

Please write clearly in block capitals.

Centre number

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Candidate number

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Surname *StemUp Model Solution*

Forename(s)

Candidate signature

GCSE MATHEMATICS

H

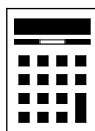
Higher Tier Paper 2 Calculator

Thursday 8 November 2018 Morning Time allowed: 1 hour 30 minutes

Materials

For this paper you must have:

- a calculator
- mathematical instruments.



Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.

Advice

In all calculations, show clearly how you work out your answer.

For Examiner's Use	
Pages	Mark
2–3	
4–5	
6–7	
8–9	
10–11	
12–13	
14–15	
16–17	
18–19	
20–21	
22–23	
TOTAL	



N 0 V 1 8 8 3 0 0 2 H 0 1

Answer **all** questions in the spaces provided

- 1** What does $(A \cap B)$ represent in $P(A \cap B)$?
Circle your answer.

[1 mark]

A or B or both

A but not B

not A and not B

A and B

- 2** P is $(4, 9)$ and Q is $(-2, 1)$
Circle the midpoint of PQ .

[1 mark]

(1, 5)

(3, 4)

(3, 5)

(6, 8)

- 3** Which of these is a geometric progression?
Circle your answer.

[1 mark]

1 3 5 7 9

1 3 6 10 15

1 4 9 16 25

1 3 9 27 81



- 4 The bearing of A from B is 310°
Circle the bearing of B from A .

[1 mark]

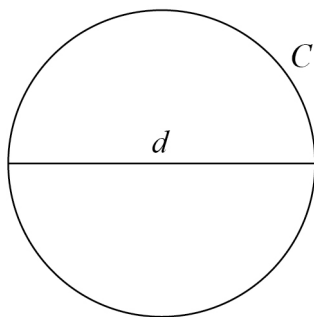
050°

110°

130°

220°

- 5 A circle has circumference C and diameter d .



$$C = kd$$

What **value** does the constant k represent?

[1 mark]

Answer _____ π _____



- 6 Here is some information about 20 trains leaving a station.

Number of minutes late, t	Number of trains	Midpoint	$f \times x$
$0 \leq t < 5$	12	2.5	30
$5 \leq t < 10$	7	7.5	52.5
$10 \leq t < 15$	1	12.5	12.5
$t \geq 15$	0	—	0

- 6 (a) Work out an estimate of the mean number of minutes late.

[3 marks]

$$\Sigma fx = 2.5 \times 12 + 7.5 \times 7 + 12.5 \times 1$$

$$= 30 + 52.5 + 12.5 = 95$$

$$\text{Mean} = 95 \div 20$$

$$= 4.75$$

Answer 4.75 minutes



- 6 (b)** The station manager looks at the information in more detail.

Number of minutes late, t	Number of trains
$0 \leq t < 2$	12
$2 \leq t < 4$	0
$4 \leq t < 6$	7
$6 \leq t < 8$	0
$8 \leq t < 10$	0
$10 \leq t < 12$	1

He works out an estimate of the mean using this information.

How does his estimate compare with the answer to part (a)?

Tick **one** box.

[1 mark]

☐

Higher than part (a)

☐

Same as part (a)

☒

Lower than part (a)

☐

Not possible to tell

Turn over for the next question

Turn over ►



7

Work out the values of a and b in the identity

$$5(7x + 8) + 3(2x + b) \equiv ax + 13$$

[4 marks]

$$5(7x + 8) + 3(2x + b) = 35x + 40 + 6x + 3b$$

$$= 41x + 40 + 3b$$

$$\text{Compare } x \text{ terms: } a = 41$$

$$\text{Compare numbers: } 40 + 3b = 13$$

$$3b = -27$$

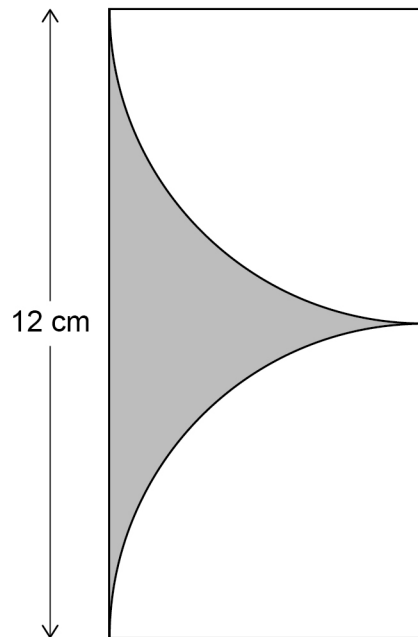
$$b = -9$$

$$a = \underline{\quad 41 \quad} \quad b = \underline{\quad -9 \quad}$$



8

Two identical quarter circles are cut from a rectangle as shown.

Not drawn
accurately

Work out the shaded area.

[4 marks]

$$\text{Radius of each quarter circle} = 12 \div 2 = 6 \text{ cm}$$

$$\text{Rectangle} = 12 \times 6 = 72 \text{ cm}^2$$

$$\text{Two quarter circles} = \pi \times 6^2 \div 2 = 18\pi = 56.5486\dots$$

$$\text{Shaded area} = 72 - 18\pi$$

$$= 15.4513\dots$$

$$\text{Answer } \underline{15.45} \text{ cm}^2$$

Turn over ►



9

The diagrams show the position of a tap when off and fully on.

The tap is fully on when the angle of turn is 180°

Off



Fully on



When fully on, water flows out of the tap at 14 litres per minute.

The rate at which water flows out is in direct proportion to the angle of turn.

The tap is turned 135°



The water flows into a tank with a capacity of 79.8 litres.

Will it take **less than** $7\frac{1}{2}$ minutes to fill the tank?

You **must** show your working.

[4 marks]

$$\text{Flow rate} = 135 \div 180 \times 14$$

$$= 10.5 \text{ litres per minute}$$

$$\text{Time to fill} = 79.8 \div 10.5$$

$$= 7.6 \text{ minutes } (= 7 \text{ minutes } 36 \text{ seconds})$$

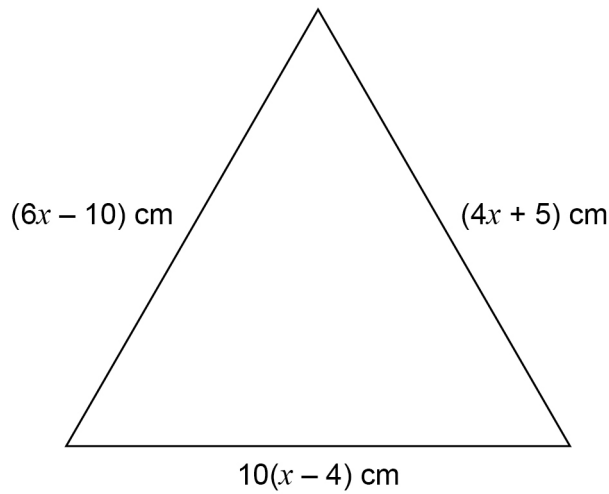
7.6 minutes is more than 7.5 minutes

No, it will take more than $7\frac{1}{2}$ minutes.



10

This triangle is equilateral.

Not drawn
accurately

Is the perimeter of the triangle greater than one metre?

You **must** show your working.**[5 marks]**

$$\text{Equilateral, so } 6x - 10 = 4x + 5$$

$$6x - 4x = 5 + 10$$

$$2x = 15$$

$$x = 7.5$$

$$\text{Side} = 4 \times 7.5 + 5 = 35 \text{ cm} \quad (6 \times 7.5 - 10 = 35, \quad 10(7.5 - 4) = 35)$$

$$\text{Perimeter} = 3 \times 35 = 105 \text{ cm}$$

$$1 \text{ metre} = 100 \text{ cm} \text{ and } 105 \text{ cm} > 100 \text{ cm}$$

Yes, the perimeter is greater than one metre.



- 11 An approximation for the value of π is given by

$$4 \left(1 - \frac{22}{57} + \frac{22}{85} - \frac{22}{105} + \frac{22}{117} - \frac{22}{242} \right)$$

Use your calculator to show that this approximation is within 0.1 of 3.14

[2 marks]

$$4 \times (1 - 22 \div 57 + 22 \div 85 - 22 \div 105 + 22 \div 117 - 22 \div 242)$$

$$= 3.04183961...$$

$$3.14 - 3.0418... = 0.0981...$$

$$0.0981... < 0.1$$

so the approximation is within 0.1 of 3.14

- 12 Work out

$$\frac{9.12 \times 10^{10}}{3.2 \times 10^4}$$

Give your answer in standard form.

[2 marks]

$$9.12 \div 3.2 = 2.85$$

$$10^{10} \div 10^4 = 10^6$$

Answer 2.85×10^6



13

Ashraf is going to put boxes into a crate.

The crate is a cuboid measuring 2.5 m by 2 m by 1.2 m

Each box is a cube of length 50 cm

He does these calculations.

volume of crate	=	$2.5 \times 2 \times 1.2$
	=	6 m^3
volume of one box	=	$0.5 \times 0.5 \times 0.5$
	=	0.125 m^3
number of boxes	=	$6 \div 0.125$
	=	48

He claims,

“I can put 48 boxes in the crate.”

Evaluate Ashraf's method **and** claim.

[2 marks]

His method does not work: $1.2 \div 0.5 = 2.4$, which is not a

whole number, so the boxes do not fit the crate exactly.

Only 2 layers fit: $2.5 \div 0.5 = 5$, $2 \div 0.5 = 4$, $5 \times 4 \times 2 = 40$

His claim is wrong: he can only fit 40 boxes, not 48.

14

The cross section of a prism has n sides.

Circle the expression for the number of edges of the prism.

[1 mark]

$2n$

$3n$

$n + 2$

$2n + 3$

Turn over ►



15

The volume of a medal is 45 cm^3

The medal is made from copper and tin.

$\text{volume of copper} : \text{volume of tin} = 22 : 3$

The density of copper is 8.96 g/cm^3

The density of tin is 7.31 g/cm^3

Work out the mass of the medal.

[4 marks]

$$\text{Total parts} = 22 + 3 = 25$$

$$\text{One part} = 45 \div 25 = 1.8 \text{ cm}^3$$

$$\text{Copper: } 22 \times 1.8 = 39.6 \text{ cm}^3 \quad \text{Tin: } 3 \times 1.8 = 5.4 \text{ cm}^3$$

$$\text{Mass of copper} = 39.6 \times 8.96 = 354.816 \text{ g}$$

$$\text{Mass of tin} = 5.4 \times 7.31 = 39.474 \text{ g}$$

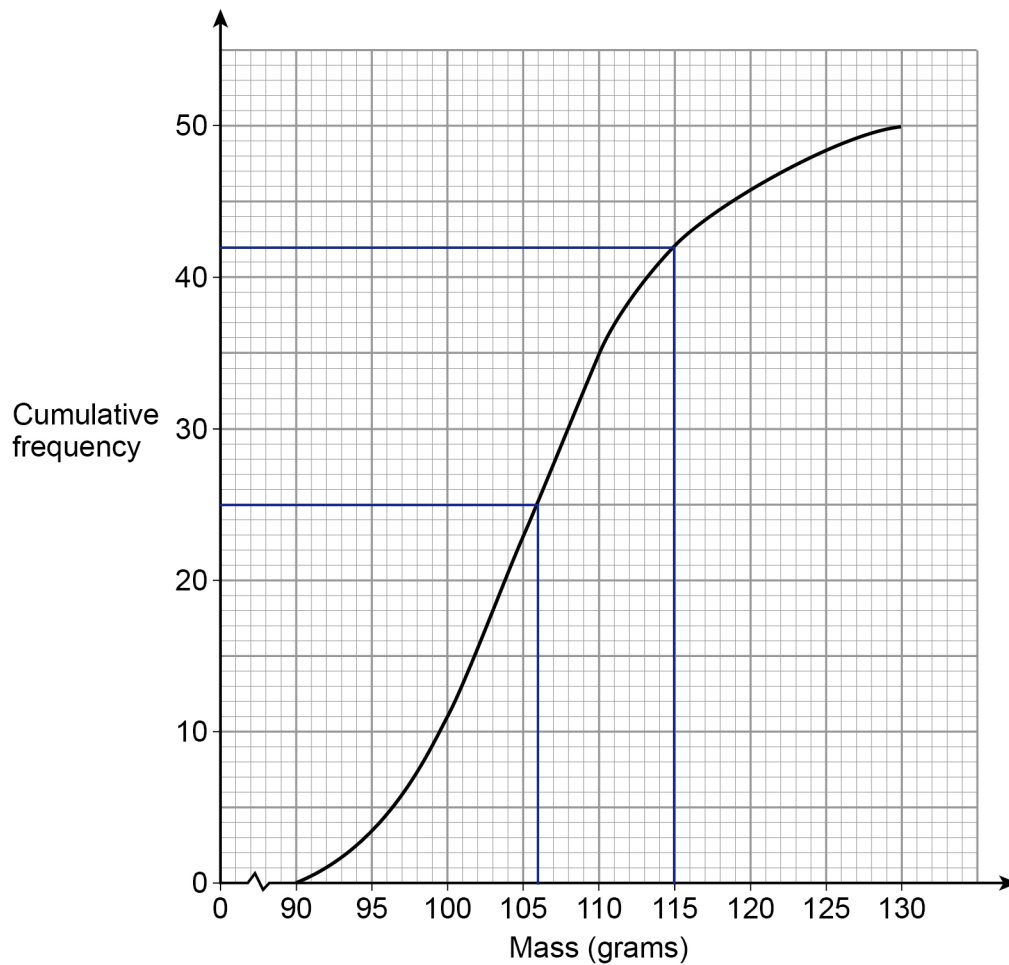
$$\text{Total mass} = 354.816 + 39.474$$

$$= 394.29$$

Answer 394.29 grams



- 16** The cumulative frequency graph shows information about the masses of 50 apples.



- 16 (a)** Use the graph to estimate the median mass of the apples.

[1 mark]

Answer 106 grams

- 16 (b)** Estimate the proportion of the apples that have a mass greater than 115 grams.

[2 marks]

At 115 g, cumulative frequency = 42

$50 - 42 = 8$ apples, $8 \div 50 = 0.16$

Answer 0.16



17

 a is a prime number. b is an even number.

$$N = a^2 + ab$$

Circle the correct statement about N .

[1 mark]

could be
even or odd

always even

always prime

always odd

18

A bag contains 20 discs.

10 are red, 7 are blue and 3 are green.

18 (a)

Marnie takes a disc at random before putting it back in the bag.

Nick then takes a disc at random before putting it back in the bag.

Olly then takes a disc at random.

Work out the probability that they all take a red disc.

[2 marks]

$$\frac{10}{20} \times \frac{10}{20} \times \frac{10}{20} = \frac{1000}{8000} = \frac{1}{8}$$

Answer $\frac{1}{8}$



18 (b)

All 20 discs are in the bag.

Reggie takes three discs at random, one after the other.

After he takes a disc he does **not** put it back in the bag.

Reggie's first disc is blue.

Work out the probability that all three discs are different colours.

[3 marks]*Blue taken: 19 discs left, 10 red, 6 blue, 3 green*

$$P(\text{red then green}) = \frac{10}{19} \times \frac{3}{18} = \frac{30}{342}$$

$$P(\text{green then red}) = \frac{3}{19} \times \frac{10}{18} = \frac{30}{342}$$

$$P(\text{all different}) = \frac{30}{342} + \frac{30}{342} = \frac{60}{342} = \frac{10}{57}$$

Answer $\frac{10}{57}$

Turn over ►

19

Lunch

Choose one starter and one main course

There are four starters and ten main courses to choose from.

Two of the starters and three of the main courses are suitable for vegans.

What percentage of the possible lunches have **both** courses suitable for vegans?**[3 marks]**

$$\text{Possible lunches} = 4 \times 10 = 40$$

$$\text{Vegan lunches} = 2 \times 3 = 6$$

$$6 \div 40 \times 100 = 15$$

Answer 15 %

20

 n is a positive integer.Prove algebraically that $2n^2\left(\frac{3}{n} + n\right) + 6n(n^2 - 1)$ is a cube number.**[3 marks]**

Expand both brackets:

$$\frac{6n^2}{n} + 2n^3 + 6n^3 - 6n$$

$$= 6n + 2n^3 + 6n^3 - 6n$$

$$= 8n^3 = (2n)^3$$

 $2n$ is an integer, so this is a cube number.

- 21 y is inversely proportional to $\sqrt{x}$
 $y = 4$ when $x = 9$

- 21 (a) Work out an equation connecting y and x .

[3 marks]

$$y = \frac{k}{\sqrt{x}}$$

$$4 = \frac{k}{\sqrt{9}} = \frac{k}{3}$$

$$k = 4 \times 3 = 12$$

Answer $y = \frac{12}{\sqrt{x}}$

- 21 (b) Work out the value of y when $x = 25$

[2 marks]

$$y = \frac{12}{\sqrt{25}} = \frac{12}{5}$$

Answer 2.4

Turn over for the next question



22

Simplify fully

$$\frac{x^5 - 4x^3}{3x - 6}$$

[3 marks]

$$x^5 - 4x^3 = x^3(x^2 - 4) = x^3(x + 2)(x - 2)$$

$$3x - 6 = 3(x - 2)$$

$$\frac{x^3(x + 2)(x - 2)}{3(x - 2)} = \frac{x^3(x + 2)}{3}$$

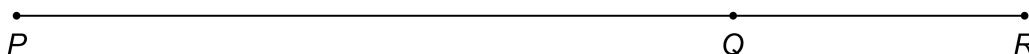
Answer $\frac{x^3(x + 2)}{3}$

23

 PQR is a straight line.

$$PQ : QR = 3 : 1$$

$$\overrightarrow{PQ} = \mathbf{a}$$

Not drawn
accuratelyCircle the vector $\overrightarrow{RQ}$

[1 mark]

$$\frac{1}{3} \mathbf{a}$$

$$\frac{1}{4} \mathbf{a}$$

$$\boxed{-\frac{1}{3} \mathbf{a}}$$

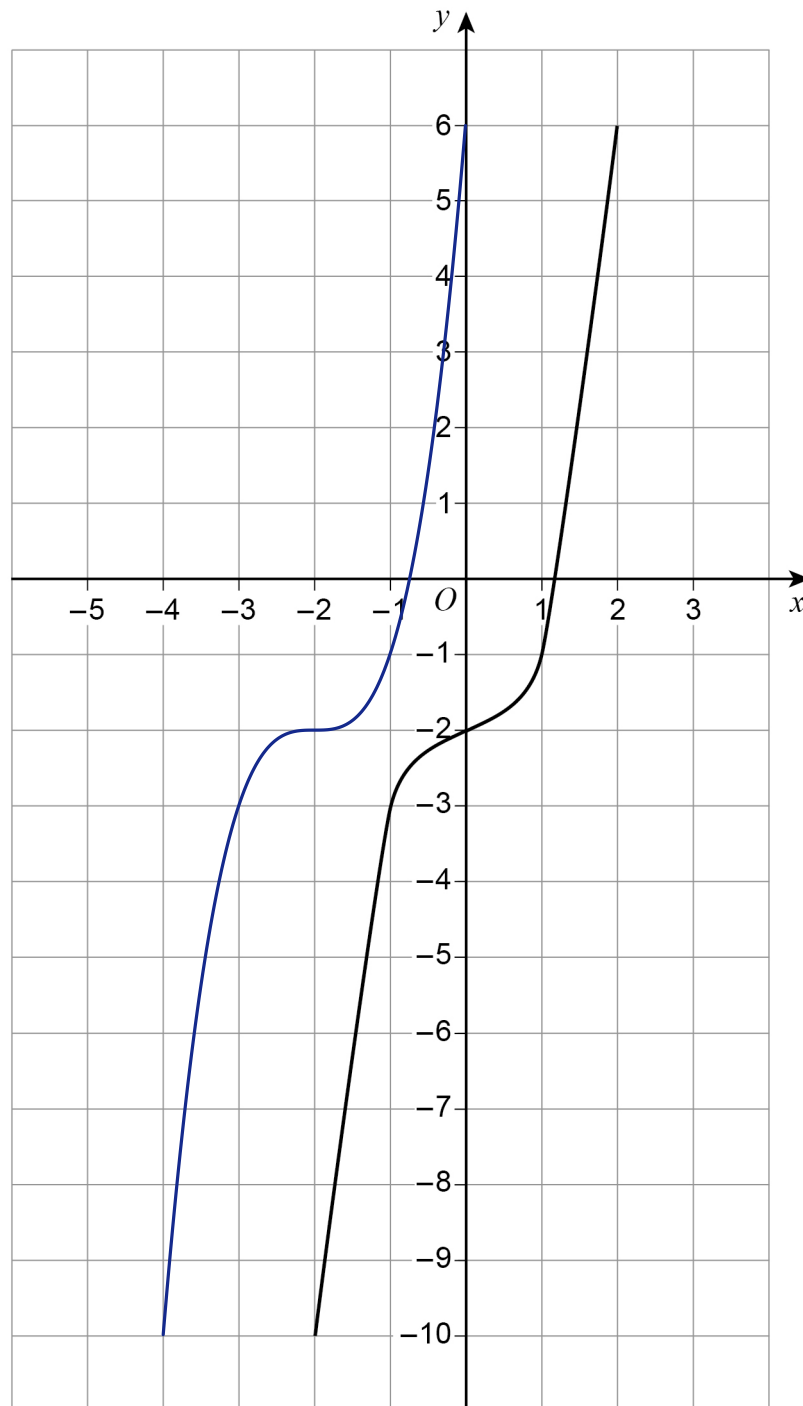
$$-\frac{1}{4} \mathbf{a}$$



24

Here is a sketch of $y = f(x)$

The curve passes through the points

 $(-2, -10)$ $(-1, -3)$ $(0, -2)$ $(1, -1)$ $(2, 6)$ On the grid, sketch the curve $y = f(x + 2)$

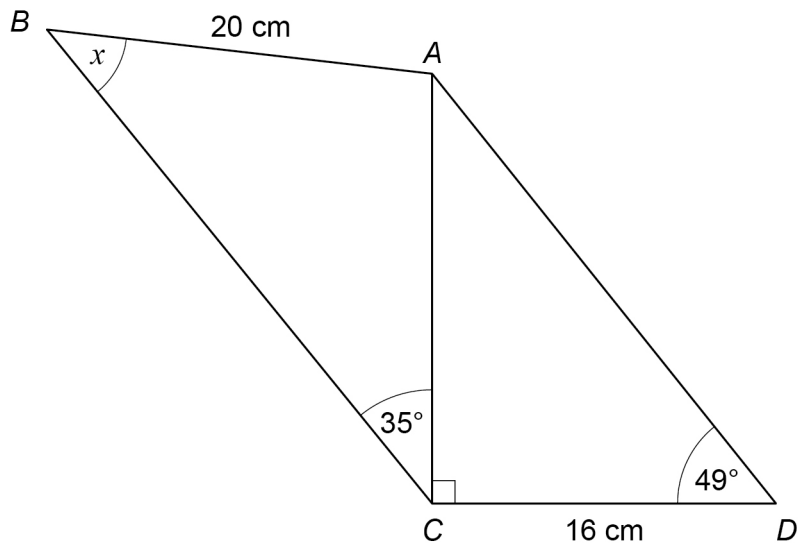
[2 marks]

6

Turn over ►



25

 ABC and ACD are triangles.Not drawn
accuratelyWork out the size of angle x .**[5 marks]**

$$\text{Triangle } ACD: \tan 49^\circ = AC \div 16$$

$$AC = 16 \times \tan 49^\circ = 18.4058... \text{ cm}$$

Triangle ABC , sine rule:

$$\frac{\sin x}{18.4058...} = \frac{\sin 35^\circ}{20}$$

$$\sin x = 18.4058... \times \sin 35^\circ \div 20 = 0.52786...$$

$$x = \sin^{-1}(0.52786...) = 31.8609...$$

Answer 31.9 degrees

26

$$f(x) = \frac{x}{x+2}$$

$$g(x) = x^2 - 2$$

Work out $fg(x)$ Give your answer in the form $a + bx^n$ where a , b and n are integers.**[3 marks]**

$$fg(x) = f(x^2 - 2) = \frac{x^2 - 2}{x^2 - 2 + 2}$$

$$= \frac{x^2 - 2}{x^2} = \frac{x^2}{x^2} - \frac{2}{x^2}$$

$$= 1 - 2x^{-2}$$

Answer $1 - 2x^{-2}$

27

The point $\left(3, \frac{1}{64}\right)$ lies on the curve $y = k^{-x}$ where k is a constant.Show that the point $\left(\frac{1}{2}, \frac{1}{2}\right)$ lies on the curve.**[3 marks]**

$$\frac{1}{64} = k^3 \quad \text{so} \quad k = \frac{1}{4} = 0.25$$

$$\text{When } x = 0.5: y = 0.25^{0.5} = \sqrt{0.25} = 0.5$$

$$y = \frac{1}{2} \text{ when } x = \frac{1}{2}, \text{ so the point lies on the curve.}$$



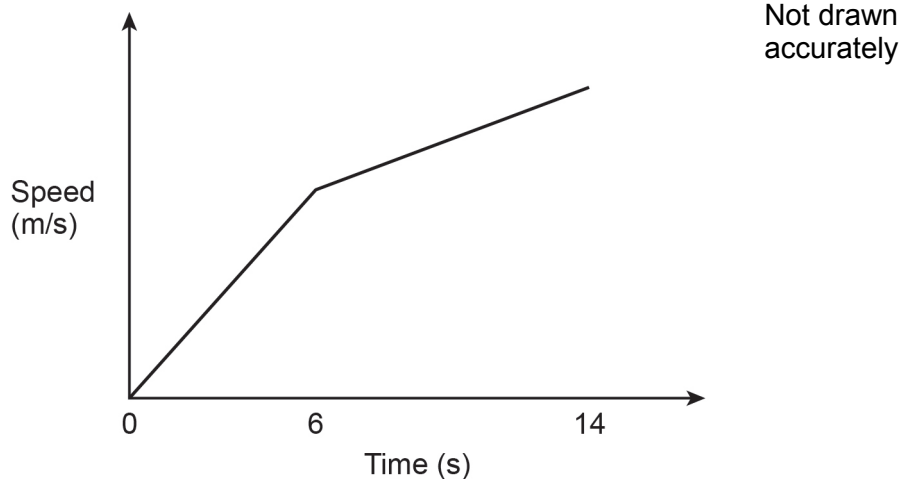
28 Izzy runs an 80-metre race in 14 seconds.

During the first 6 seconds her speed increases at a constant rate.

During the last 8 seconds her speed increases at a different constant rate.

Her speed at 14 seconds is 2 m/s more than her speed at 6 seconds.

Here is a sketch of her speed-time graph.



28 (a) Work out her acceleration during the last 8 seconds.

State the units of your answer.

[2 marks]

$$\text{Acceleration} = \text{gradient} = 2 \div 8$$

$$= 0.25$$

Answer 0.25 m/s²



28 (b) When Izzy finishes the 80-metre race, her speed is v m/s

Work out the value of v .

[4 marks]

Let the speed at 6 s be u m/s, so at 14 s it is $u + 2$

Distance = area under graph = 80

$$\frac{1}{2} \times 6 \times u + \frac{1}{2} \times 8 \times (u + u + 2) = 80$$

$$3u + 8u + 8 = 80$$

$$11u = 72, \quad u = 72 \div 11 = 6.5454\dots$$

$$v = u + 2 = 94 \div 11 = 8.5454\dots$$

$$v = 8.55 \text{ (3 s.f.)}$$

Answer 8.55

END OF QUESTIONS



There are no questions printed on this page

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outside the
box*

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