ignore limits oe Or use of area of trapezium Sub of correct limits into their integral. Or trapezium using 1 and m/m and 2 Any correct 3-term QE = 0 or $(m-3)^2 = 2.5$ or $\frac{6 - \sqrt{10}}{2}$ oe; single correct ans
		Total: 7	

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5	(i)	Po(1.6) stated or implied $P(X > 3) = 1 - e^{-1.6} \left(1 + 1.6 + \frac{1.6^2}{2} + \frac{1.6^3}{3!} \right)$ = 0.0788 (3 sf)	M1 M1 A1 [3]	Allow M1 for $1 - P(X \leq 3)$, incorrect λ and allow one end error SR Use of Bin scores B1 only for 0.0788
	(ii)	$\lambda = \frac{n}{2500}$ $e^{-\frac{n}{2500}} < 0.05$ Allow = Allow incorrect λ $-\frac{n}{2500} < \ln 0.05$ Attempt ln bs $n > 7489.3$ (1 dp) Smallest $n = 7490$	B1 M1 M1 A1 [4]	or $e^{-\mu} < 0.05$ M1 or $\frac{2499}{2500}$ B1 $\left(\frac{2499}{2500} \right)^n < 0.05$ M1 $n \ln \frac{2499}{2500} < \ln 0.05$ M1 Smallest $n = 7488$ A1 $-\mu < \ln 0.05$ M1 $(\mu > 2.9957)$ $n = \mu \times 2500$ B1 Smallest $n = 7490$ A1
			Total: 7	
6	(i)	$E(T) = 9 \times 78 + 7 \times 66$ (= 1164) $\text{Var}(T) = 9 \times 7^2 + 7 \times 5^2$ (= 616) $\frac{1200 - '1164'}{\sqrt{616}}$ (= 1.450) $P(z < 1.450) = \Phi(1.450)$ = 0.927 (3 sf)	B1 B1 M1 M1 A1 [5]	Or $9 \times 78 + 7 \times 66 - 1200$ $\pm$ Allow without $\sqrt{}$ Correct tail consistent with their mean
	(ii)	$E(D) = 66 - 78$ (= -12) $\text{Var}(D) = 7^2 + 5^2$ (= 74) $\frac{0 - ('-12')}{\sqrt{74}}$ (= 1.395) $P(D > 0) = 1 - \Phi('1.395')$ 0.0815 (3 sf)	B1 M1 M1 A1 [4]	Both needed $\pm$ Allow without $\sqrt{}$ Correct tail consistent with their mean Similar scheme for $P(M - W) < 0$
			Total: 9	

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7	(i)	Prob could be different later in day or on a different day oe	B1 [1]	or any explanation why not random or “Not random” or “Not representative”
	(ii)	Looking for decrease (or improvement) H_0 : P(not arrive) = 0.2 H_1 : P(not arrive) < 0.2	B1 B1 [2]	oe Allow “ $p = 0.2$ ”
	(iii)	Concluding that prob has <u>decreased</u> (or publicity has worked) when it hasn’t oe	B1 [1]	In context
	(iv)	$P(X = 0)$ and $P(X = 1)$ attempted $P(X \leq 2) = 0.8^{30} + 30 \times 0.8^{29} \times 0.2 + {}^{30}C_2 \times 0.8^{28} \times 0.2^2$ (= 0.0442) $P(X \leq 3) = 0.8^{30} + 30 \times 0.8^{29} \times 0.2 + {}^{30}C_2 \times 0.8^{28} \times 0.2^2 + {}^{30}C_3 \times 0.8^{27} \times 0.2^3$ = 0.123 cr is $X \leq 2$ $P(\text{Type I}) = 0.0442$ (3 sf)	M1 M1 B1 A1 A1 [5]	B(30, 0.2) Not nec’y added May be implied by calc $P(X \leq 2)$ or $P(X \leq 3)$ Attempt $P(X \leq 2)$ Or ‘0.0442’ + ${}^{30}C_3 \times 0.8^{27} \times 0.2^3 = 0.123$
	(v)	3 is outside cr No evidence that p has decreased (or that publicity has worked)	M1 A1 ✓ [2]	Comparison of 3 with their cr or $P(X \leq 3) = 0.123$ which is > 0.05 Correct conclusion. No contradictions
			Total: 11	
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1	(i)	N(352, ...) Variance = 2.9	B1 B1	[2]	no recovery in (ii) for each B mark accept sd = $\sqrt{2.9} = 1.70(29)$ stated
	(ii)	$\frac{354 - 352}{\sqrt{2.9}} \quad (= 1.174)$ $1 - \Phi(1.174)$ $= 0.120$ (3 sf)	M1 M1 A1	[3]	with their mean and var Or $\frac{354.05 - 352}{\sqrt{2.9}}$ or correct restart $(= 1.204)$ (accept sd/var mix)1 $-\Phi(1.204)$ $= 0.114$ (3 sf) Incorrect cc can score M1M1A0
Total				[5]	
2		$(\Phi^{-1}(0.99) =) 2.326$ seen N(λ , λ) seen or implied $\frac{55.5 - \lambda}{\sqrt{\lambda}} = + "2.326"$ $\lambda + "2.326" \sqrt{\lambda} - 55.5 = 0$ $\sqrt{\lambda} = \frac{-"2.326" \pm \sqrt{"2.326"}^2 + 4 \times 55.5}}{2}$ $(= 6.377.. \text{ or } - 8.703..)$ $\lambda = 40.7$ (3 sf)	B1 M1 M1 M1 A1	[5]	must be Φ^{-1} , not Φ allow with wrong or no cc & $\Phi(0.99)$ (= 0.8389) must = "z" or attempt at z (0.99 / 0.01 M0) for correct method of solving their quad in $\sqrt{\lambda}$ and squaring to find λ cao, one ans only Without cc, $\lambda = 40.2$: lose final A1
Total				[5]	
3	(i)	0.4 or 2/5 or 26/65	B1	[1]	no recovery in (ii) for the B mark
	(ii)	"0.4" + $z \times \sqrt{\frac{0.4 \times 0.6}{65}} = 0.516$ oe $z = \left(0.116 \times \sqrt{\frac{65}{0.4 \times 0.6}} \right) = 1.909$ $(\Phi(1.909) = 0.97(18))$ $2(0.97 - 1)$ $\alpha = 94$	M1 A1 M1 A1	[4]	or "0.4" - $z \times \sqrt{\frac{0.4 \times 0.6}{65}} = 0.284$ or $z \times \sqrt{\frac{0.4 \times 0.6}{65}} = 0.116$ oe for fully correct method to find α from their z allow 94.36 or 94.4 or 94.374
Total				[5]	

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4	(i)	$k \int_{-2}^2 (4 - x^2) dx = 1$ $k \left[4x - \frac{x^3}{3} \right]_{-2}^2 = 1$ $\left(k \left(8 - \frac{8}{3} - \left(-8 - \left(-\frac{8}{3} \right) \right) \right) \right)$ $k \times \frac{32}{3} = 1$ oe Not e.g. $k \times 10.7 = k$ $k = \frac{3}{32}$ AG	M1 A1 A1	 [3]	attempt Integral $f(x) = 1$, ignore limits correct integration & limits exact answer correctly found
	(ii)	Inverted parabola, vertex on y axis $E(X) = 0$	B1 B1	 [2]	parabola must finish on x axis at ± 2 , labelled (ignore markings on y axis)
	(iii)	$\frac{3}{32} \int_{-2}^1 (4 - x^2) dx$ $\frac{3}{32} \left[4x - \frac{x^3}{3} \right]_{-2}^1$ $\frac{3}{32} \left(4 - \frac{1}{3} - \left(-8 - \left(-\frac{8}{3} \right) \right) \right)$ $= \frac{27}{32}$ or 0.844 (3 sf)	M1 A1 A1	 [3]	or $1 - \frac{3}{32} \int_1^2 (4 - x^2) dx$ ignore limits or $1 - \frac{3}{32} \left[4x - \frac{x^3}{3} \right]_1^2$ correct integration and correct limits $= 1 - \frac{3}{32} \left(8 - \frac{8}{3} - \left(4 - \frac{1}{3} \right) \right)$
Total				[8]	

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5 (a)	$\lambda = 4.5$ $e^{-4.5} \quad (= 0.011109)$ $\left(\frac{99}{100}\right)^{450} \quad (= 0.010860)$ $\left(\frac{0.011109 - 0.010860}{0.010860} \times 100\right)$ $= 2.29\% \text{ (3 sf)}$	B1 M1 M1 A1	[4]	alone allow any λ
(b)	$H_0: P(6) = \frac{1}{6} \text{ or } p = \frac{1}{6}$ $H_1: P(6) < \frac{1}{6} \text{ or } p < \frac{1}{6}$ $\left(\frac{5}{6}\right)^{25} + 25\left(\frac{5}{6}\right)^{24} \times \frac{1}{6} + {}^{25}C_2 \left(\frac{5}{6}\right)^{23} \times \left(\frac{1}{6}\right)^2$ $= 0.189 \text{ (3 sf)}$ comp 0.1 No reason to believe die biased	B1 M1 A1 M1 A1	[5]	Both needed allow one error (extra term / missing term / incorrect term) CR method: attempt at least P(0) and P(0 and 1) (0.010... and 0.06... < 0.1) CR is 0,1 and must see 0.189 for A1 valid comp '0.189' with 0.1 oe valid comparison of 2 with CR correct conclusion, ✓ their 0.189 no contradictions
Total			[9]	
6 (i)	$H_0: \mu = 2.60$ $H_1: \mu > 2.60$ $\pm \frac{2.64 - 2.6}{0.2 \div \sqrt{75}}$ $= \pm 1.732$ '1.732' > 1.645 Reject H_0 . There is evidence that μ has increased	B1 M1 A1 B1 ✓	[4]	allow pop mean, not just 'mean' accept $\pm 1.73 \text{ (3 sf)}$ valid comparison with 1.645 (or 0.0416 < 0.05) and correct conclusion ✓ their 1.732 no contradictions (or CV method $x_{crit} = 2.638$ M1A1 comp 2.64 > 2.638 and concln B1 ✓) SR two tail test, using 1.96 (or using 0.025) can score B0M1A1B1ft max 3/4

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(ii)	$\frac{x - 2.6}{0.2 \div \sqrt{75}} = 1.645 \quad (x = 2.638)$ $\pm \frac{2.638 - 2.68}{0.2 \div \sqrt{75}}$ $= \pm 1.819$ $\Phi(-1.819) = 1 - \Phi(1.819)$ $= 0.0345 \text{ or } 0.0344$	M1 M1 A1 M1 A1	[5]	for standardising with their “ 2.638 “ using 2.68 accept 1.82 (3 sf) indep M mark, calculate correct area/prob consistent with their working
Total			[9]	
7 (i)	est $\mu = 2.087$ est $\sigma^2 = \frac{100}{99} \left(\frac{435.57}{100} - 2.087^2 \right)$ = 0.000132(3232) or 131/99 0000	B1 M1 A1	[3]	allow 2.09 1/99 (435.57 – 208.7 ² /100) without $\frac{100}{99}$: 0.000131 M0A0
(ii)	$E(Y - X) = 2.12 - 2.087 (= 0.033)$ $\text{Var}(Y - X) = 0.000144 + '0.00013232'$ = 0.000276(32) $\frac{0.01 - '0.033'}{\sqrt{0.00027632}} (= -1.384)$ $\Phi(-1.384) = 1 - \Phi(1.384)$ = 0.0832	B1 M1 A1 M1 M1 A1	[6]	or 2.12 – 2.087 – 0.01 for $Y - X - 0.01 < 0$ allow 2.09 for 2.087 or $\sqrt{(0.012^2 + '0.00013232')}$ M1 = 0.016623 A1 $\sqrt{\text{their } E(Y - X) \text{ \& Var}(Y - X)}$ var must be a combination of the two vars correct area/prob consistent with their working SR use of biased var (0.000131) in (i) and (ii) scores in (ii) B1M1 A1 for 0.000275 and M1M1 A1 for 0.0827 (6/6 available)
Total			[9]	
	Total for paper		[50]	