AQA

Please write clearly in block capitals.

Centre number | | | | | | Candidate number | | | | |

Surname StemUp Model Solution

Forename(s) _____

Candidate signature _____

I declare this is my own work.

A-level MATHEMATICS

Paper 1

Wednesday 3 June 2020 Afternoon Time allowed: 2 hours

Materials
- You must have the AQA Formulae for A-level Mathematics booklet.
- You should have a graphical or scientific calculator that meets the requirements of the specification.

Instructions
- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer each question in the space provided for that question. If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information
- The marks for questions are shown in brackets.
- The maximum mark for this paper is 100.

Advice
- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

For Examiner's Use	
Question	Mark
1	
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TOTAL	

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Answer **all** questions in the spaces provided.

1 The first three terms, in ascending powers of x, of the binomial expansion of $(9+2x)^{\frac{1}{2}}$ are given by

$$(9+2x)^{\frac{1}{2}} \approx a + \frac{x}{3} - \frac{x^2}{54}$$

where a is a constant.

1 (a) State the range of values of x for which this expansion is valid.

Circle your answer.

[1 mark]

$|x| < \frac{2}{9}$ $\quad$ $|x| < \frac{2}{3}$ $\quad$ $|x| < 1$ $\quad$ (circled) $|x| < \frac{9}{2}$

1 (b) Find the value of a.

Circle your answer.

[1 mark]

1 $\quad$ 2 $\quad$ (circled) 3 $\quad$ 9

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2 A student is searching for a solution to the equation $f(x) = 0$

He correctly evaluates

$$f(-1) = -1 \text{ and } f(1) = 1$$

and concludes that there must be a root between -1 and 1 due to the change of sign.

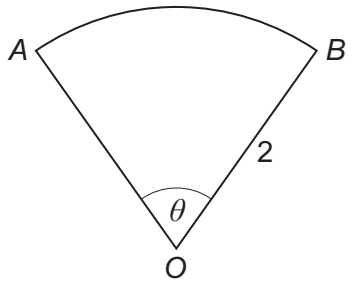
Select the function $f(x)$ for which the conclusion is **incorrect**.

Circle your answer.

[1 mark]

(circled) $f(x) = \frac{1}{x}$ $\quad f(x) = x$ $\quad f(x) = x^3$ $\quad f(x) = \frac{2x+1}{x+2}$

3 The diagram shows a sector OAB of a circle with centre O and radius 2



The angle AOB is θ radians and the perimeter of the sector is 6

Find the value of θ

Circle your answer.

[1 mark]

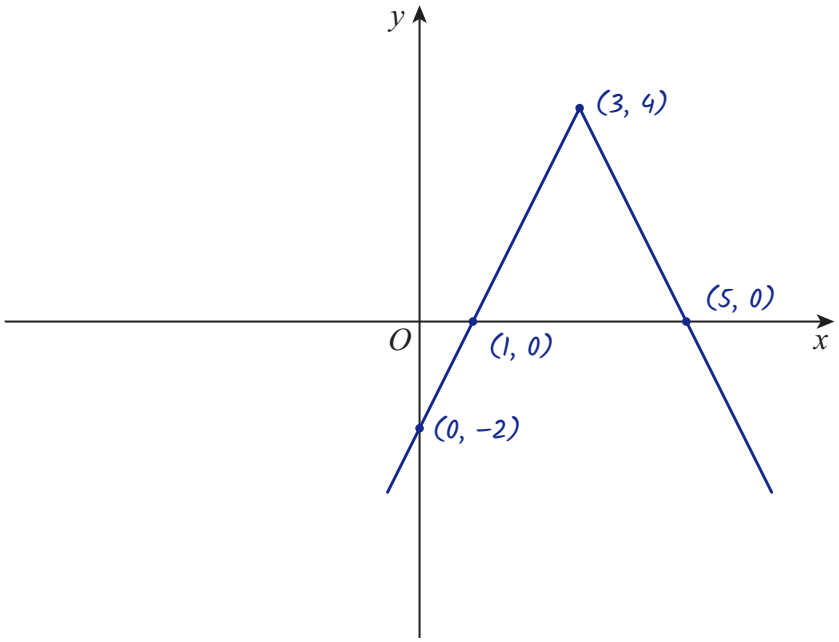
(circled) 1 $\quad \sqrt{3}$ $\quad 2$ $\quad 3$

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4 (a) Sketch the graph of

$$y = 4 - |2x - 6|$$



[3 marks]

4 (b) Solve the inequality

$$4 - |2x - 6| > 2$$

[2 marks]

$4 - |2x - 6| > 2 \Rightarrow |2x - 6| < 2$

$-2 < 2x - 6 < 2$

$4 < 2x < 8$

$2 < x < 4$

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5 Prove that, for integer values of n such that $0 \leq n < 4$

$$2^{n+2} > 3^n$$

[2 marks]

Proof by exhaustion: the integers with $0 \leq n < 4$ are 0, 1, 2, 3

$n = 0$: $2^2 = 4$, $3^0 = 1$, $4 > 1$ true

$n = 1$: $2^3 = 8$, $3^1 = 3$, $8 > 3$ true

$n = 2$: $2^4 = 16$, $3^2 = 9$, $16 > 9$ true

$n = 3$: $2^5 = 32$, $3^3 = 27$, $32 > 27$ true

Hence $2^{n+2} > 3^n$ for all integer values of n such that $0 \leq n < 4$

Turn over for the next question

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6 Four students, Tom, Josh, Floella and Georgia are attempting to complete the indefinite integral

$$\int \frac{1}{x}\,\mathrm{d}x \qquad \text{for } x > 0$$

Each of the students' solutions is shown below:

Tom $\int \frac{1}{x}\,\mathrm{d}x = \ln x$

Josh $\int \frac{1}{x}\,\mathrm{d}x = k \ln x$

Floella $\int \frac{1}{x}\,\mathrm{d}x = \ln Ax$

Georgia $\int \frac{1}{x}\,\mathrm{d}x = \ln x + c$

6 (a) (i) Explain what is wrong with Tom's answer.

[1 mark]

Tom has not included an arbitrary constant of integration (+ c).

6 (a) (ii) Explain what is wrong with Josh's answer.

[1 mark]

Josh's constant is in the wrong place: it multiplies ln x instead of being added. Differentiating k ln x gives $\frac{k}{x}$, not $\frac{1}{x}$ (unless k = 1).

6 (b) Explain why Floella and Georgia's answers are equivalent.

[2 marks]

ln Ax = ln A + ln x (laws of logs)

A is an arbitrary constant, so ln A is also a constant.

Letting c = ln A gives ln Ax = ln x + c,

so Floella's and Georgia's answers are equivalent.

Do not write outside the box

7 Consecutive terms of a sequence are related by

$$u_{n+1} = 3 - (u_n)^2$$

7 (a) In the case that $u_1 = 2$

7 (a) (i) Find u_3

[2 marks]

$u_2 = 3 - (2)^2 = 3 - 4 = -1$

$u_3 = 3 - (-1)^2 = 3 - 1 = 2$

$u_3 = 2$

7 (a) (ii) Find u_{50}

[1 mark]

Terms alternate 2, −1, 2, −1, ... so every even term is −1

$u_{50} = -1$

7 (b) State a different value for u_1 which gives the same value for u_{50} as found in part **(a)(ii)**.

[1 mark]

$u_1 = -2$ $(u_2 = 3 - (-2)^2 = -1$, then $-1, 2, -1, \ldots)$

Turn over for the next question

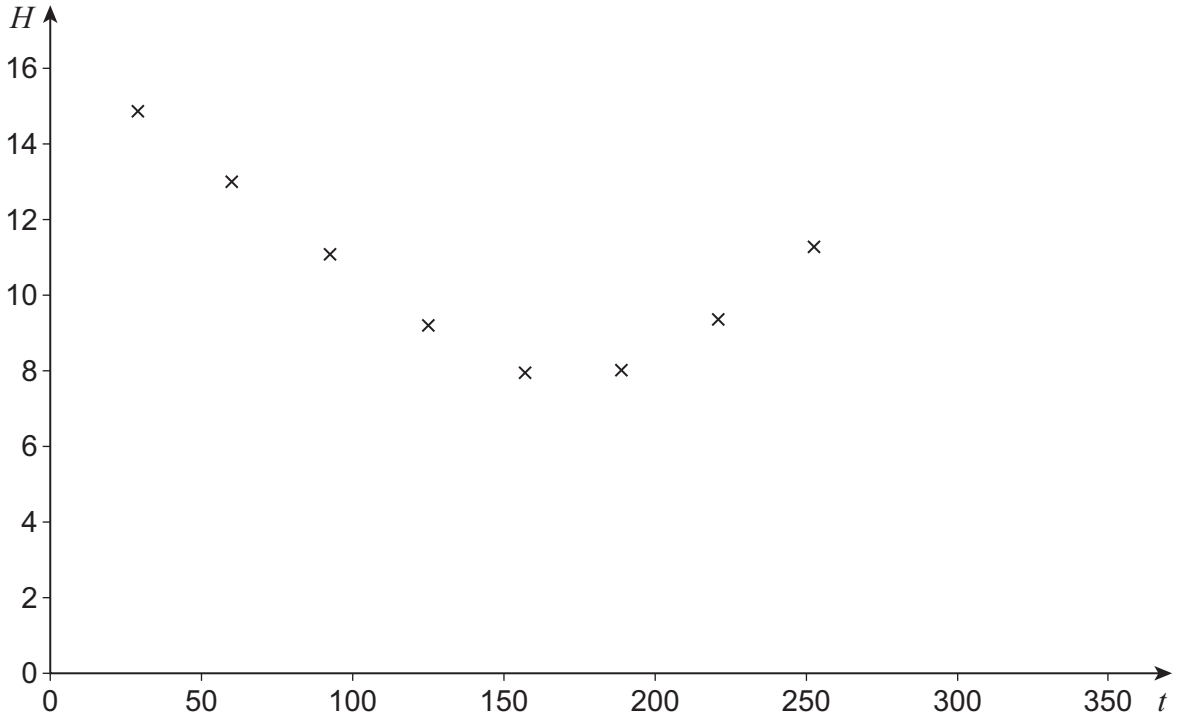
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8 Mike, an amateur astronomer who lives in the South of England, wants to know how the number of hours of darkness changes through the year.

On various days between February and September he records the length of time, H hours, of darkness along with t, the number of days after 1 January.

His results are shown in **Figure 1** below.

Figure 1



Mike models this data using the equation

$$H = 3.87 \sin\left(\frac{2\pi(t + 101.75)}{365}\right) + 11.7$$

8 (a) Find the minimum number of hours of darkness predicted by Mike's model. Give your answer to the nearest minute.

[2 marks]

Minimum when $\sin\left(\frac{2\pi(t + 101.75)}{365}\right) = -1$

$H_{min} = 3.87 \times (-1) + 11.7 = 7.83$ hours

$0.83 \times 60 = 49.8$ minutes

Minimum = 7 hours 50 minutes

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8 (b) Find the maximum number of consecutive days where the number of hours of darkness predicted by Mike's model exceeds 14

[3 marks]

$3.87 \sin\left(\frac{2\pi(t + 101.75)}{365}\right) + 11.7 = 14$

$\sin\left(\frac{2\pi(t + 101.75)}{365}\right) = \frac{2.3}{3.87} = 0.594315...$

$\frac{2\pi(t + 101.75)}{365} = 0.636414...$ or $\pi - 0.636414... = 2.505179...$

$t = -64.78$ or $t = 43.78$

Next interval (add 365 days): $t = 300.22$ or $t = 408.78$

$H > 14$ for $300.22 < t < 408.78$

$408.78 - 300.22 = 108.56$

Maximum number of consecutive days = 108

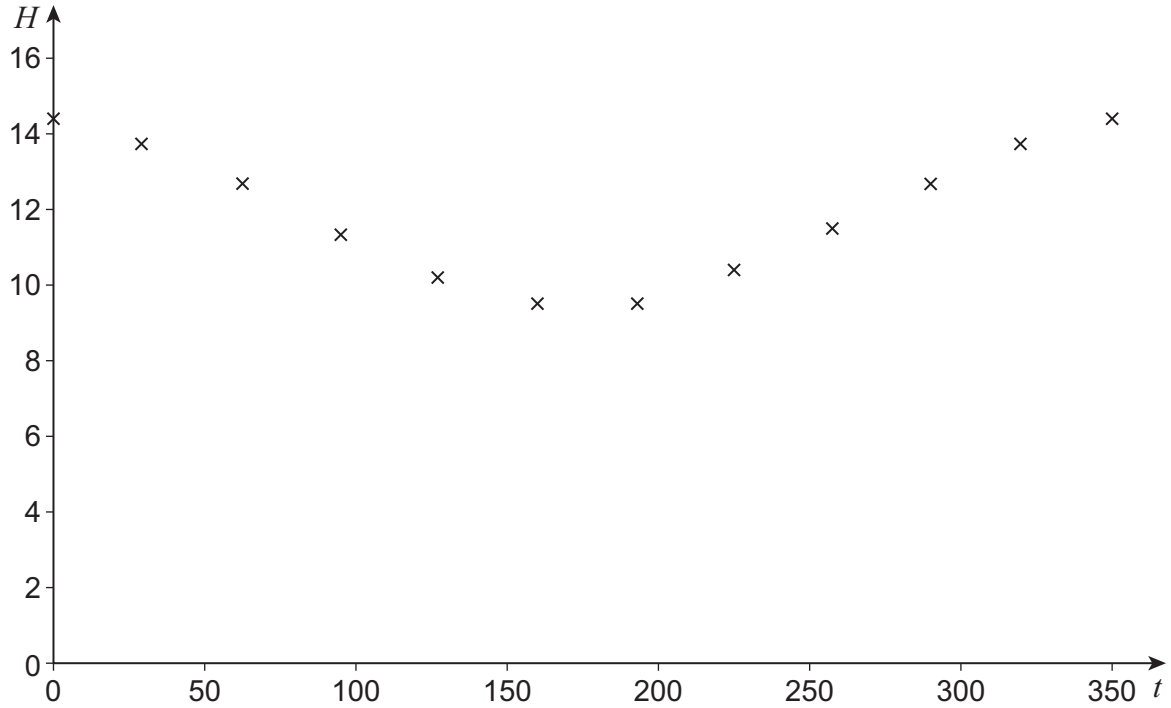
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8 (c) Mike's friend Sofia, who lives in Spain, also records the number of hours of darkness on various days throughout the year.

Her results are shown in **Figure 2** below.

Figure 2



Sofia attempts to model her data by refining Mike's model.

She decides to increase the 3.87 value, leaving everything else unchanged.

Explain whether Sofia's refinement is appropriate.

[2 marks]

Increasing 3.87 would increase the amplitude of the graph, so the range of hours of darkness predicted would increase. Sofia's data has a smaller range (about 9.5 to 14.4 hours) than Mike's, which suggests a lower amplitude, not a higher one. So Sofia's refinement is not appropriate.

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Turn over for the next question

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ANSWER IN THE SPACES PROVIDED

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9 Chloe is attempting to write $\dfrac{2x^2+x}{(x+1)(x+2)^2}$ as partial fractions, with constant numerators.

Her incorrect attempt is shown below.

Step 1 $\dfrac{2x^2+x}{(x+1)(x+2)^2} \equiv \dfrac{A}{x+1} + \dfrac{B}{(x+2)^2}$

Step 2 $2x^2+x \equiv A(x+2)^2 + B(x+1)$

Step 3 Let $x=-1 \Rightarrow A=1$
Let $x=-2 \Rightarrow B=-6$

Answer $\dfrac{2x^2+x}{(x+1)(x+2)^2} \equiv \dfrac{1}{x+1} - \dfrac{6}{(x+2)^2}$

9 (a) (i) By using a counter example, show that the answer obtained by Chloe cannot be correct.

[2 marks]

Let $x = 0$:

$LHS = \dfrac{2(0)^2 + 0}{(0+1)(0+2)^2} = 0$

$RHS = \dfrac{1}{0+1} - \dfrac{6}{(0+2)^2} = 1 - \dfrac{6}{4} = -\dfrac{1}{2}$

$0 \neq -0.5$ so $LHS \neq RHS$

$\therefore$ Chloe's answer must be incorrect.

9 (a) (ii) Explain her mistake in Step 1.

[1 mark]

She should have included an extra term $\dfrac{C}{x+2}$ in Step 1, since

$(x+2)^2$ is a repeated factor in the denominator.

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9 (b) Write $\dfrac{2x^2 + x}{(x+1)(x+2)^2}$ as partial fractions, with constant numerators.

[4 marks]

$\dfrac{2x^2 + x}{(x+1)(x+2)^2} \equiv \dfrac{A}{x+1} + \dfrac{B}{x+2} + \dfrac{C}{(x+2)^2}$

$2x^2 + x \equiv A(x+2)^2 + B(x+1)(x+2) + C(x+1)$

$x = -1$: $2 - 1 = A(1)^2 \Rightarrow A = 1$

$x = -2$: $8 - 2 = C(-1) \Rightarrow C = -6$

Compare x^2 coefficients: $2 = A + B \Rightarrow B = 1$

$\dfrac{2x^2 + x}{(x+1)(x+2)^2} \equiv \dfrac{1}{x+1} + \dfrac{1}{x+2} - \dfrac{6}{(x+2)^2}$

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10 (a) An arithmetic series is given by

$$\sum_{r=5}^{20}(4r+1)$$

10 (a) (i) Write down the first term of the series.

[1 mark]

$r = 5$: $4(5) + 1 = 21$

10 (a) (ii) Write down the common difference of the series.

[1 mark]

$d = 4$

10 (a) (iii) Find the number of terms of the series.

[1 mark]

$20 - 5 + 1 = 16$ terms

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10 (b) A **different** arithmetic series is given by

$$\sum_{r=10}^{100} (br + c)$$

where b and c are constants.

The sum of this series is 7735

10 (b) (i) Show that $55b + c = 85$

[4 marks]

Number of terms $n = 100 - 10 + 1 = 91$

First term $a = 10b + c$, last term $l = 100b + c$

$S = \frac{n}{2}(a + l) = \frac{91}{2}(10b + c + 100b + c) = 7735$

$\frac{91}{2}(110b + 2c) = 7735$

$91(55b + c) = 7735$

$55b + c = \frac{7735}{91} = 85$ as required

Turn over ▶

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10 (b) (ii) The 40th term of the series is 4 times the 2nd term.

Find the values of b and c.

[4 marks]

The kth term has $r = k + 9$

2nd term ($r = 11$): $11b + c$

40th term ($r = 49$): $49b + c$

$49b + c = 4(11b + c)$

$49b + c = 44b + 4c \Rightarrow 5b - 3c = 0$

From (b)(i): $c = 85 - 55b$

$5b - 3(85 - 55b) = 0$

$5b - 255 + 165b = 0 \Rightarrow 170b = 255$

$b = 1.5$

$c = 85 - 55(1.5) = 2.5$

$b = 1.5$, $c = 2.5$

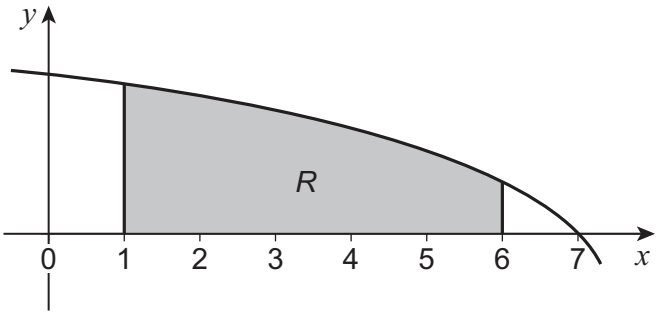
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11 The region R enclosed by the lines $x = 1$, $x = 6$, $y = 0$ and the curve

$$y = \ln(8 - x)$$

is shown shaded in **Figure 3** below.

Figure 3



All distances are measured in centimetres.

11 (a) Use a single trapezium to find an approximate value of the area of the shaded region, giving your answer in cm^2 to two decimal places.

[2 marks]

$f(1) = \ln 7 = 1.945910\ldots$, $f(6) = \ln 2 = 0.693147\ldots$

Area $\approx \frac{1}{2} \times 5 \times (\ln 7 + \ln 2)$

$= 2.5 \ln 14 = 6.59764\ldots$

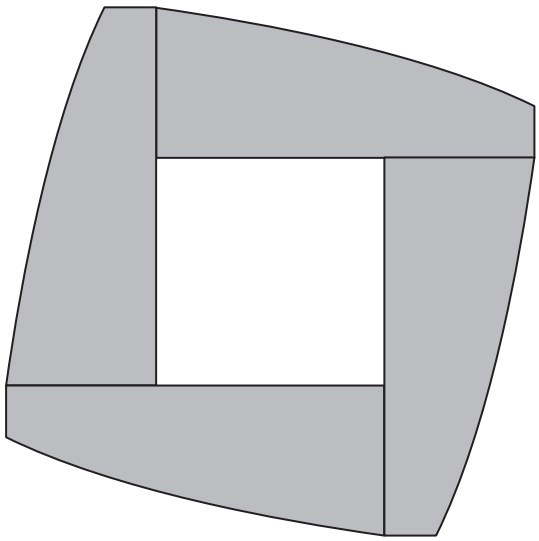
Area $\approx 6.60\ cm^2$

Question 11 continues on the next page

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11 (b) Shape *B* is made from four copies of region *R* as shown in **Figure 4** below.

Figure 4



Shape *B* is cut from metal of thickness 2 mm

The metal has a density of 10.5 g/cm^3

Use the trapezium rule with **six** ordinates to calculate an approximate value of the mass of Shape *B*.

Give your answer to the nearest gram.

[5 marks]

$h = 1$: $x = 1, 2, 3, 4, 5, 6$

$y = \ln 7, \ln 6, \ln 5, \ln 4, \ln 3, \ln 2$

$= 1.9459, 1.7918, 1.6094, 1.3863, 1.0986, 0.6931$

Area of $R \approx \frac{1}{2} \times 1 \times [\ln 7 + \ln 2 + 2(\ln 6 + \ln 5 + \ln 4 + \ln 3)]$

$= \frac{1}{2} \times [2.639057... + 2(5.886104...)]$

$= 7.205632...$ cm^2

Area of $B = 4 \times 7.205632... = 28.82253...$ cm^2

Thickness = 2 mm = 0.2 cm

Volume $= 28.82253... \times 0.2 = 5.764506...$ cm^3

Mass $= 5.764506... \times 10.5 = 60.5273...$ g

Mass ≈ 61 g

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11 (c) Without further calculation, give one reason why the mass found in part **(b)** may be:

11 (c) (i) an underestimate.

[1 mark]

y = ln(8 − x) is concave (it curves downwards), so the tops of the trapezia all lie below the curve and the area of R, and hence the mass, is underestimated.

11 (c) (ii) an overestimate.

[1 mark]

The numbers used in the calculation (the ordinates, and possibly the thickness and density) have been rounded; if they were rounded up, the calculated mass would be too large.

Turn over for the next question

Do not write outside the box

12 A curve C has equation

$$x^3 \sin y + \cos y = Ax$$

where A is a constant.

C passes through the point $P\left(\sqrt{3}, \frac{\pi}{6}\right)$

12 (a) Show that $A = 2$

[2 marks]

$(\sqrt{3})^3 \sin\frac{\pi}{6} + \cos\frac{\pi}{6} = A\sqrt{3}$

$3\sqrt{3} \times \frac{1}{2} + \frac{\sqrt{3}}{2} = A\sqrt{3}$

$2\sqrt{3} = A\sqrt{3}$

$A = 2$ as required

12 (b) (i) Show that $\frac{dy}{dx} = \frac{2 - 3x^2 \sin y}{x^3 \cos y - \sin y}$

[5 marks]

Differentiate implicitly with respect to x (product rule on $x^3 \sin y$):

$3x^2 \sin y + x^3 \cos y \frac{dy}{dx} - \sin y \frac{dy}{dx} = 2$

$\frac{dy}{dx}(x^3 \cos y - \sin y) = 2 - 3x^2 \sin y$

$\frac{dy}{dx} = \frac{2 - 3x^2 \sin y}{x^3 \cos y - \sin y}$ as required

Do not write outside the box

12 (b) (ii) Hence, find the gradient of the curve at P.

[2 marks]

At P: $\frac{dy}{dx} = \frac{2 - 3(\sqrt{3})^2 \sin(\pi/6)}{(\sqrt{3})^3 \cos(\pi/6) - \sin(\pi/6)}$

$= \frac{2 - 4.5}{4.5 - 0.5} = \frac{-2.5}{4}$

Gradient $= -\frac{5}{8}$

12 (b) (iii) The tangent to C at P intersects the x-axis at Q.

Find the exact x-coordinate of Q.

[4 marks]

Tangent at P: $y - \frac{\pi}{6} = -\frac{5}{8}(x - \sqrt{3})$

At Q, $y = 0$: $-\frac{\pi}{6} = -\frac{5}{8}(x - \sqrt{3})$

$x - \sqrt{3} = \frac{8}{5} \times \frac{\pi}{6} = \frac{4\pi}{15}$

$x = \sqrt{3} + \frac{4\pi}{15}$

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13 The function f is defined by

$$\mathrm{f}(x) = \frac{2x+3}{x-2} \qquad x \in \mathbb{R},\ x \neq 2$$

13 (a) (i) Find f^{-1}

[3 marks]

$y = \frac{2x+3}{x-2}$

$xy - 2y = 2x + 3$

$xy - 2x = 2y + 3$

$x(y-2) = 2y + 3$

$x = \frac{2y+3}{y-2}$

$f^{-1}(x) = \frac{2x+3}{x-2}, \quad x \in \mathbb{R},\ x \neq 2$

13 (a) (ii) Write down an expression for $\mathrm{ff}(x)$.

[1 mark]

$f^{-1} = f$ (f is self-inverse), so $ff(x) = x$

Do not write outside the box

13 (b) The function g is defined by

$$g(x) = \frac{2x^2 - 5x}{2} \qquad x \in \mathbb{R},\ 0 \leq x \leq 4$$

13 (b) (i) Find the range of g.

[3 marks]

$g(x) = x^2 - \frac{5}{2}x = (x - \frac{5}{4})^2 - \frac{25}{16}$

Vertex at $x = 1.25$ (in the domain): minimum $g(1.25) = -\frac{25}{16} = -1.5625$

$g(0) = 0$, $g(4) = \frac{2(16) - 5(4)}{2} = 6$

Greatest value is $g(4) = 6$

Range: $\{y : -1.5625 \leq y \leq 6\}$

13 (b) (ii) Determine whether g has an inverse.

Fully justify your answer.

[2 marks]

$g(0) = 0$ and $g(2.5) = \frac{2(6.25) - 12.5}{2} = 0$

so $g(0) = g(2.5)$: g is many-to-one (not one-to-one) on $0 \leq x \leq 4$

$\therefore$ g does not have an inverse.

Do not write outside the box

13 (c) Show that

$$\text{gf}(x) = \frac{48 + 29x - 2x^2}{2x^2 - 8x + 8}$$

[4 marks]

$gf(x) = g\left(\frac{2x+3}{x-2}\right) = \frac{1}{2}\left[2\left(\frac{2x+3}{x-2}\right)^2 - 5\left(\frac{2x+3}{x-2}\right)\right]$

$= \frac{1}{2} \times \frac{2(2x+3)^2 - 5(2x+3)(x-2)}{(x-2)^2}$

$= \frac{2(4x^2 + 12x + 9) - 5(2x^2 - x - 6)}{2(x^2 - 4x + 4)}$

$= \frac{8x^2 + 24x + 18 - 10x^2 + 5x + 30}{2x^2 - 8x + 8}$

$= \frac{48 + 29x - 2x^2}{2x^2 - 8x + 8}$ as required

Do not write outside the box

13 (d) It can be shown that fg is given by

$$\mathrm{fg}(x) = \frac{4x^2 - 10x + 6}{2x^2 - 5x - 4}$$

with domain $\{x \in \mathbb{R} : 0 \leq x \leq 4,\ x \neq a\}$

Find the value of a.

Fully justify your answer.

[2 marks]

fg(x) is undefined when g(x) = 2 (f is not defined at 2),

i.e. when $2x^2 - 5x - 4 = 0$

$x = \frac{5 \pm \sqrt{(25 + 32)}}{4} = \frac{5 \pm \sqrt{57}}{4}$

$\frac{5 - \sqrt{57}}{4} = -0.637... < 0$, not in $0 \leq x \leq 4$, so reject

$\frac{5 + \sqrt{57}}{4} = 3.137...$ which lies in $0 \leq x \leq 4$

$a = \frac{5 + \sqrt{57}}{4}$

Turn over for the next question

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14 The function f is defined by

$$f(x) = 3^x\sqrt{x} - 1 \qquad \text{where } x \geq 0$$

14 (a) $f(x) = 0$ has a single solution at the point $x = \alpha$

By considering a suitable change of sign, show that α lies between 0 and 1

[2 marks]

$f(0) = 3^0 \times \sqrt{0} - 1 = -1 < 0$

$f(1) = 3^1 \times \sqrt{1} - 1 = 2 > 0$

f is continuous for $x \geq 0$ and there is a change of sign,

so α lies between 0 and 1 $(0 < \alpha < 1)$

14 (b) (i) Show that

$$f'(x) = \frac{3^x(1 + x\ln 9)}{2\sqrt{x}}$$

[3 marks]

$f(x) = 3^x x^{1/2} - 1$

Product rule: $\frac{d}{dx}(3^x) = 3^x \ln 3$, $\frac{d}{dx}(x^{1/2}) = \frac{1}{2}x^{-1/2}$

$f'(x) = 3^x \ln 3 \times \sqrt{x} + 3^x \times \frac{1}{2\sqrt{x}}$

$= 3^x\left(\frac{2x \ln 3}{2\sqrt{x}} + \frac{1}{2\sqrt{x}}\right)$

$= 3^x\left(\frac{1 + x \ln 9}{2\sqrt{x}}\right)$ since $2 \ln 3 = \ln 9$

$f'(x) = \frac{3^x(1 + x \ln 9)}{2\sqrt{x}}$ as required

Do not write outside the box

14 (b) (ii) Use the Newton–Raphson method with $x_1 = 1$ to find x_3, an approximation for α.

Give your answer to five decimal places.

[2 marks]

$x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$

$x_2 = 1 - \frac{3 \times 1 - 1}{3(1 + \ln 9) \div 2} = 1 - \frac{4}{3(1 + \ln 9)} = 0.582971...$

$x_3 = 0.582971... - \frac{0.448678...}{2.834029...} = 0.424653...$

$x_3 = 0.42465$

14 (b) (iii) Explain why the Newton–Raphson method fails to find α with $x_1 = 0$

[2 marks]

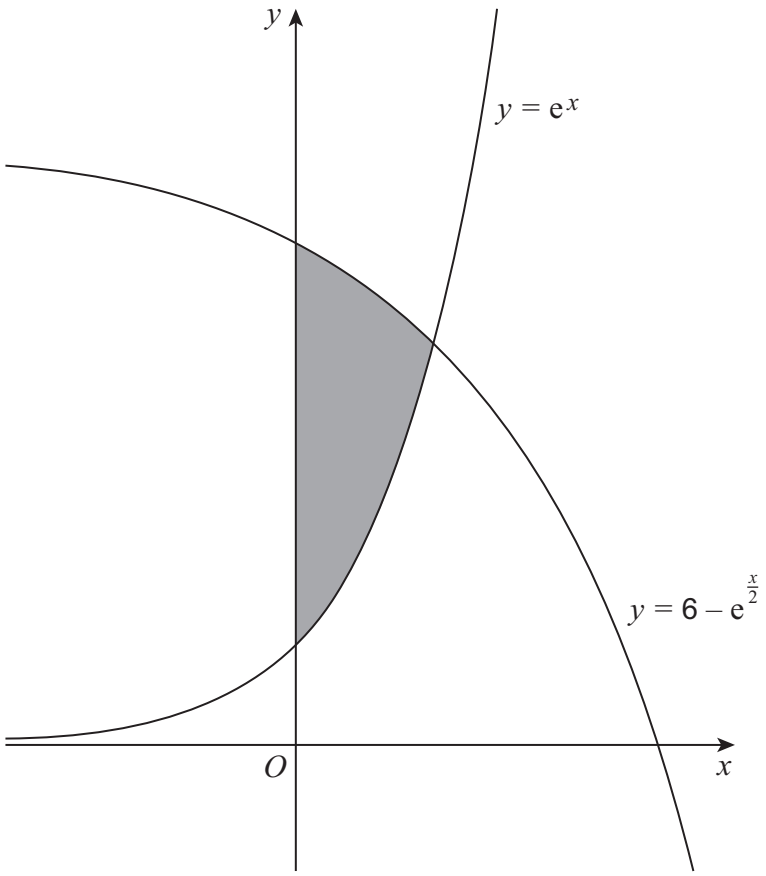
$f'(0)$ is undefined ($2\sqrt{0} = 0$): the tangent to $y = f(x)$ at $x = 0$ is vertical,

so it meets the x-axis at $x = 0$ again: $x_2 = 0$, $x_3 = 0$, ...

All values of x_n would equal 0, so convergence to α is impossible.

Do not write outside the box

15 The region enclosed between the curves $y = e^x$, $y = 6 - e^{\frac{x}{2}}$ and the line $x = 0$ is shown shaded in the diagram below.



Show that the exact area of the shaded region is

$$6 \ln 4 - 5$$

Fully justify your answer.

[10 marks]

Intersection: $e^x = 6 - e^{x/2}$

$e^x + e^{x/2} - 6 = 0$

Let $u = e^{x/2}$: $u^2 + u - 6 = 0$

$(u + 3)(u - 2) = 0 \Rightarrow e^{x/2} = -3$ or $e^{x/2} = 2$

$e^{x/2} > 0$ for all x, so $e^{x/2} = -3$ is not valid

$e^{x/2} = 2 \Rightarrow x/2 = \ln 2 \Rightarrow x = 2 \ln 2 = \ln 4$

Area $= \int_0^{\ln 4} (6 - e^{x/2} - e^x)\, dx$

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$= [\ 6x - 2e^{x/2} - e^{x}\ ]_0^{\ln 4}$

$= (6 \ln 4 - 2e^{(\ln 4)/2} - e^{\ln 4}) - (0 - 2e^{0} - e^{0})$

$= (6 \ln 4 - 2e^{\ln 2} - 4) - (0 - 2 - 1)$

$= (6 \ln 4 - 2 \times 2 - 4) + 3$

$= 6 \ln 4 - 4 - 4 + 3$

$= 6 \ln 4 - 5$ as required

END OF QUESTIONS

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